

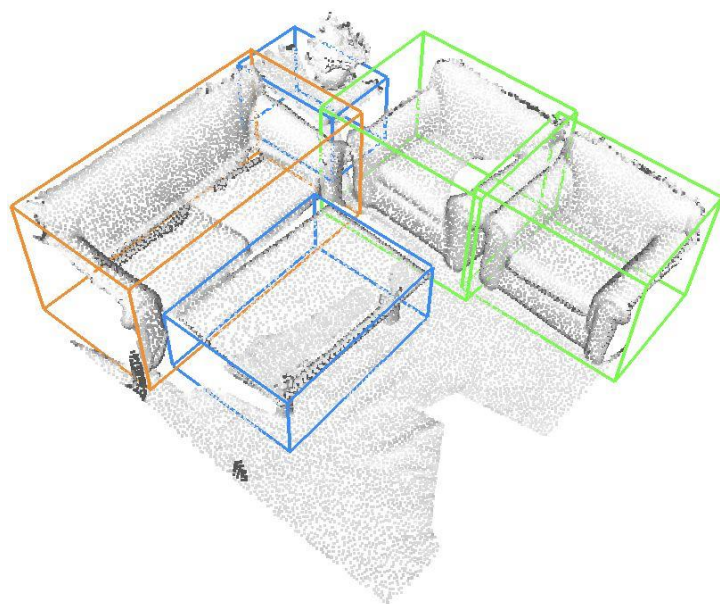
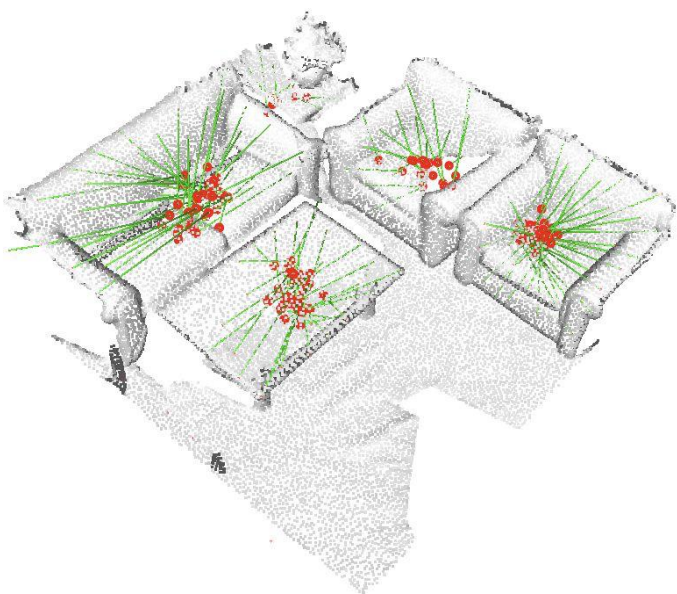
# Course Timetable

|                                      |        | Niloy | Iasonas | Paul | Nils | Leo |
|--------------------------------------|--------|-------|---------|------|------|-----|
| Introduction                         | 9:00   | X     |         |      |      |     |
| Neural Network Basics                | ~9:15  |       | X       |      |      |     |
| Supervised Learning in CG            | ~9:50  | X     |         |      |      |     |
| Unsupervised Learning in CG          | ~10:20 |       |         | X    |      |     |
| <b>Learning on Unstructured Data</b> | ~10:55 |       |         |      |      | X   |
| Learning for Simulation/Animation    | ~11:35 |       |         |      | X    |     |
| Discussion                           | 12:05  | X     | X       | X    | X    | X   |

# Deep Learning for Point Cloud Data



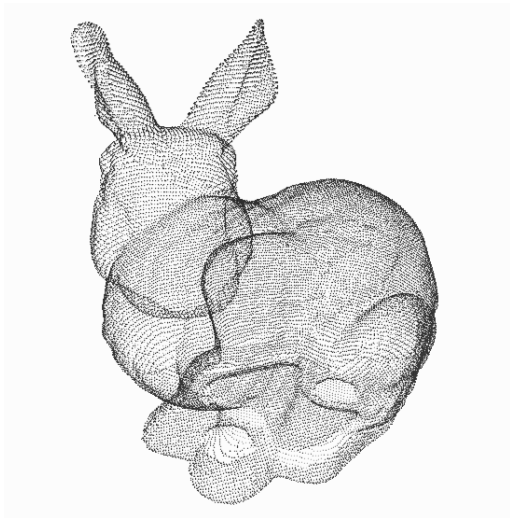
thrive  
**SIGGRAPH2019**  
LOS ANGELES • 28 JULY - 1 AUGUST



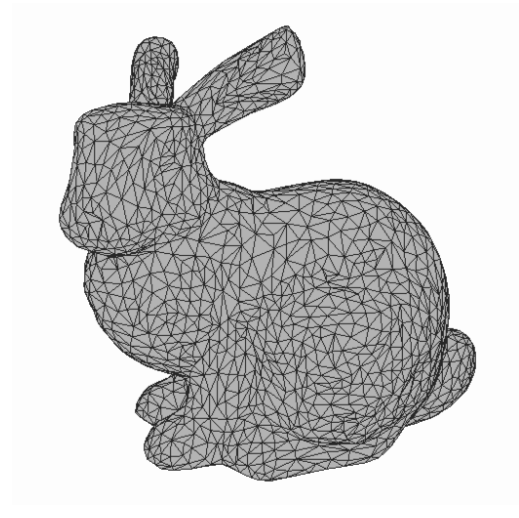
Leonidas Guibas  
Stanford University  
Facebook AI Research



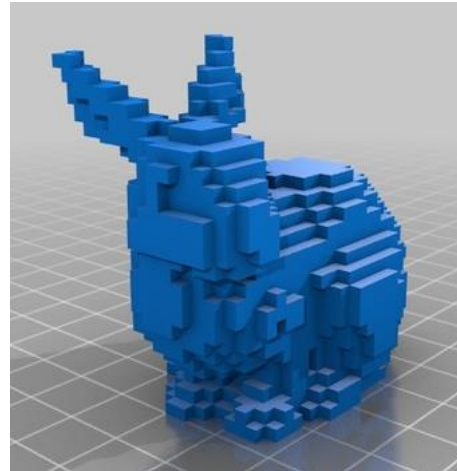
# Multiple 3D Representations



Point Cloud



Surface Mesh



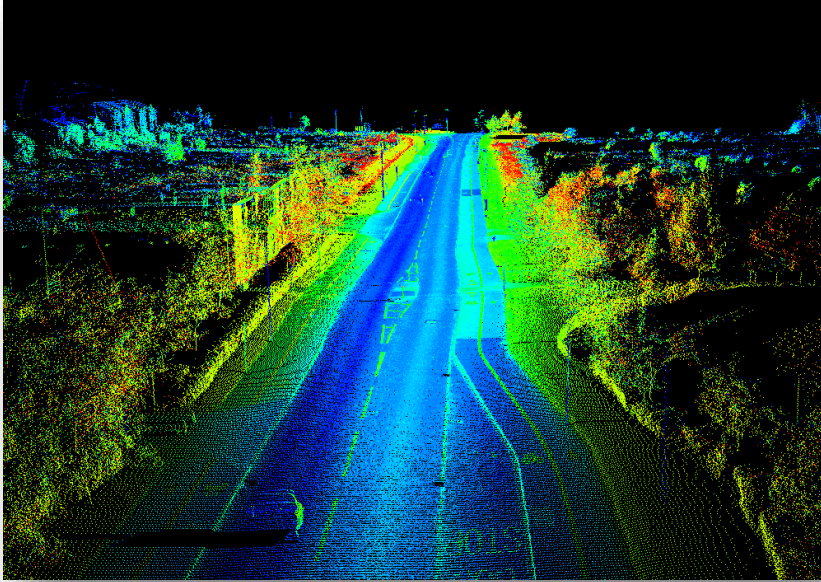
Volumetric



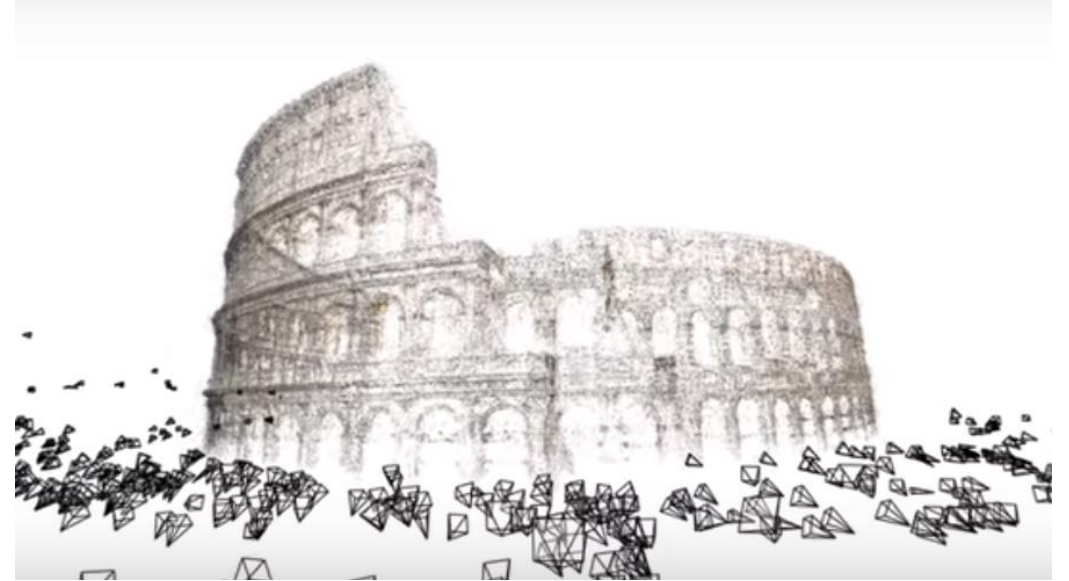
Multi-View  
Images  
RGB(D)

...

# Point Clouds



Lidar point clouds (LizardTech)



Structure from motion (Microsoft)

Depth camera (Intel)



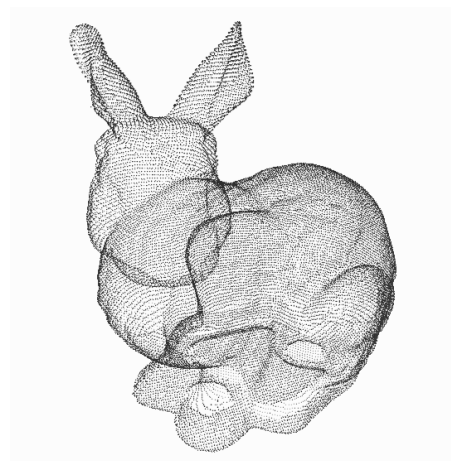
# A Common 3D Representation: Point Cloud



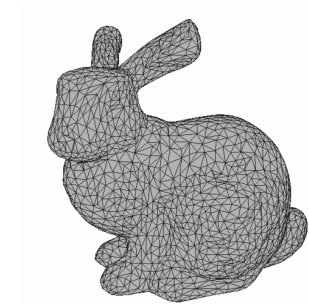
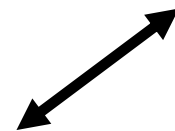
**Point clouds are close to raw sensor data**



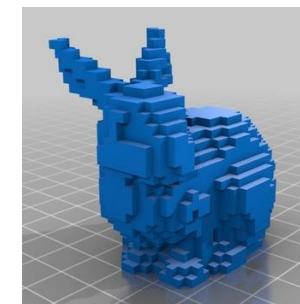
**Point clouds are representationally simple**



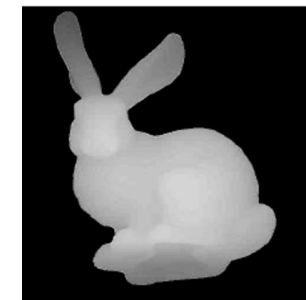
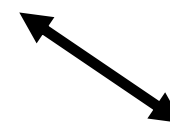
**Point Cloud**



Surface Mesh



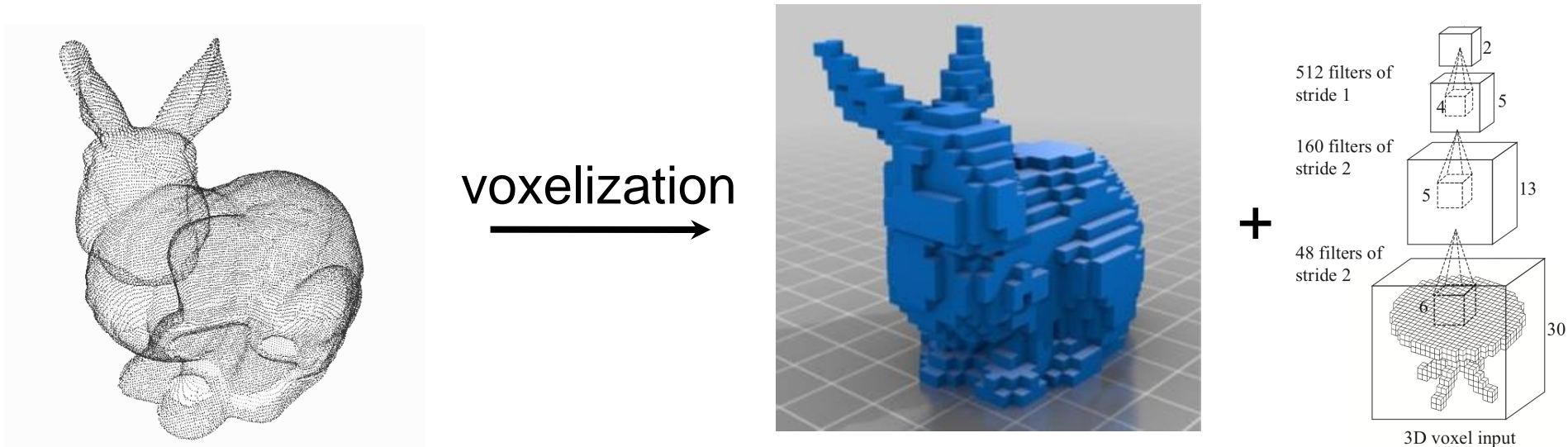
Volumetric



Depth Map  
5

# Early Work on 3D Learning

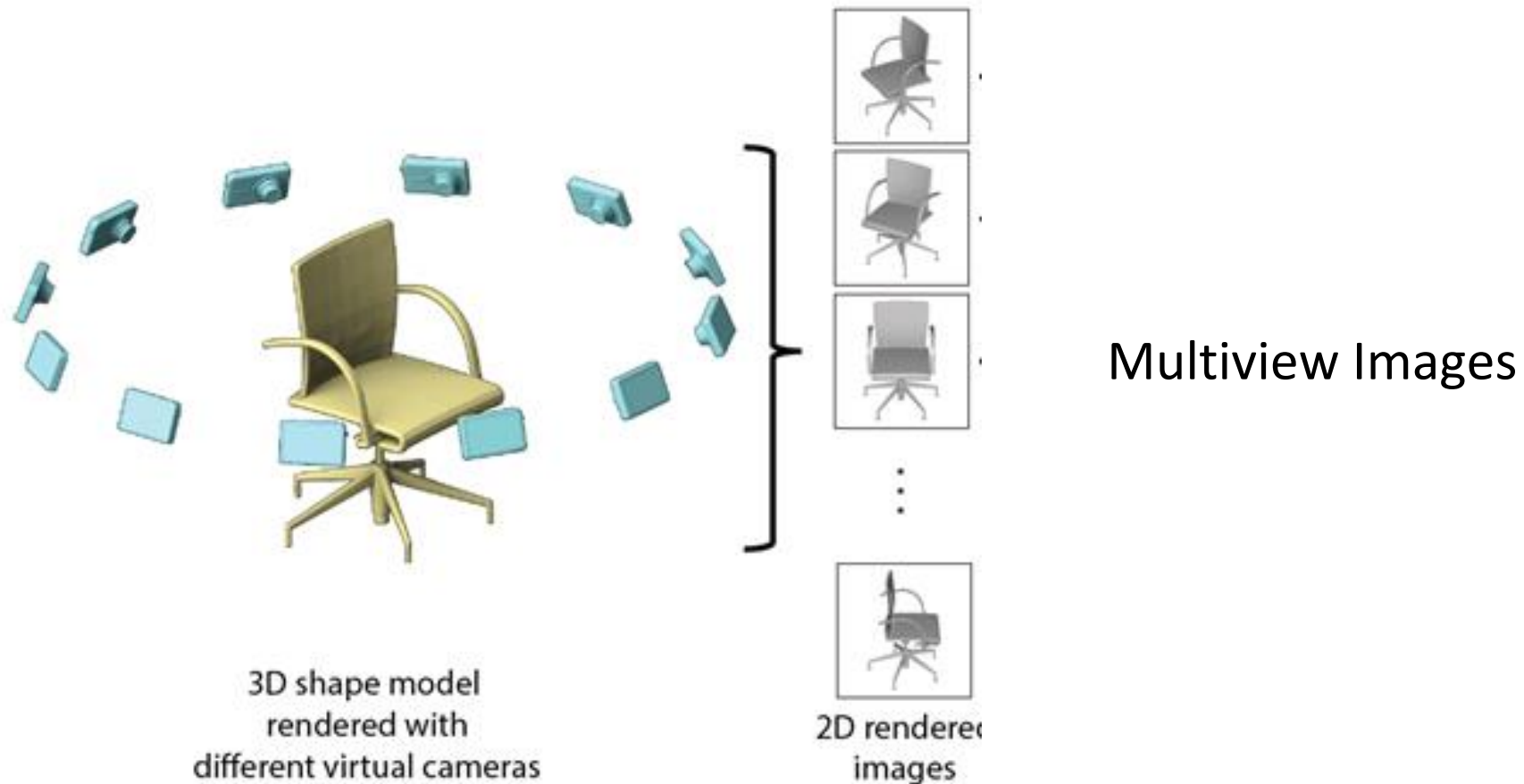
Point clouds were **converted to other regular representations** before input to a deep neural network

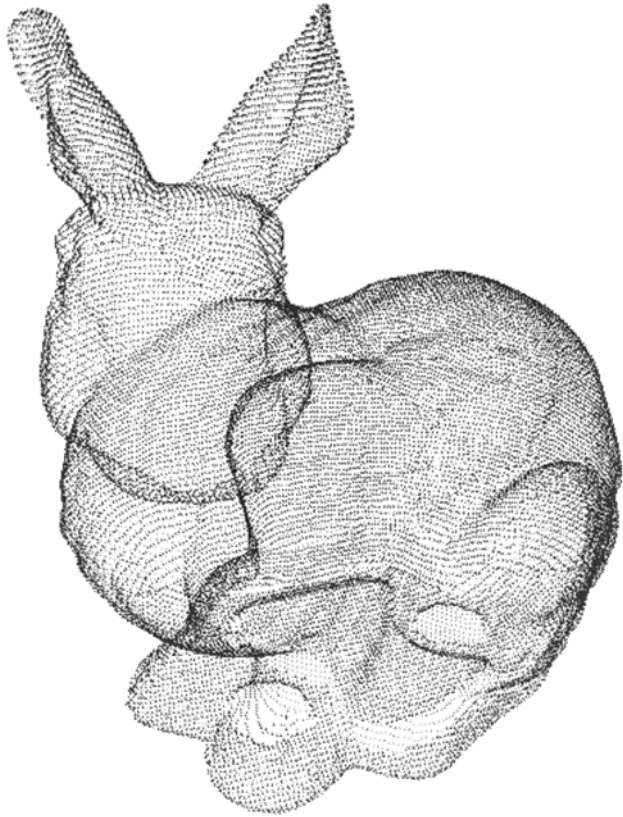


Con: High space & time complexity -- 3D convolution  $O(N^3)$   
Quantization errors in voxelization

# Earlier Work

Point clouds were **converted to other regular representations** before input to a deep neural network





## ***Research Question:***

Can we achieve effective  
**feature learning directly on  
irregular point clouds?**

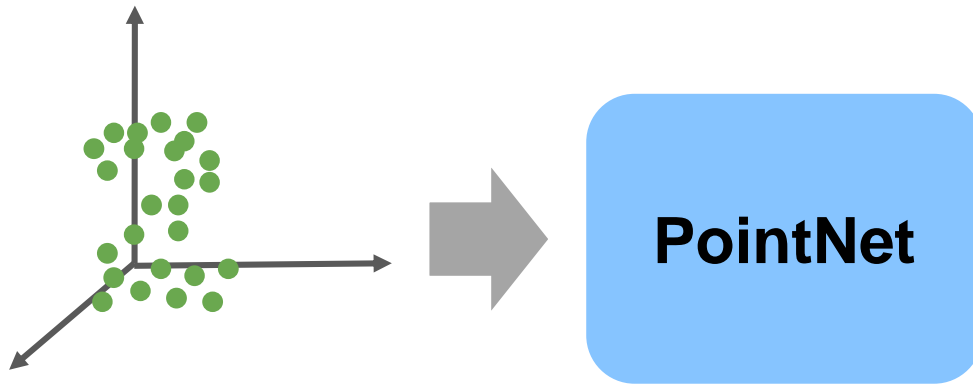


# Talk Outline

- Survey of **PointNet**, **PointNet++** architectures (~2017)
- Since the original PointNet work, an explosion of activity in this area -- very brief survey
- Applications to outdoor and indoor object detection and navigation, point cloud synthesis

# PointNet Architecture Review

## End-to-end learning for irregular point data

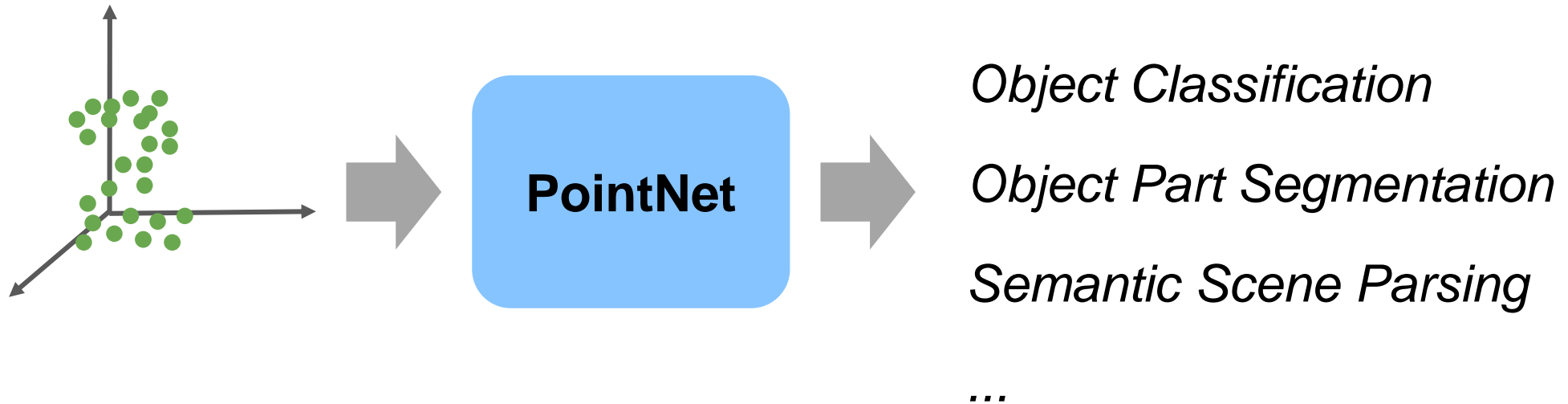


*Charles R. Qi, Hao Su, Kaichun Mo, Leonidas J. Guibas. PointNet: Deep Learning on Point Sets for 3D Classification and Segmentation. (CVPR'17)*

# PointNet Architecture Review

**End-to-end learning** for irregular point data

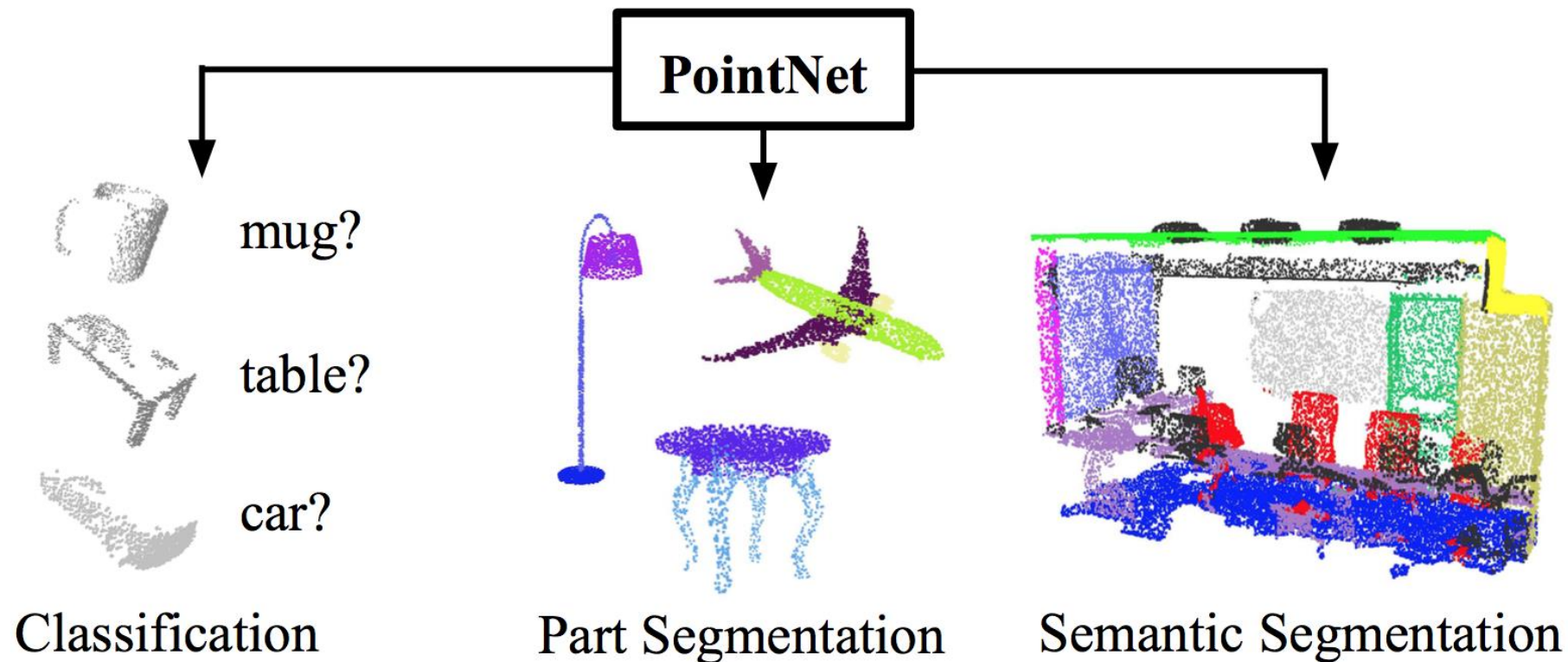
**Unified** framework for various tasks



# PointNet Architecture Review

**End-to-end learning** for irregular point data

**Unified** framework for various tasks



# Challenges

*The model has to respect key properties of point clouds:*

## **Point Permutation Invariance**

Point cloud is a set of **unordered** points

## **Spatial Transformation Invariance**

Point cloud **rigid motions** should not alter classification results

# Challenges

*The model has to respect key properties of point clouds:*

## **Point Permutation Invariance**

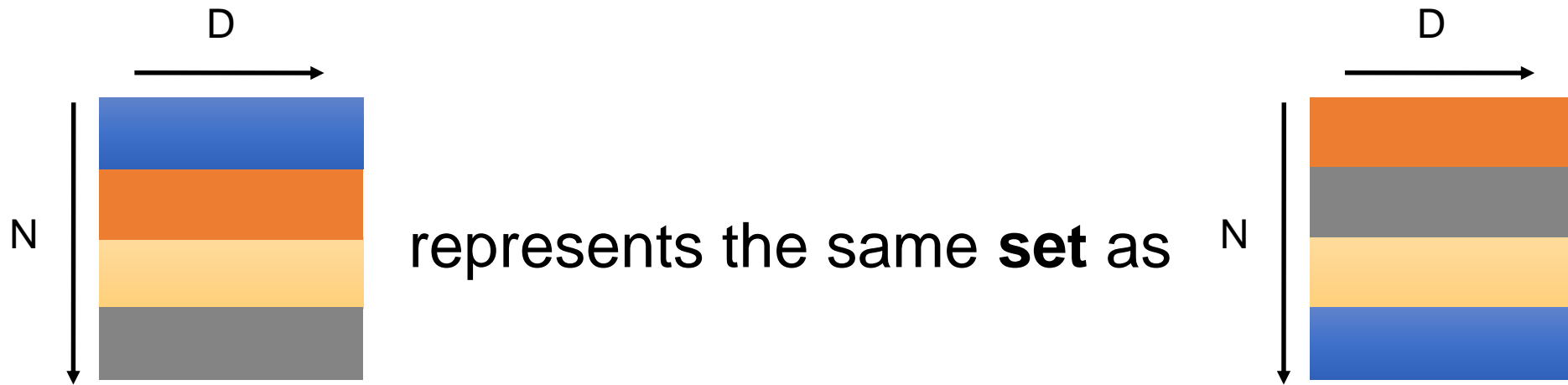
Point cloud is a set of unordered points

## **Spatial Transformation Invariance**

Point cloud rigid motions should not alter classification results

# Unordered Input

Point cloud: set of  $N$  **unordered** points, each represented by a  $D$  dim vector



**Model needs to be invariant to  $N!$  permutations**

# Permutation Invariance: Symmetric Function

$$f(x_1, x_2, \dots, x_n) \equiv f(x_{\pi_1}, x_{\pi_2}, \dots, x_{\pi_n}), \quad x_i \in \mathbb{R}^D$$

## Examples:

$$f(x_1, x_2, \dots, x_n) = \max\{x_1, x_2, \dots, x_n\}$$

$$f(x_1, x_2, \dots, x_n) = x_1 + x_2 + \dots + x_n$$

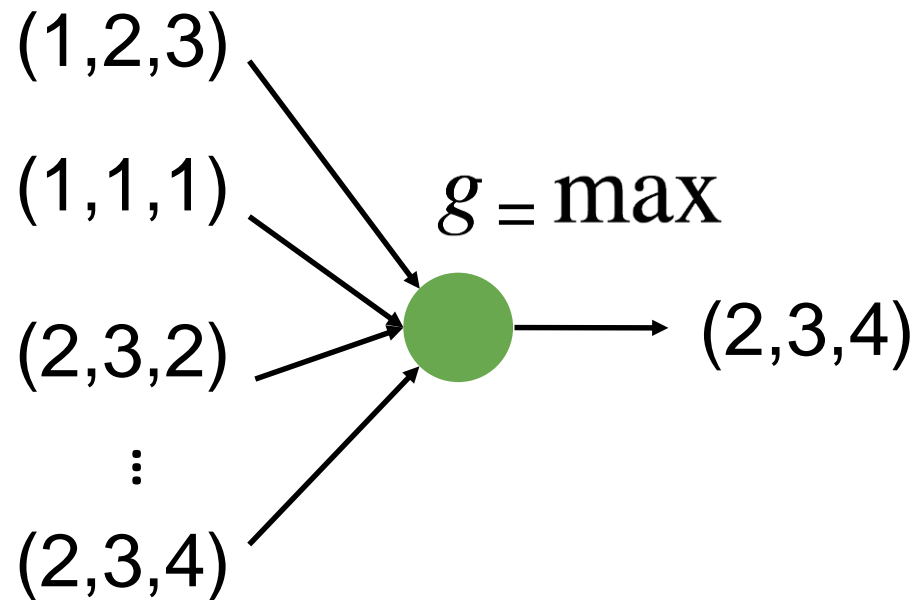
...

**How can we construct a universal family of symmetric functions by neural networks?**



# Construct Symmetric Functions by Neural Networks

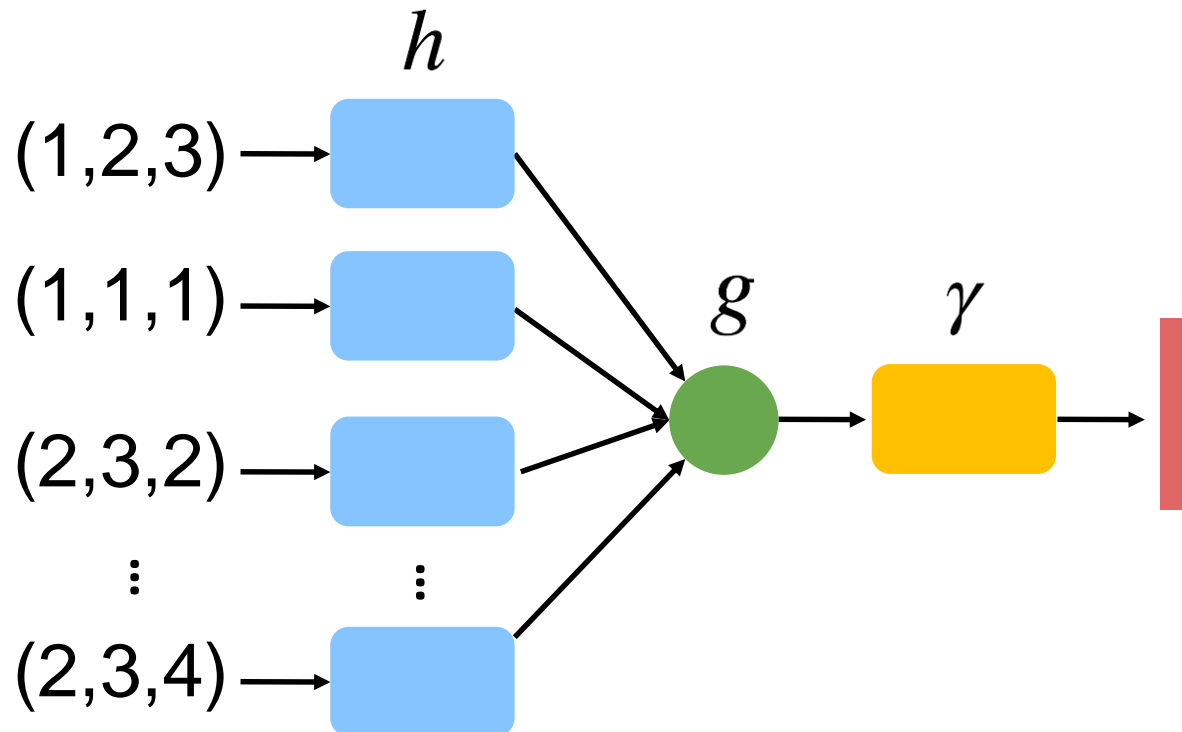
Simplest form: directly aggregate all points with a symmetric operator  $g$   
**Just discovers simple extreme/aggregate properties of the geometry.**



# Construct Symmetric Functions by Neural Networks

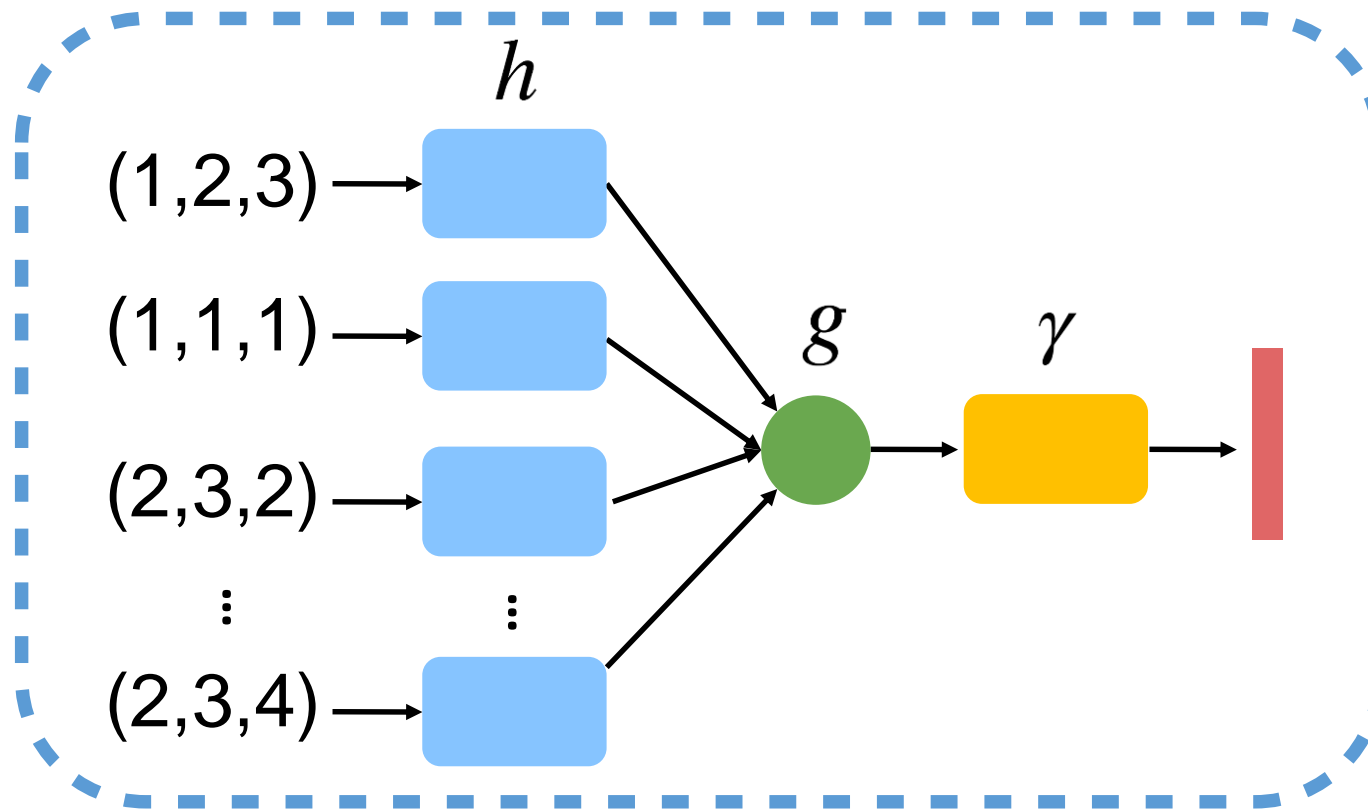
Embed points to a high-dim space before aggregation.

**Aggregation in the (redundant) high-dim space encodes more interesting properties of the geometry.**



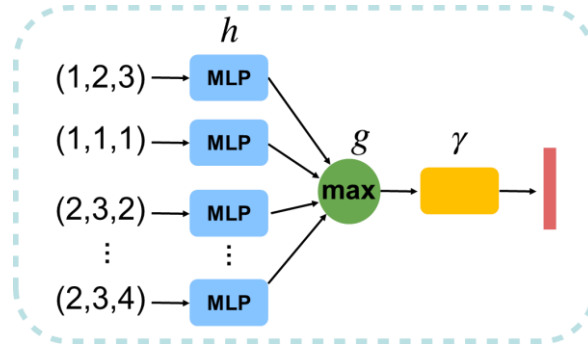
# Construct Symmetric Functions by Neural Networks

$f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$  is symmetric if  $g$  is symmetric



**PointNet (vanilla)**

# Symmetric Functions: Polynomials



$$2 \sum_{i \neq j} x_i x_j = \left( \sum_i x_i \right)^2 - \sum_i x_i^2 \qquad \sum_{i \neq j} (x_i - x_j)^2 = 3 \sum_i x_i^2 - \left( \sum_i x_i \right)^2$$

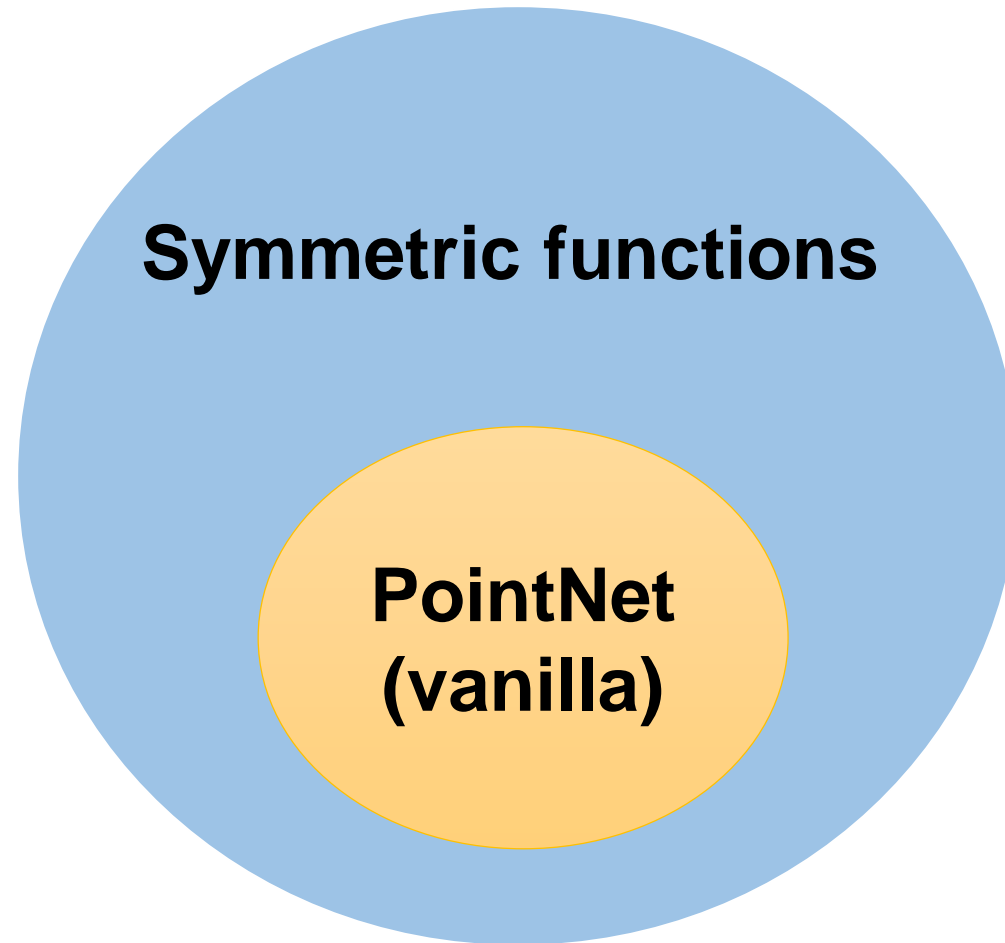
- In fact, **any** symmetric polynomial in the  $x_i$  can be expressed as a polynomial in sums of the form

$$\sum_i x_i^k$$

and can be computed by

$$f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$$

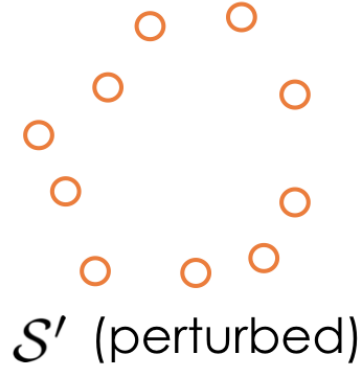
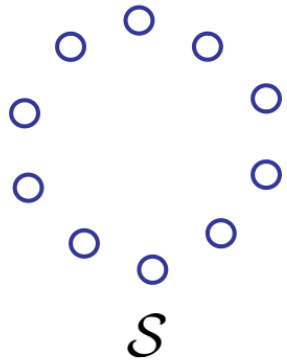
# What Symmetric Functions Can Be Constructed By PointNet?



# PointNet as a Universal Approximation to Set Functions

## Hausdorff continuous:

$f: 2^x \rightarrow \mathbb{R}$  is a continuous set function w.r.t Hausdorff distance



if  $d_{Hausdorff}(S, S') \approx 0$ , then  $f(S) \approx f(S')$

## Theorem

A Hausdorff continuous set function  $f: 2^x \rightarrow \mathbb{R}$  can be arbitrarily approximated by PointNet.

$$\left| f(S) - \gamma \left( \underset{x_i \in S}{\text{MAX}} \{h(x_i)\} \right) \right| < \epsilon$$

$$S \subseteq \mathbb{R}^d$$

**PointNet (vanilla)**

Voxel occupancy maps

# Challenges

*The model has to respect key properties of point clouds:*

## Point Permutation Invariance

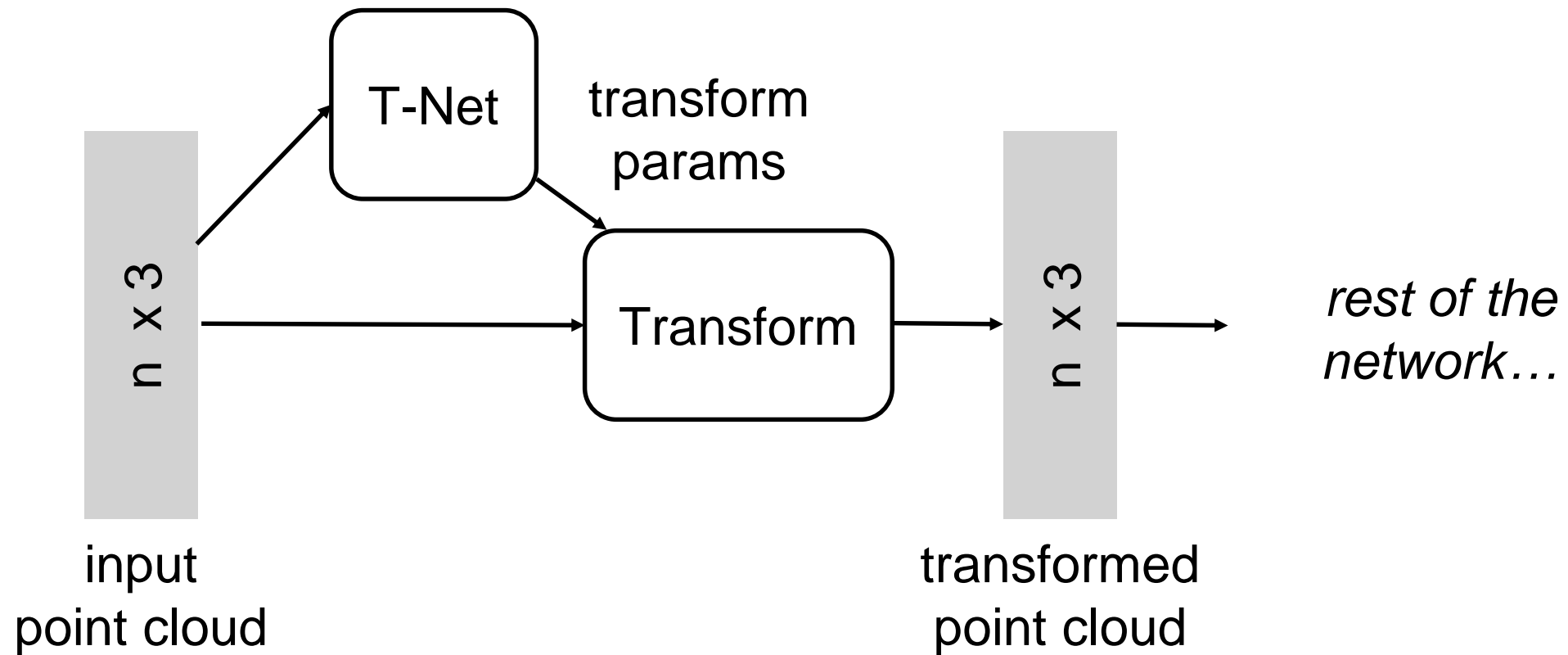
Point cloud is a set of unordered points

## Transformation Invariance

Point cloud rigid motions should not alter classification results

# Input Alignment by Transformer Network

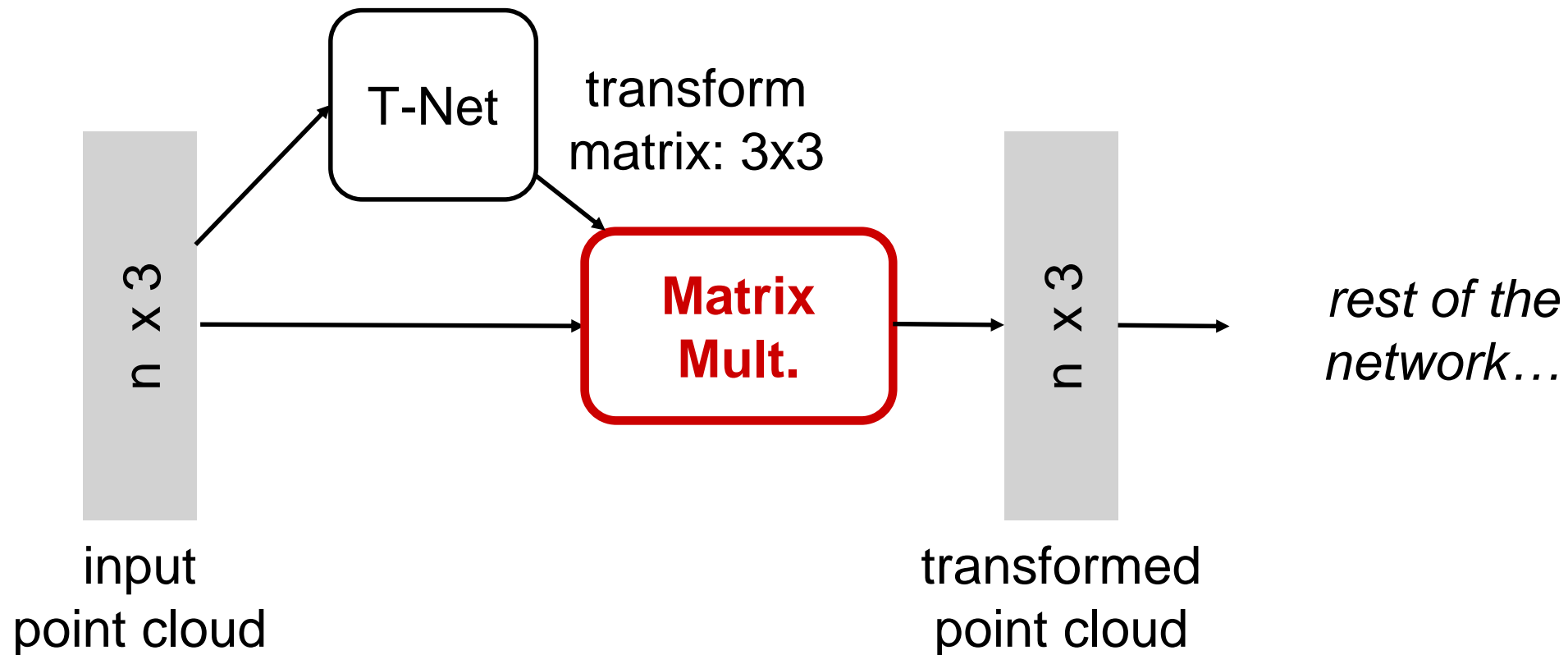
Idea: Data dependent transformation for automatic alignment





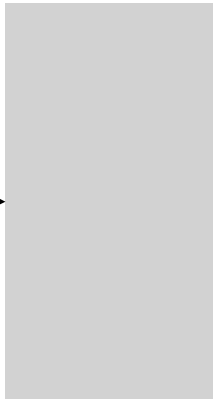
# Input Alignment by Transformer Network

Idea: Data dependent transformation for automatic alignment  
The transformation is just matrix multiplication!



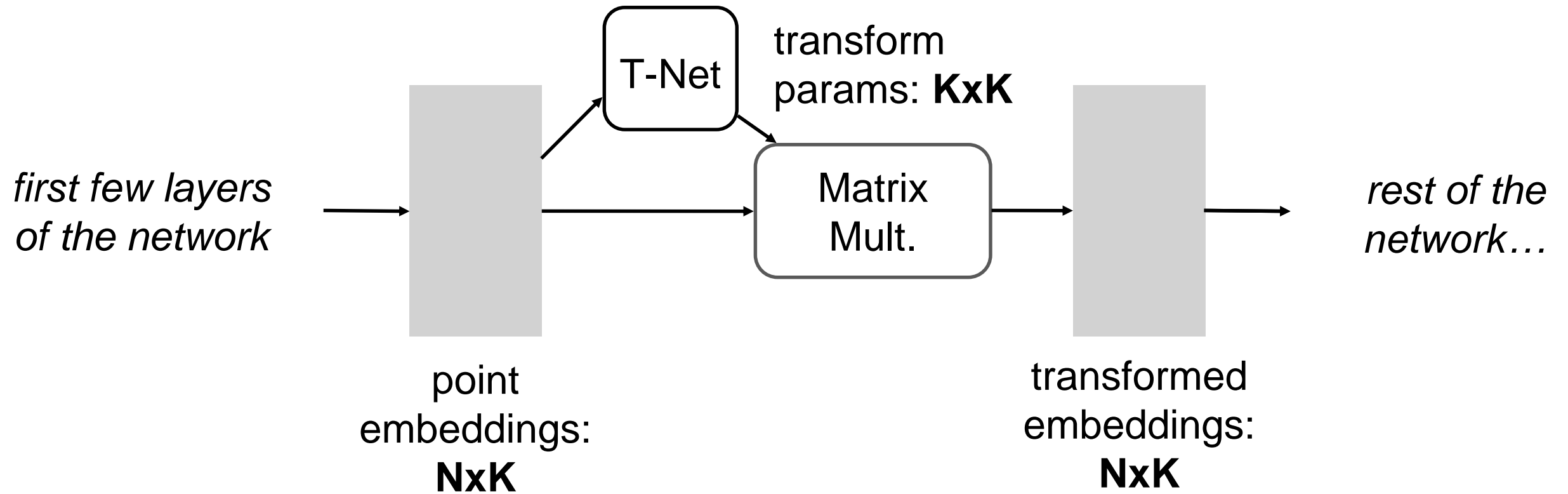
# Embedding Space Alignment

*first few layers  
of the network*

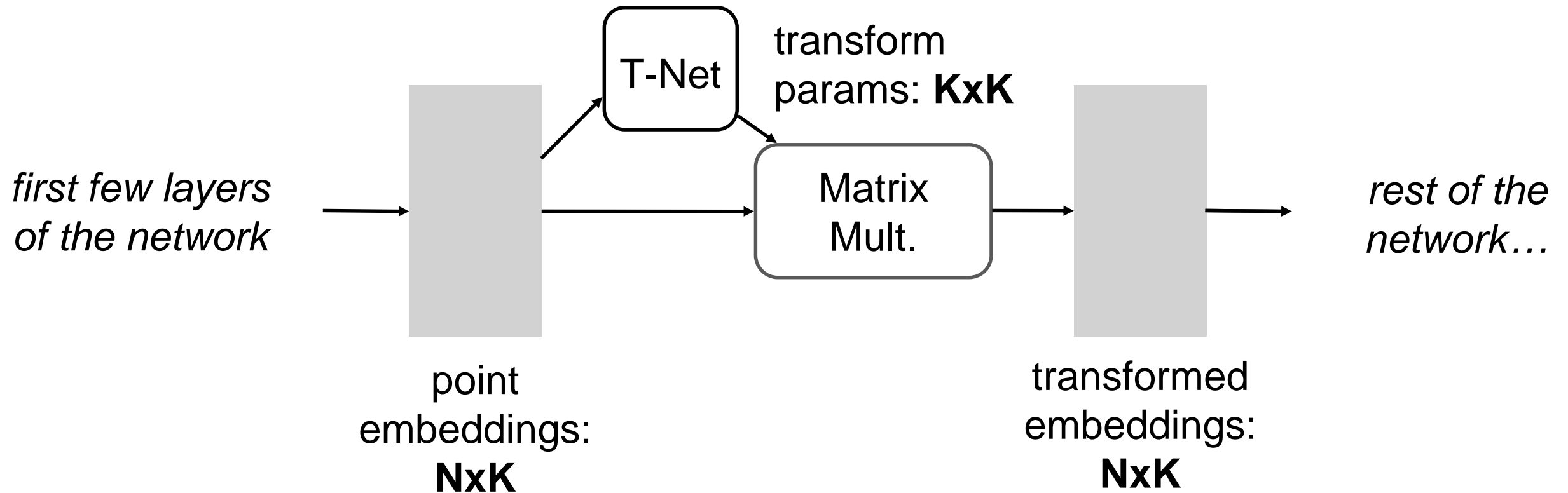


point  
embeddings:  
 **$N \times K$**

# Embedding Space Alignment



# Embedding Space Alignment



**Regularization loss:**

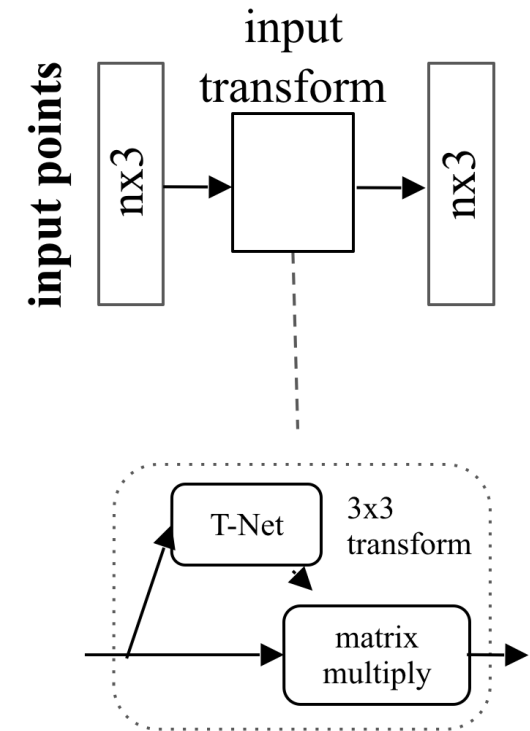
Transform matrix close to orthogonal:  $L_{reg} = \|I - AA^T\|_F^2$

# PointNet Classification Network

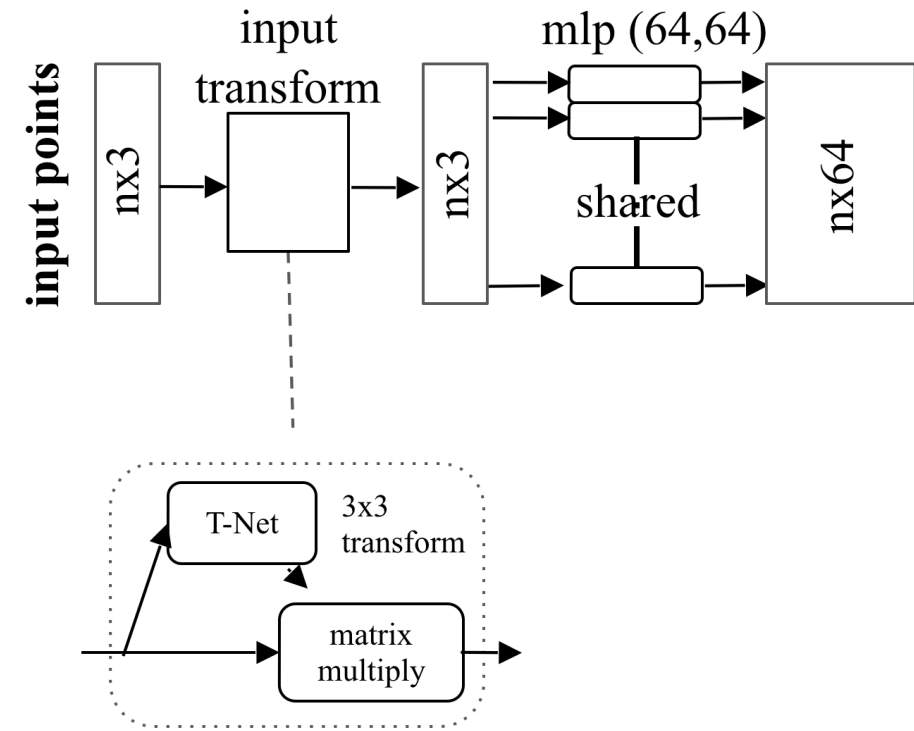
input points

$n \times 3$

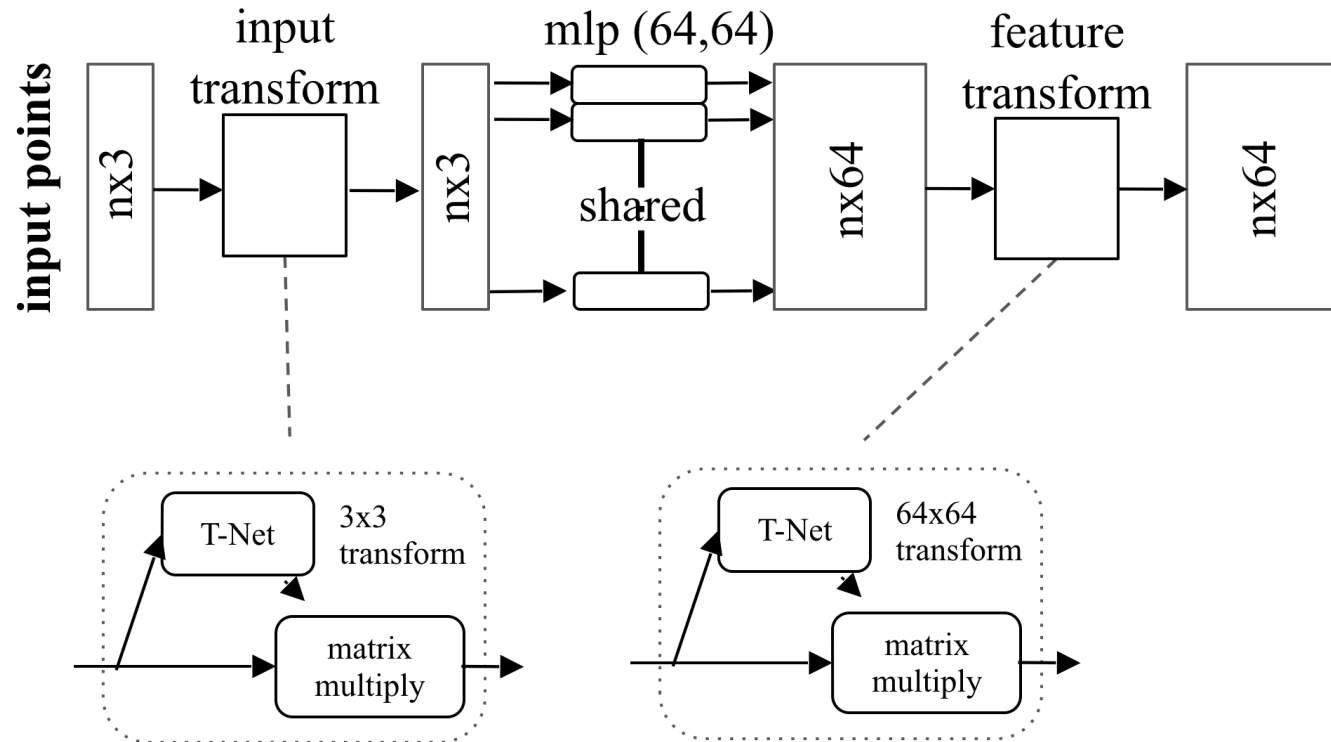
# PointNet Classification Network



# PointNet Classification Network

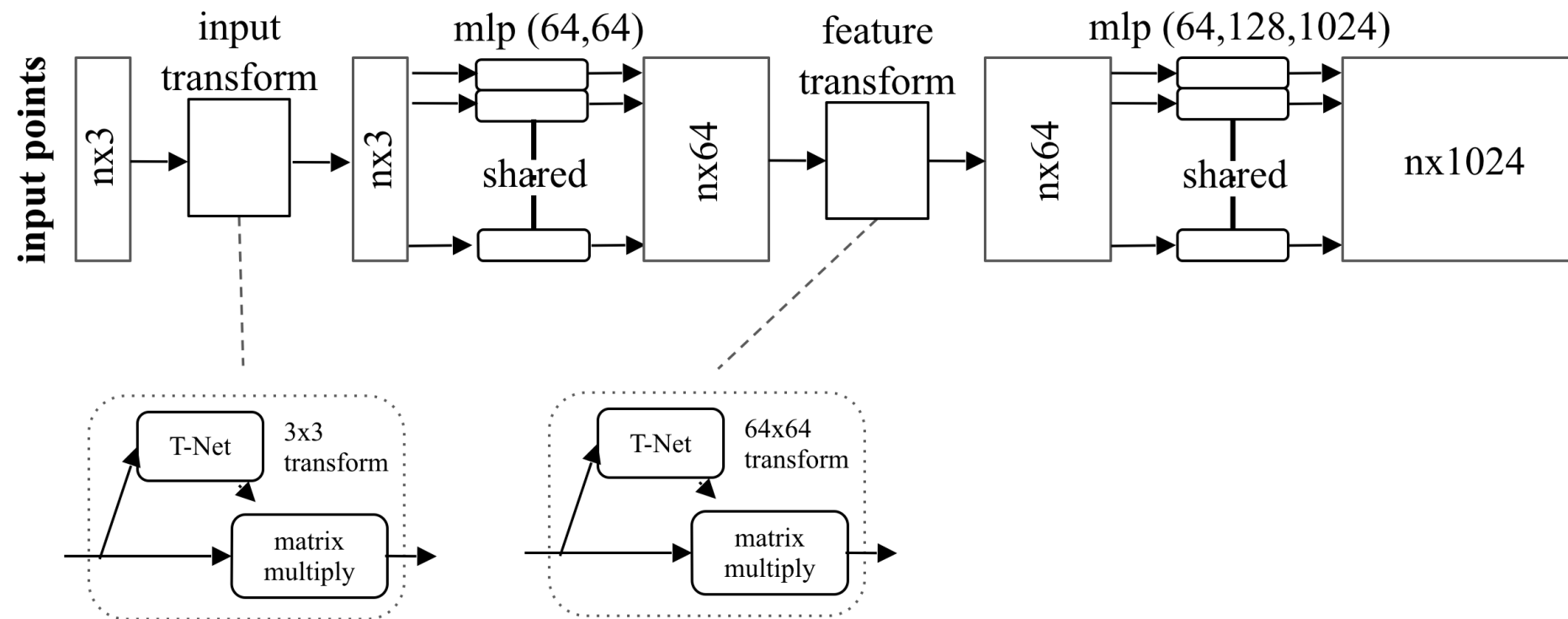


# PointNet Classification Network

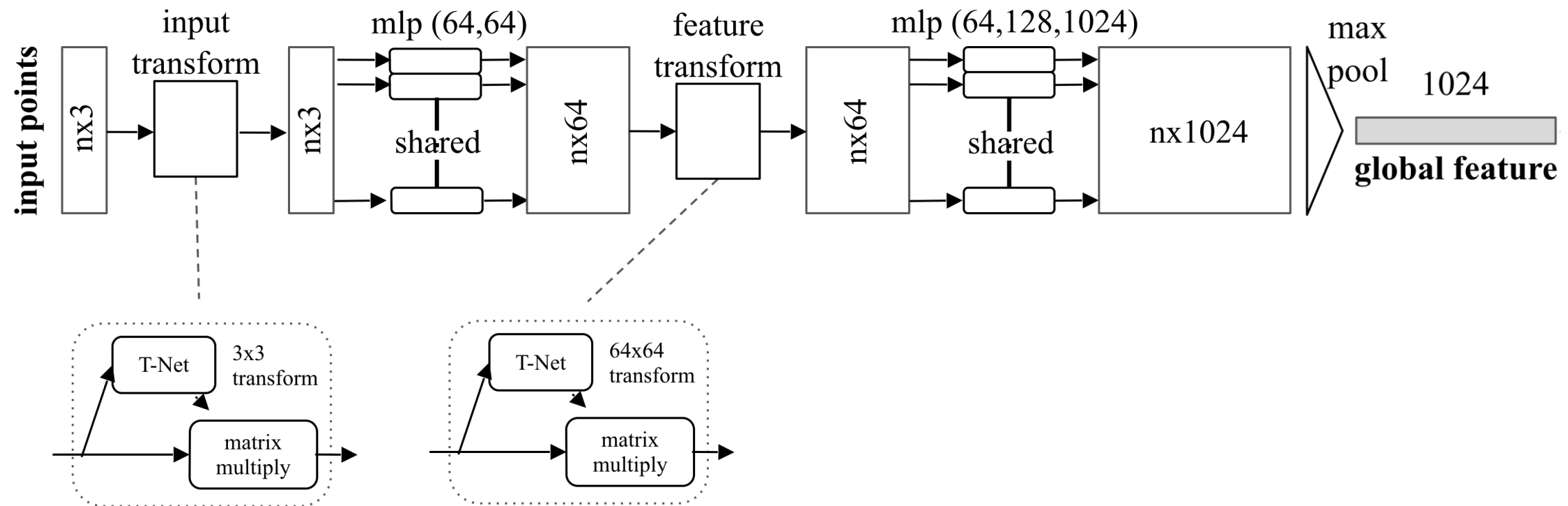




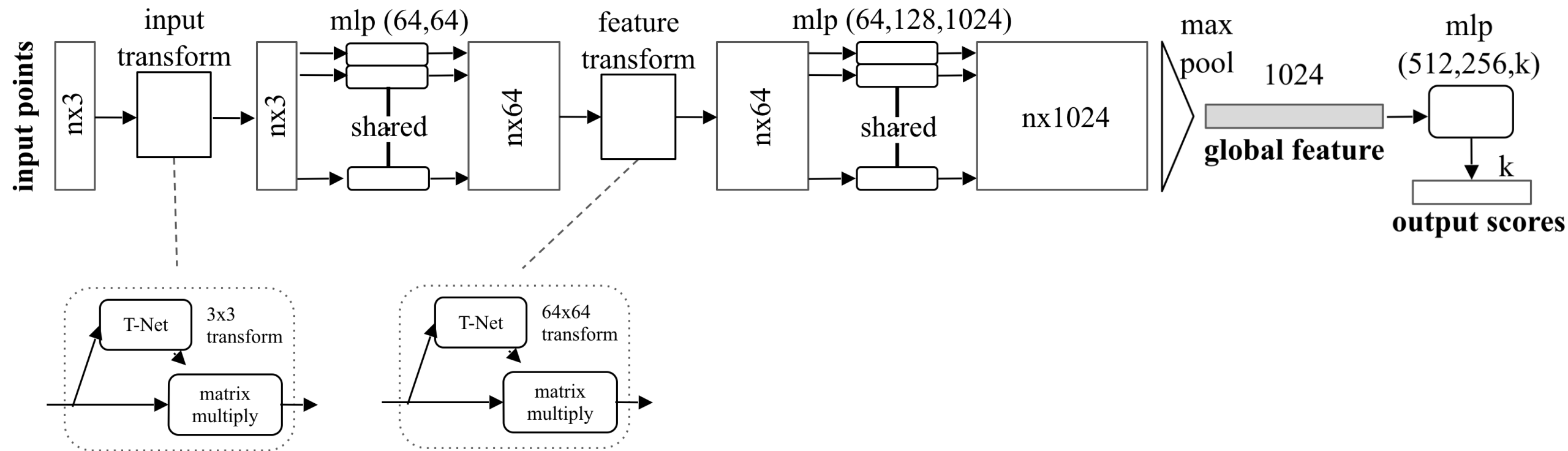
# PointNet Classification Network



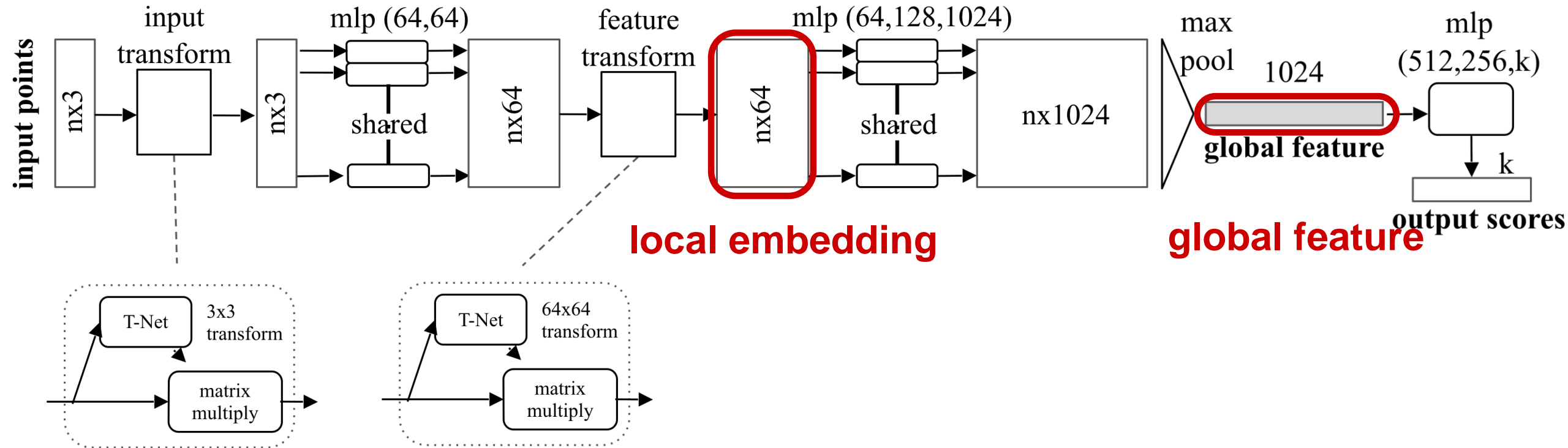
# PointNet Classification Network



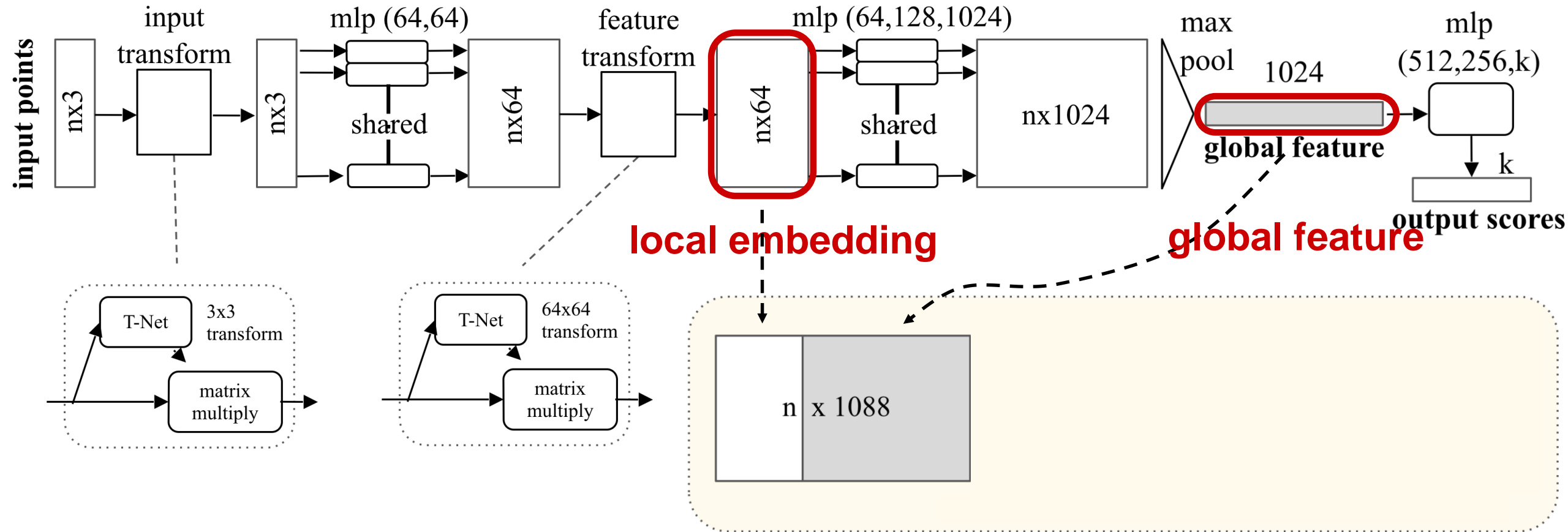
# PointNet Classification Network



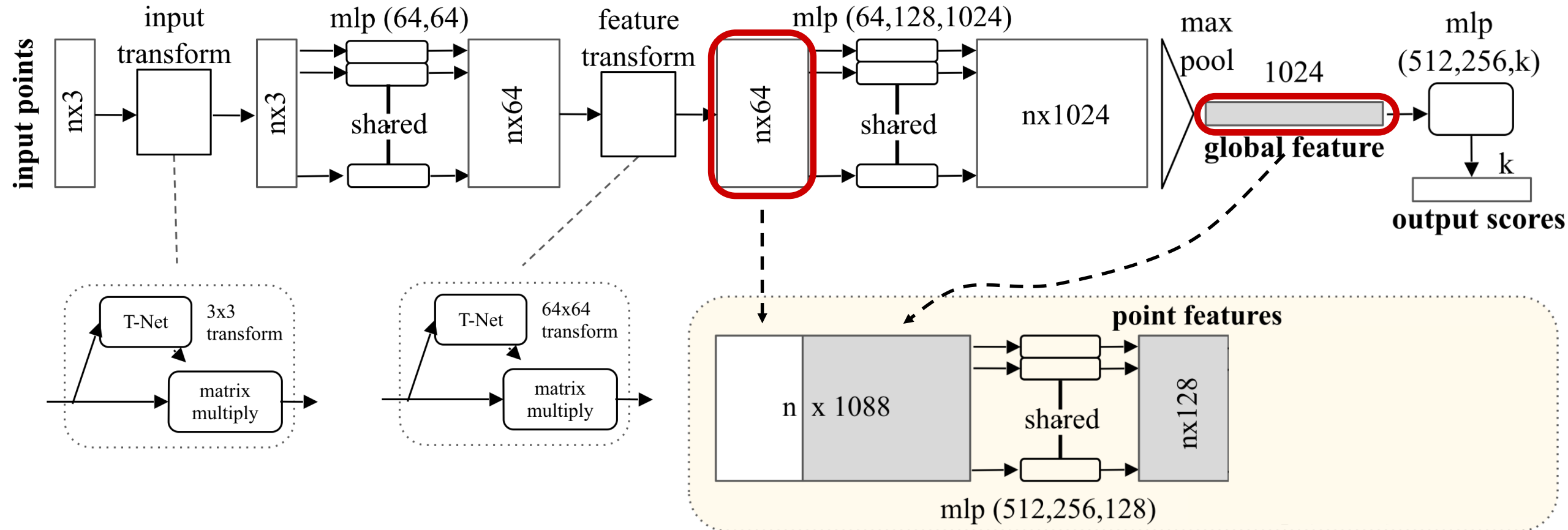
# Extension to PointNet Segmentation Network



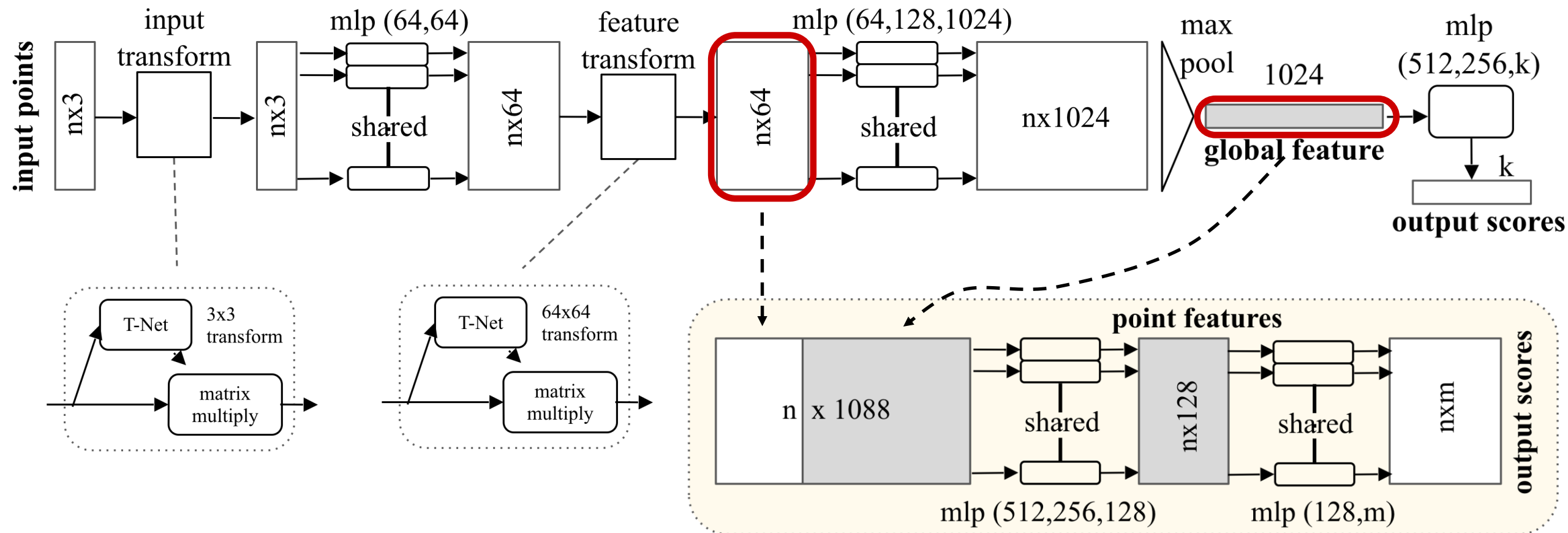
# Extension to PointNet Segmentation Network



# Extension to PointNet Segmentation Network



# Extension to PointNet Segmentation Network



# Results

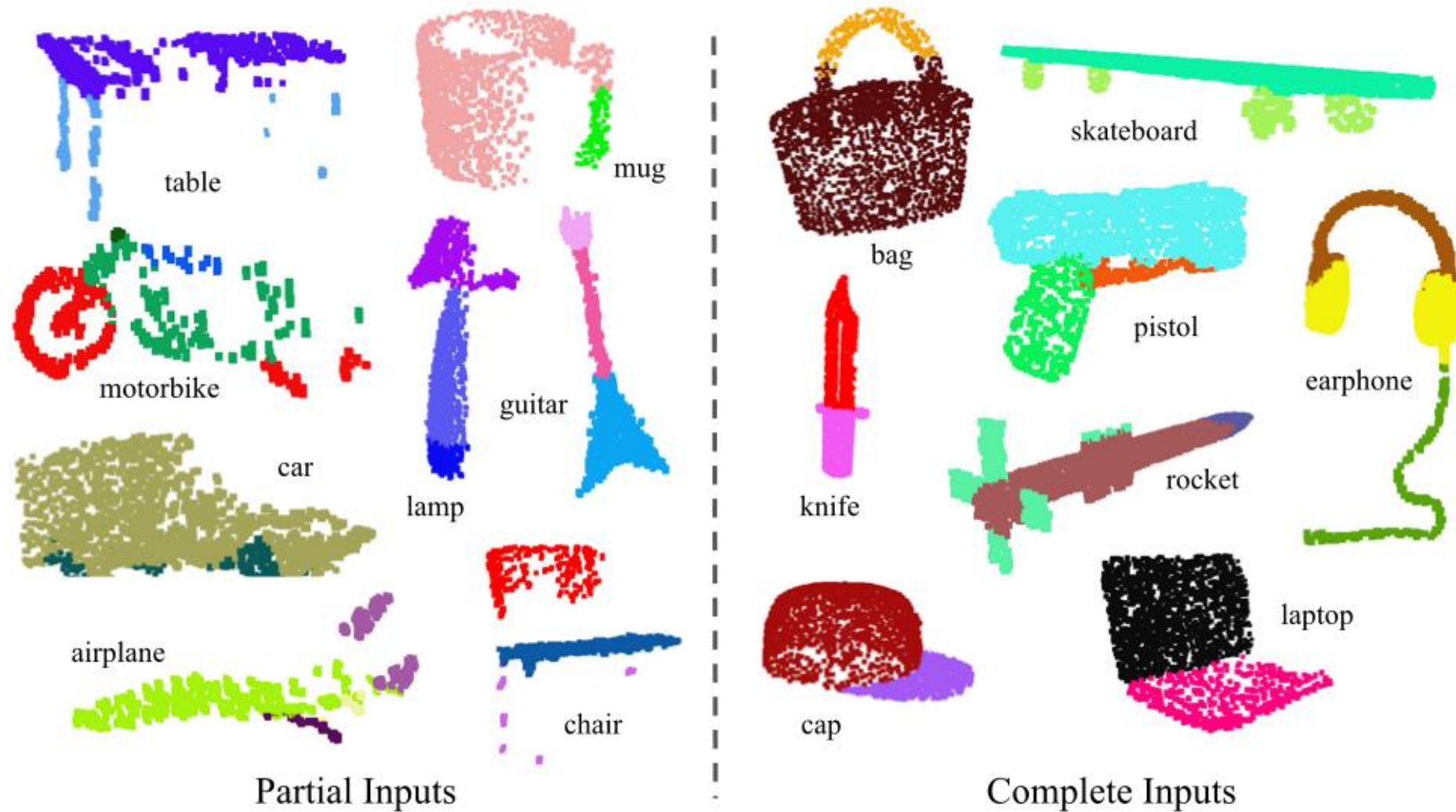


# Results on Object Classification

|                                 | input  | #views | accuracy<br>avg. class | accuracy<br>overall |
|---------------------------------|--------|--------|------------------------|---------------------|
| SPH [12]                        | mesh   | -      | 68.2                   |                     |
| <b>3D CNNs</b> 3DShapeNets [29] | volume | 1      | 77.3                   | 84.7                |
| VoxNet [18]                     | volume | 12     | 83.0                   | 85.9                |
| Subvolume [19]                  | volume | 20     | 86.0                   | <b>89.2</b>         |
| LFD [29]                        | image  | 10     | 75.5                   | -                   |
| MVCNN [24]                      | image  | 80     | <b>90.1</b>            | -                   |
| Ours baseline                   | point  | -      | 72.6                   | 77.4                |
| Ours PointNet                   | point  | 1      | 86.2                   | <b>89.2</b>         |

*dataset: ModelNet40; metric: 40-class classification accuracy (%)*

# Results on Object Part Segmentation



# Results on Object Part Segmentation

|          | mean        | aero        | bag         | cap         | car         | chair       | ear<br>phone | guitar      | knife       | lamp        | laptop      | motor       | mug         | pistol      | rocket      | skate<br>board | table       |
|----------|-------------|-------------|-------------|-------------|-------------|-------------|--------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|----------------|-------------|
| # shapes |             | 2690        | 76          | 55          | 898         | 3758        | 69           | 787         | 392         | 1547        | 451         | 202         | 184         | 283         | 66          | 152            | 5271        |
| Wu [28]  | -           | 63.2        | -           | -           | -           | 73.5        | -            | -           | -           | 74.4        | -           | -           | -           | -           | -           | -              | 74.8        |
| Yi [30]  | 81.4        | 81.0        | 78.4        | 77.7        | <b>75.7</b> | 87.6        | 61.9         | <b>92.0</b> | 85.4        | <b>82.5</b> | <b>95.7</b> | <b>70.6</b> | 91.9        | <b>85.9</b> | 53.1        | 69.8           | 75.3        |
| 3DCNN    | 79.4        | 75.1        | 72.8        | 73.3        | 70.0        | 87.2        | 63.5         | 88.4        | 79.6        | 74.4        | 93.9        | 58.7        | 91.8        | 76.4        | 51.2        | 65.3           | 77.1        |
| Ours     | <b>83.7</b> | <b>83.4</b> | <b>78.7</b> | <b>82.5</b> | 74.9        | <b>89.6</b> | <b>73.0</b>  | 91.5        | <b>85.9</b> | 80.8        | 95.3        | 65.2        | <b>93.0</b> | 81.2        | <b>57.9</b> | <b>72.8</b>    | <b>80.6</b> |

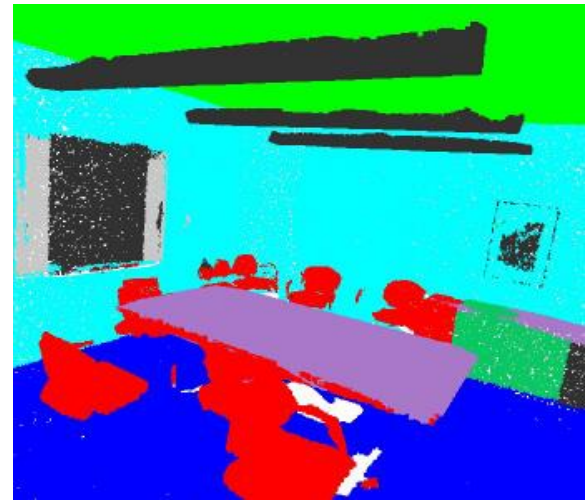
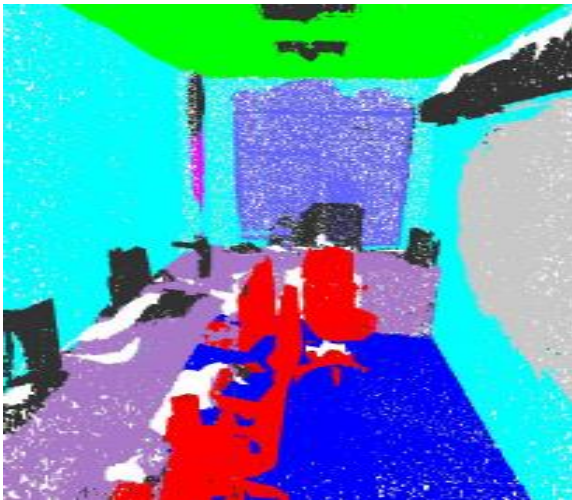
*dataset: ShapeNetPart; metric: mean IoU (%)*

# Results on Semantic Scene Parsing

Input

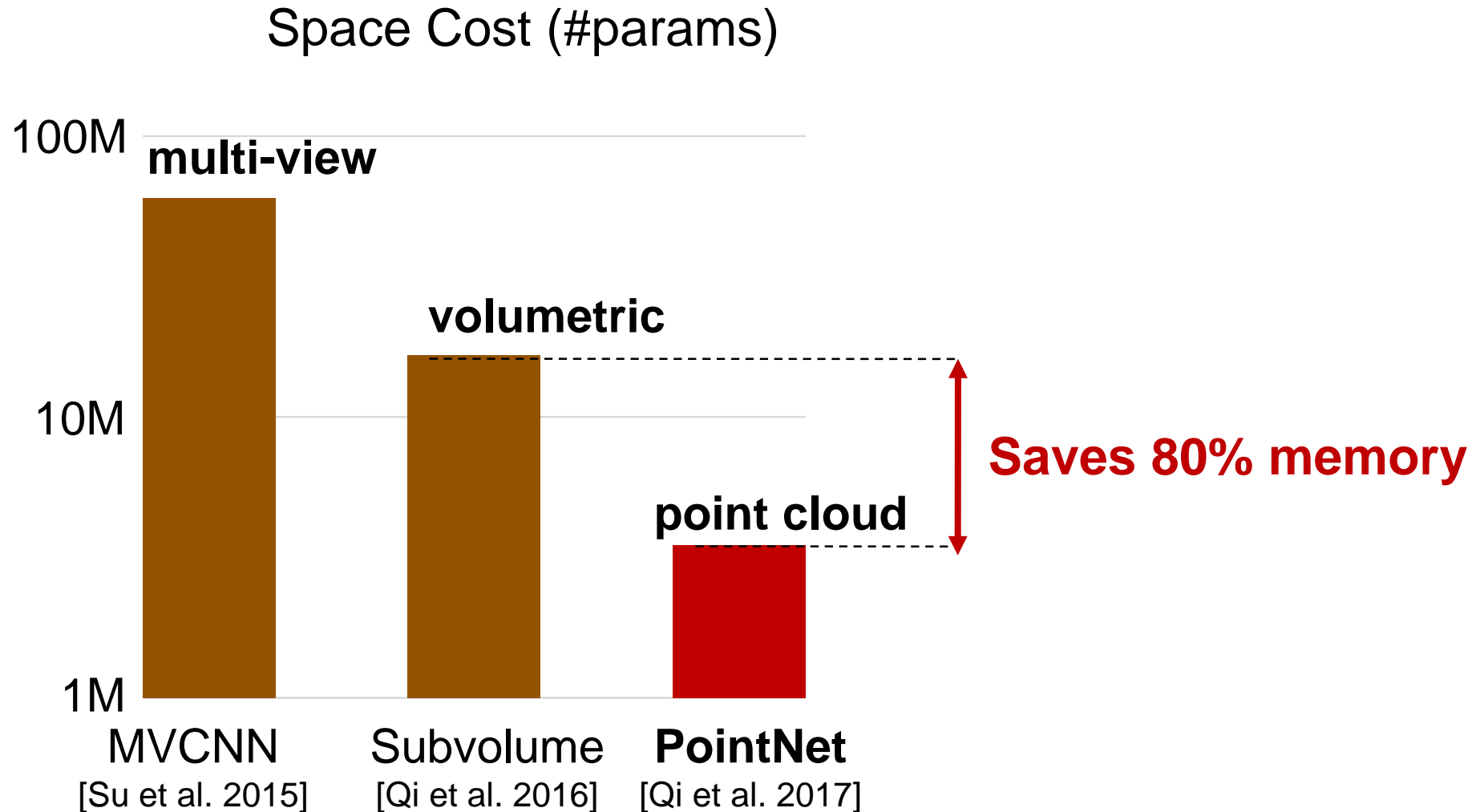


Output

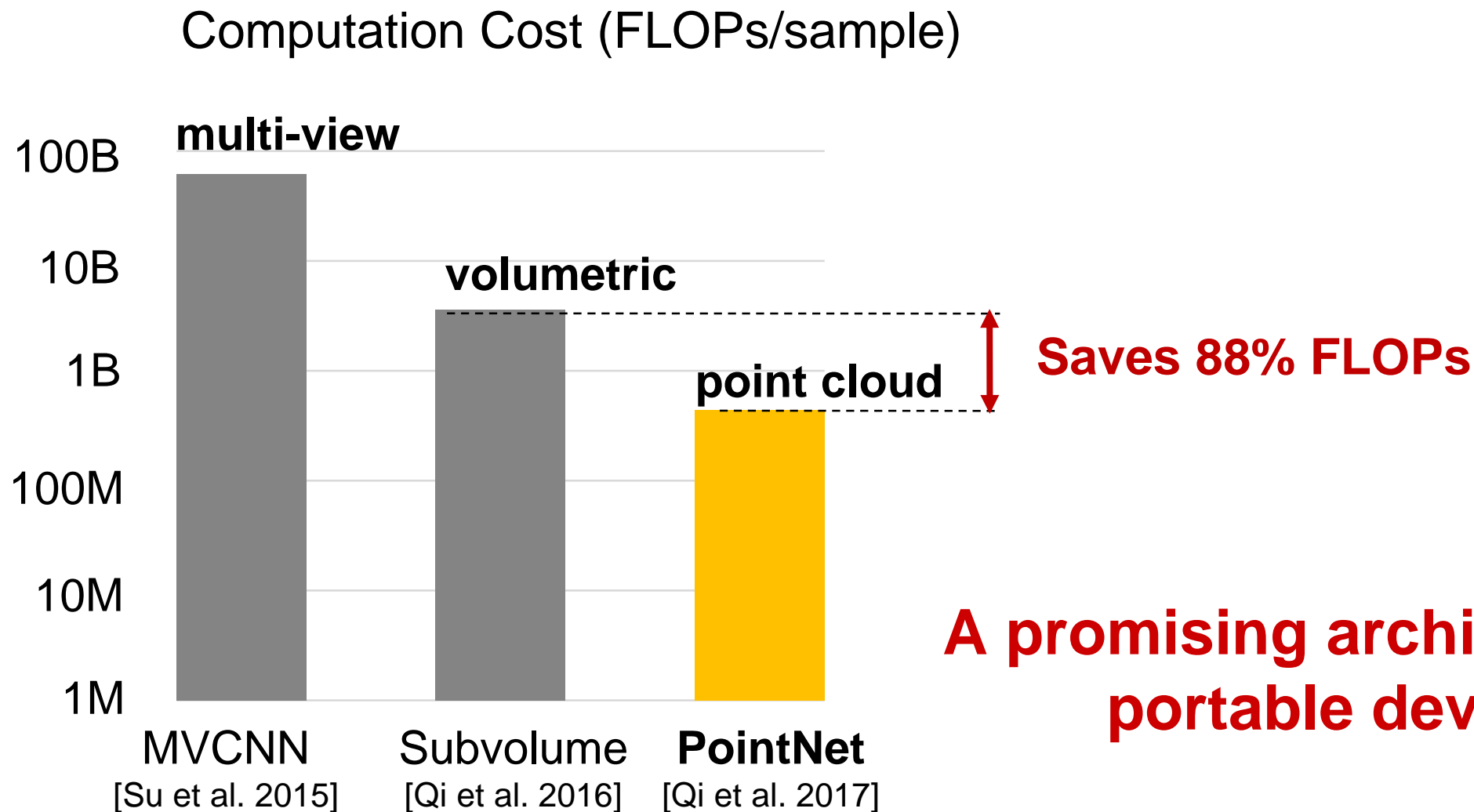


*dataset: Stanford 2D-3D-S (Matterport scans)*

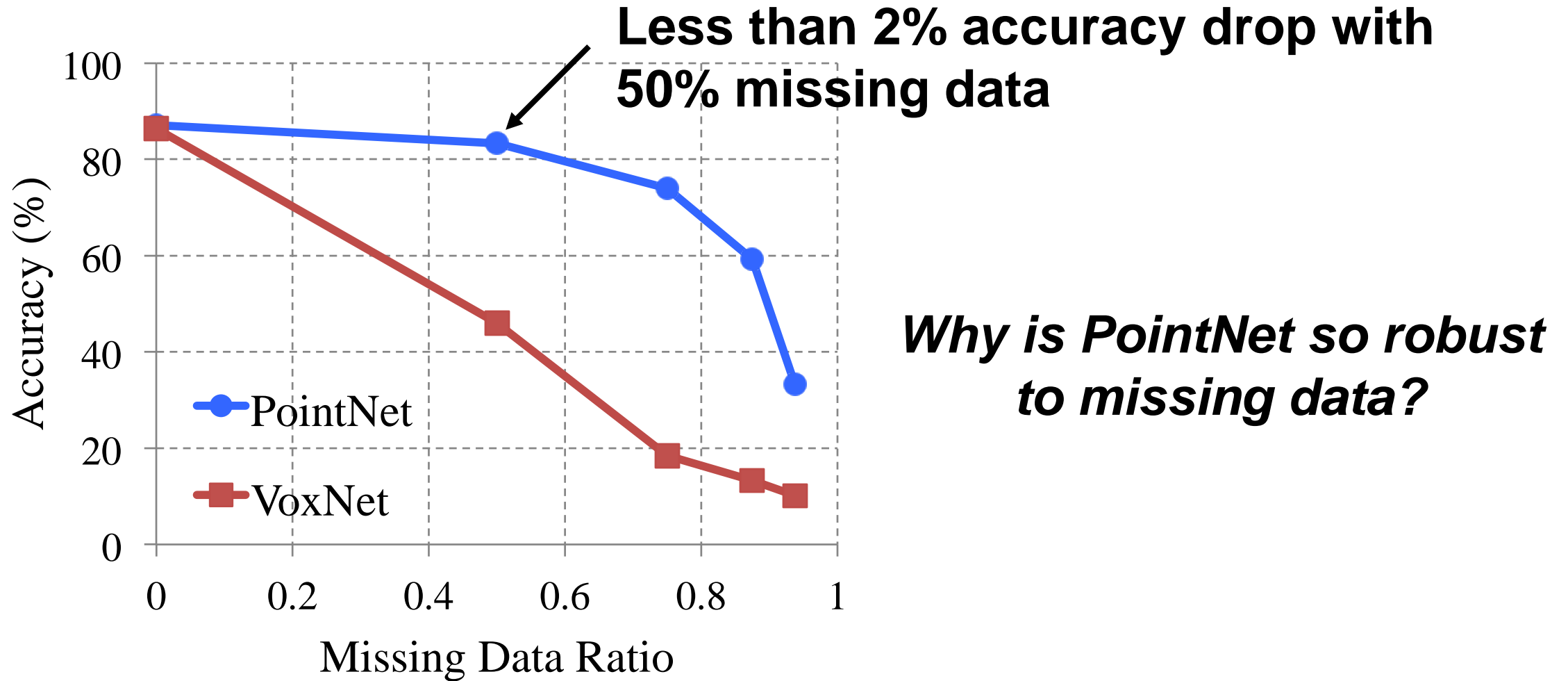
# PointNet is Light-Weight and Fast



# PointNet is Light-Weight and Fast



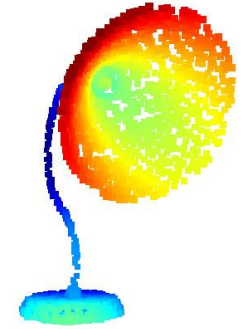
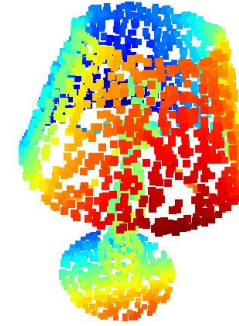
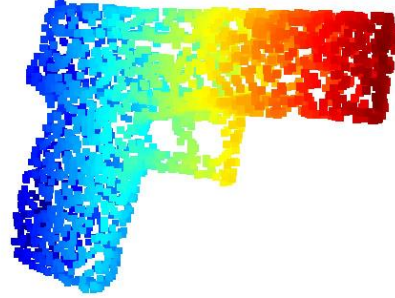
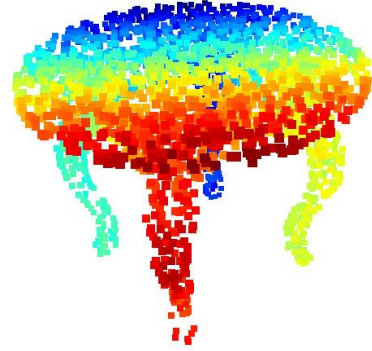
# PointNet is Robust to Data Corruption



*dataset: ModelNet40; metric: 40-class classification accuracy (%)*

# Visualizing Global Point Cloud Features

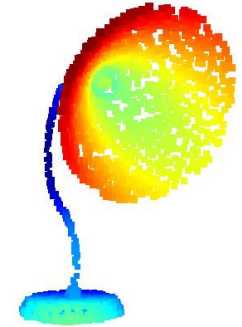
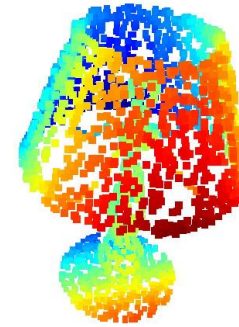
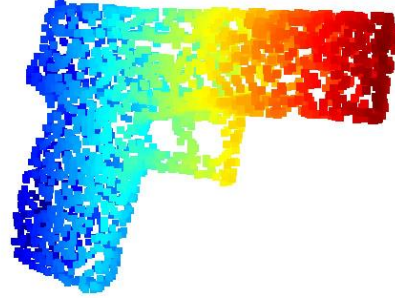
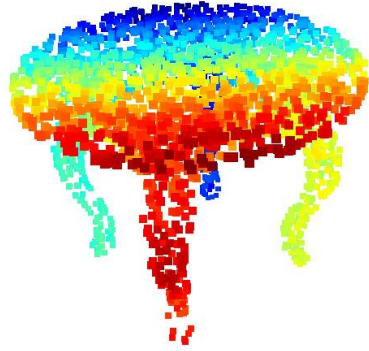
Original Shape



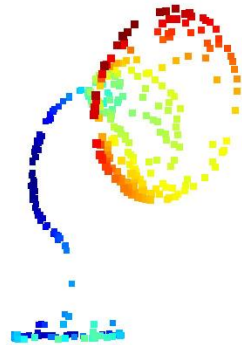
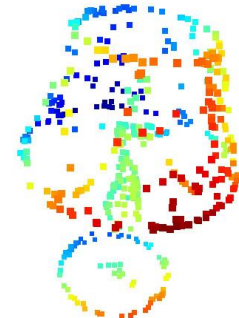
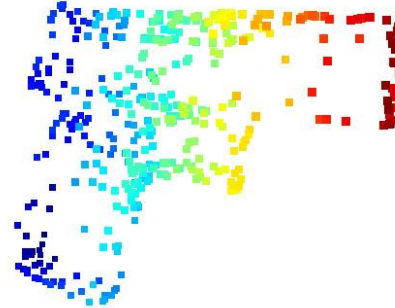
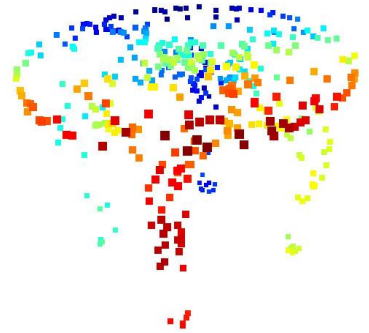


# Visualizing Global Point Cloud Features

Original Shape

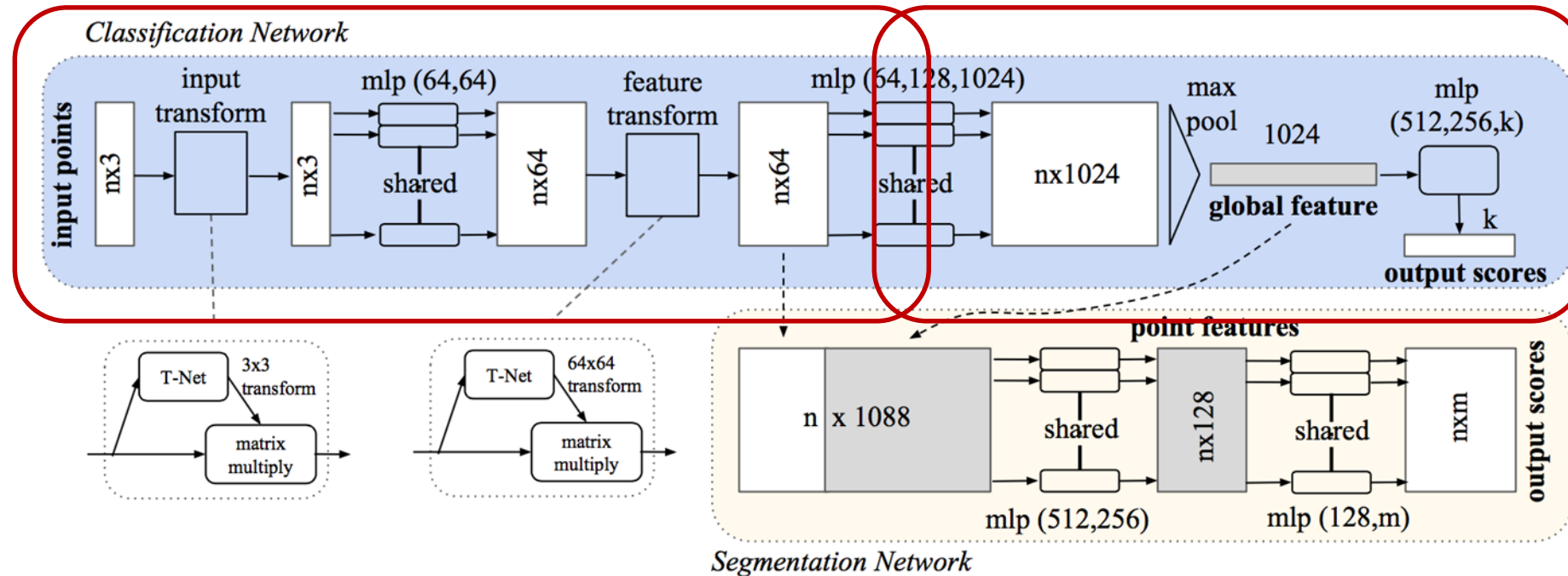


Critical Points



*PointNet learns to pick perceptually interesting points!*

# Learning Interesting Points

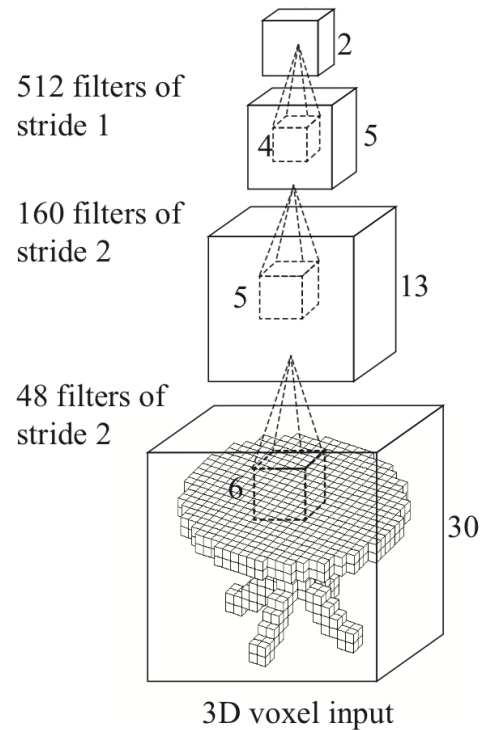


- Pointnet learns optimization criteria, which in turn pick interesting points

# From PointNet to PointNet++

# Limitations of PointNet

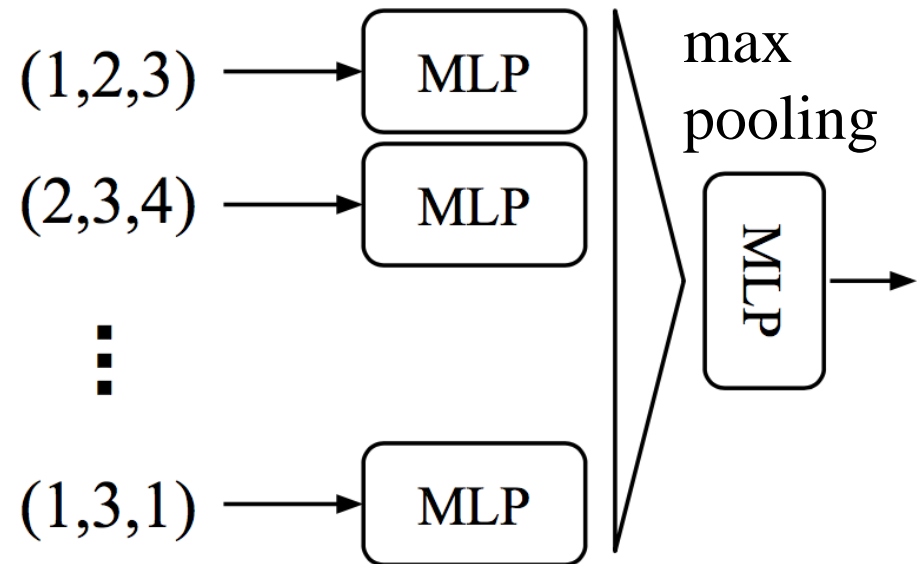
**Hierarchical feature learning**  
multiple levels of abstraction



3D CNN [Wu et al.2015]

**V.S.**

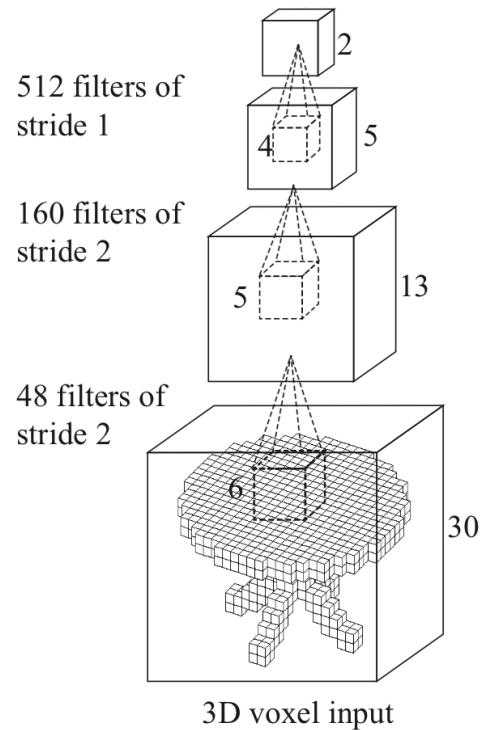
**Global feature learning**  
either **one** point or **all** points



PointNet (vanilla) [Qi et al.2017]

# Limitations of PointNet

**Hierarchical feature learning**  
multiple levels of abstraction



3D CNN [Wu et al.2015]

**V.S.**

**Global feature learning**  
either **one** point or **all** points

**No local context**

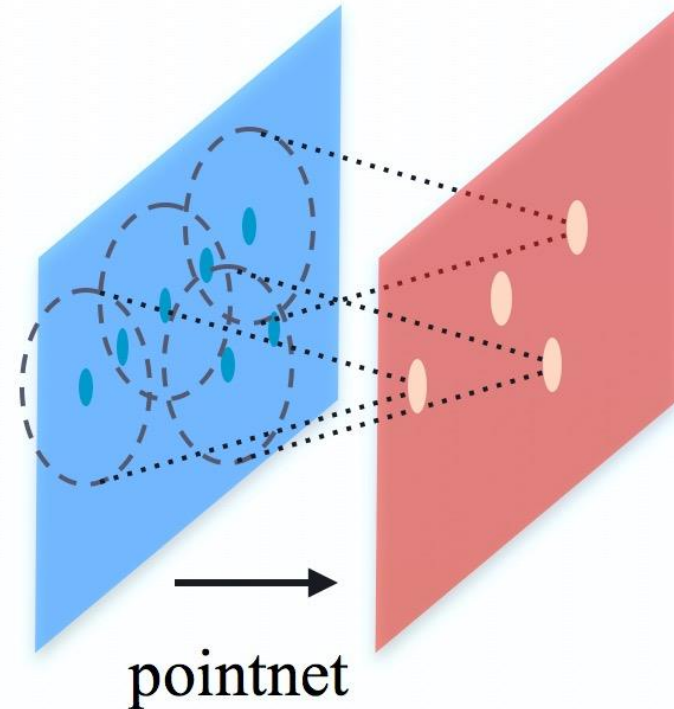
**Limited local invariance**

PointNet (vanilla) [Qi et al.2017]

# PointNet++

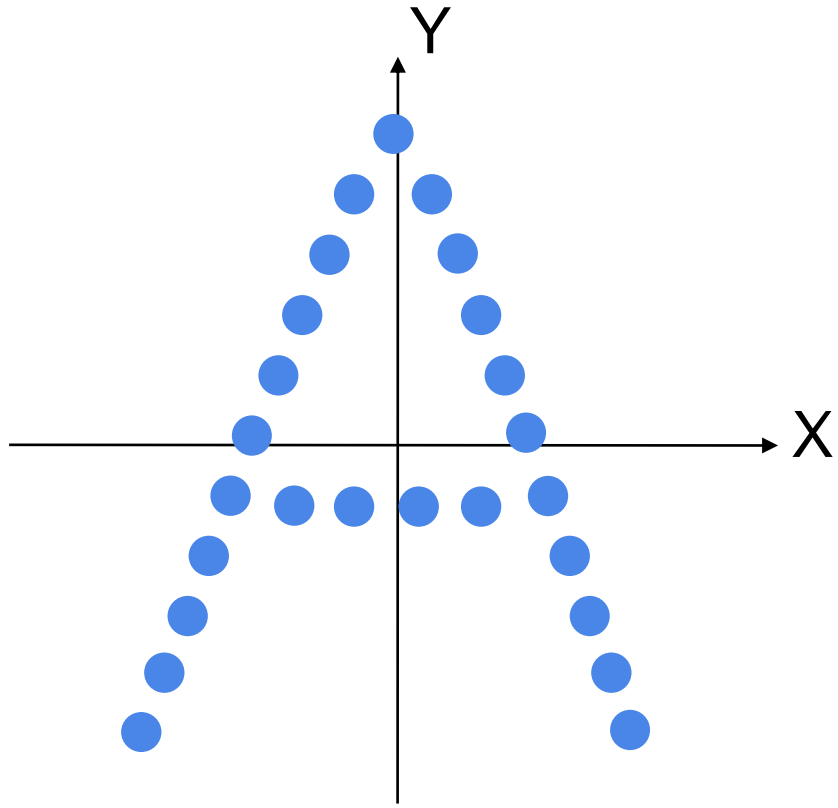
Basic idea: Recursively apply pointnet at local regions.

- ✓ Hierarchical feature learning
- ✓ Local translation invariance
- ✓ Permutation invariance



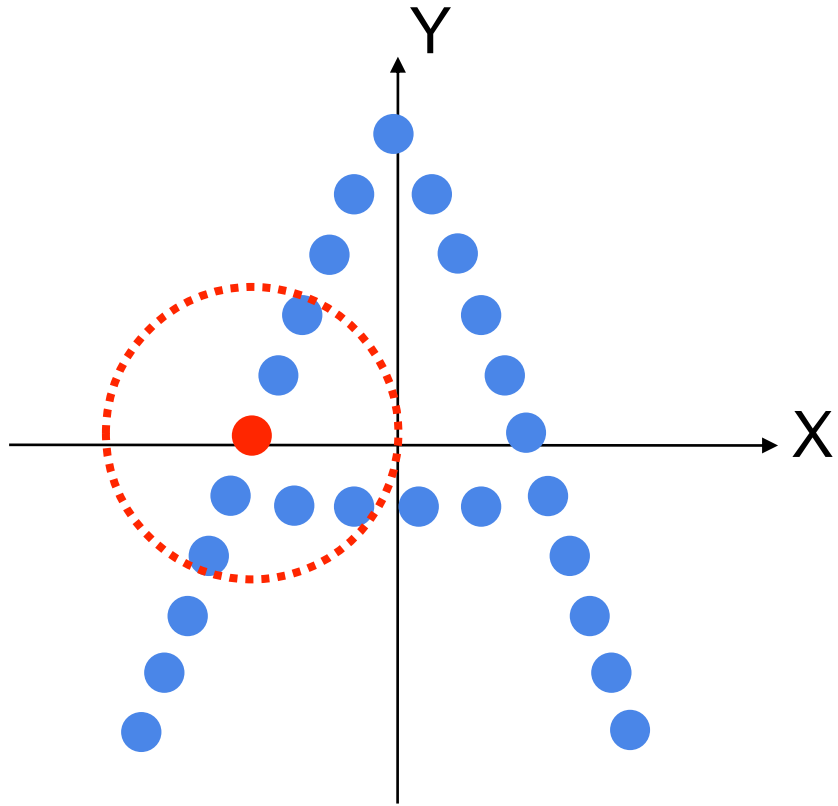
[2] Charles R. Qi, Li Yi, Hao Su, Leonidas Guibas. *PointNet++: Deep Hierarchical Feature Learning on Point Sets in a Metric Space (NIPS'17)*

# Hierarchical Point Feature Learning



$N$  points in  $(X, Y)$

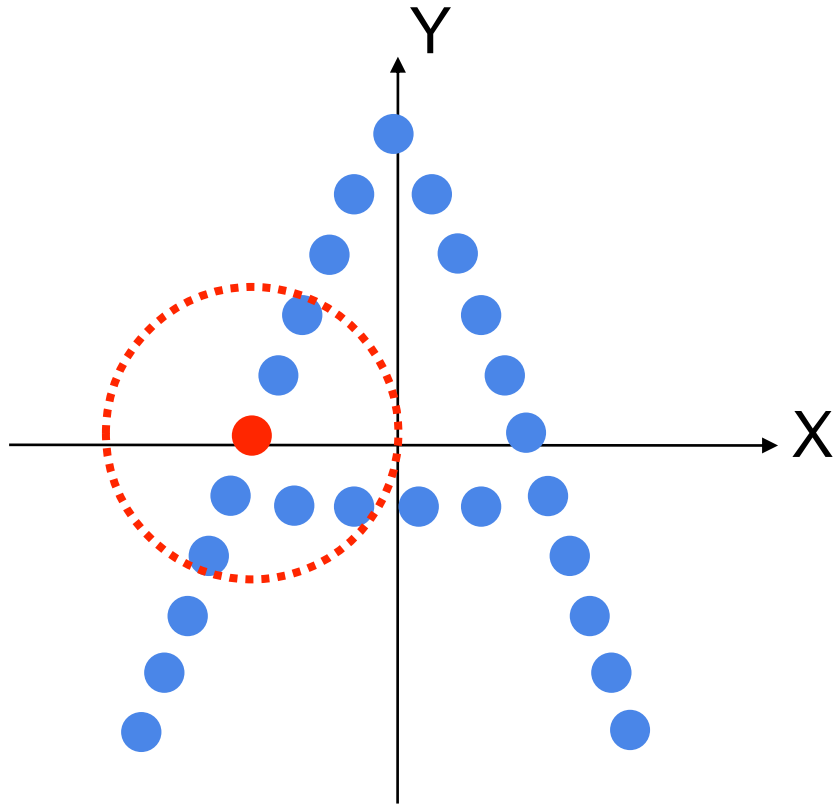
# Hierarchical Point Feature Learning



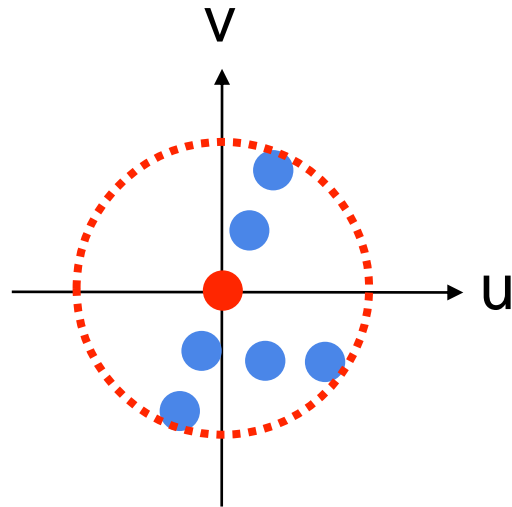
N points in  $(X, Y)$



# Hierarchical Point Feature Learning

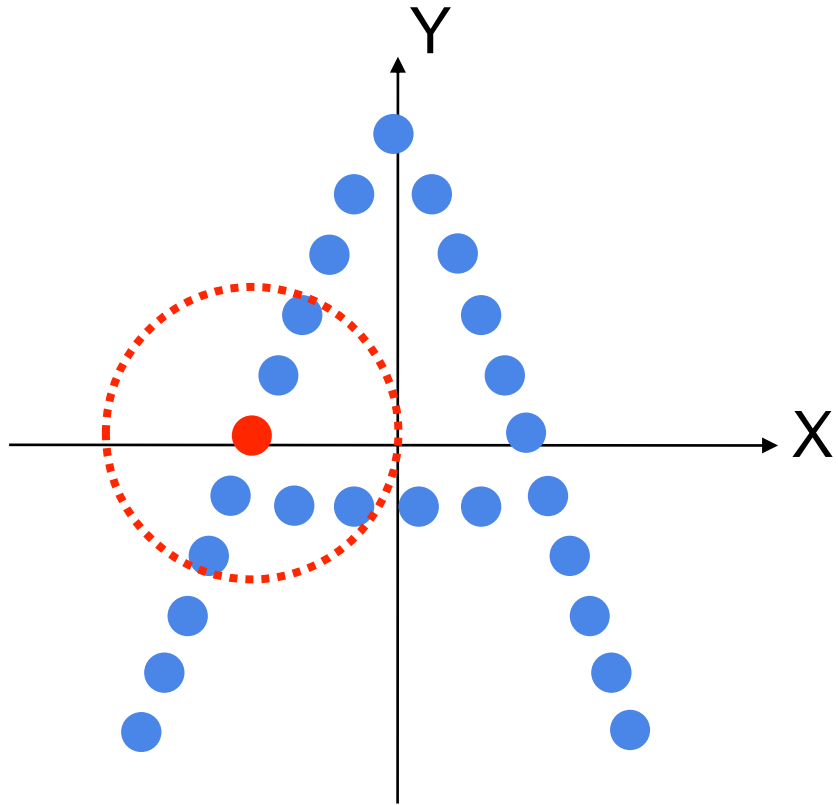


N points in  $(X, Y)$



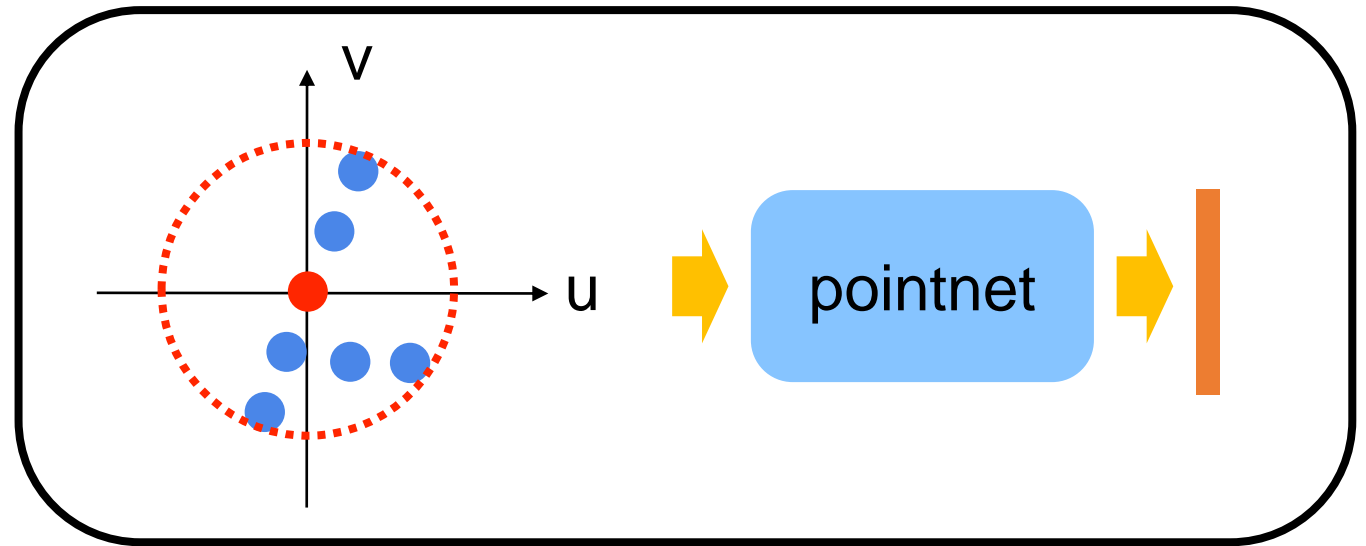
k points in local  
coordinates  $(u, v)$

# Hierarchical Point Feature Learning



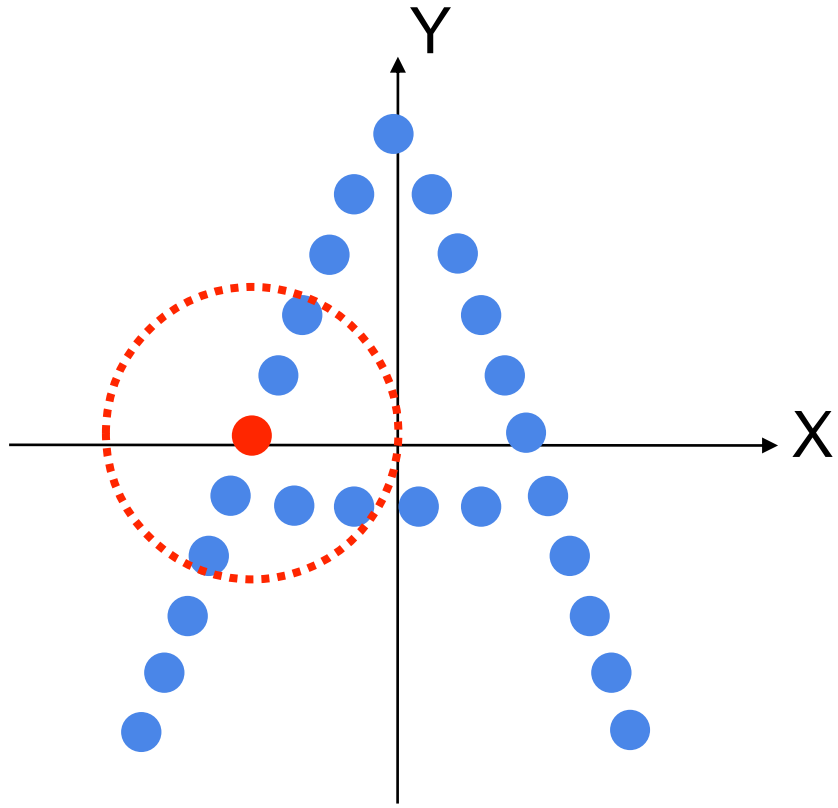
N points in  $(X, Y)$

Apply pointnet at a local region

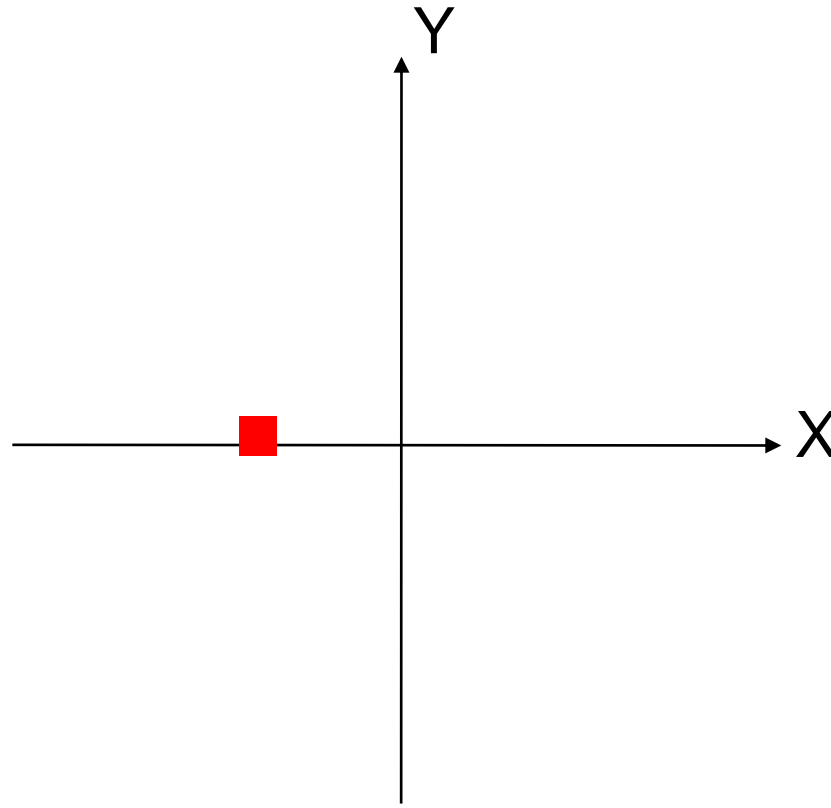


k points in local coordinates  $(u, v)$

# Hierarchical Point Feature Learning



N points in  $(X, Y)$

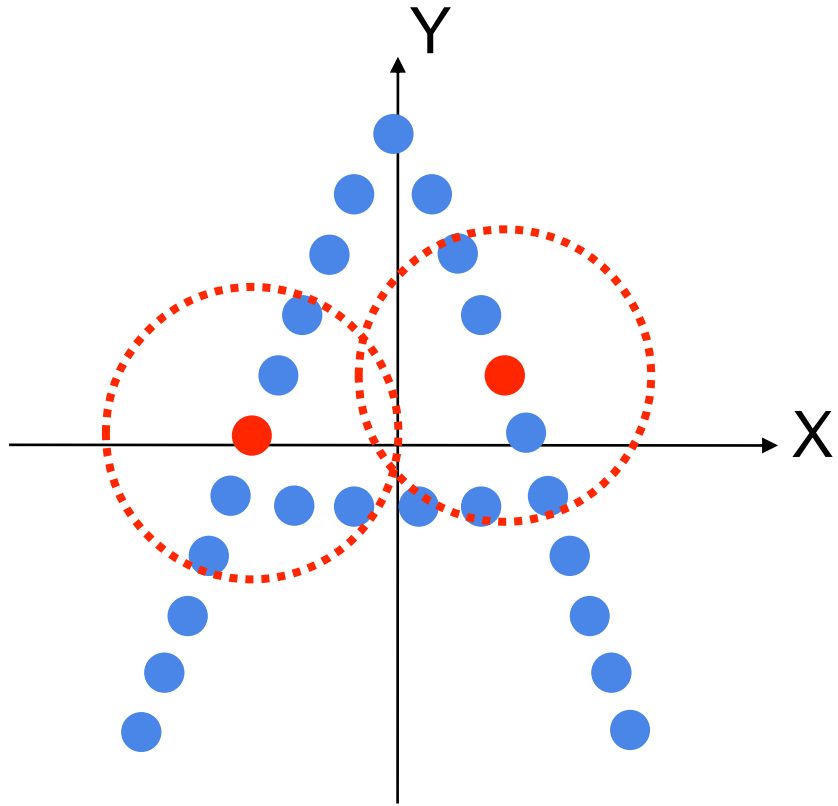


points in  $(X, Y, \mathbf{F})$

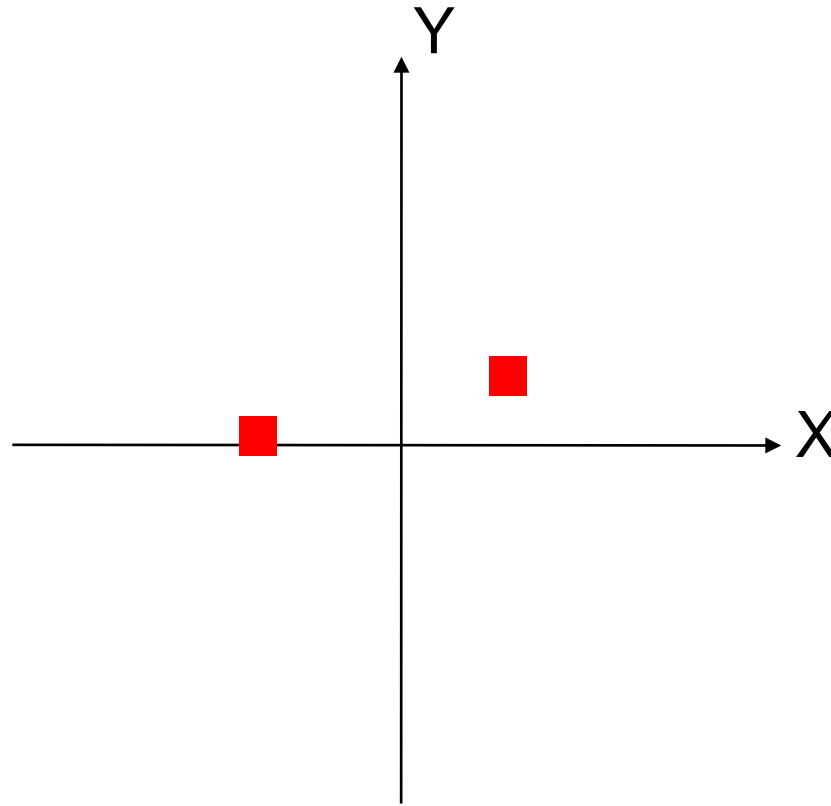
Euclidean space

**high-dim feature space**

# Hierarchical Point Feature Learning

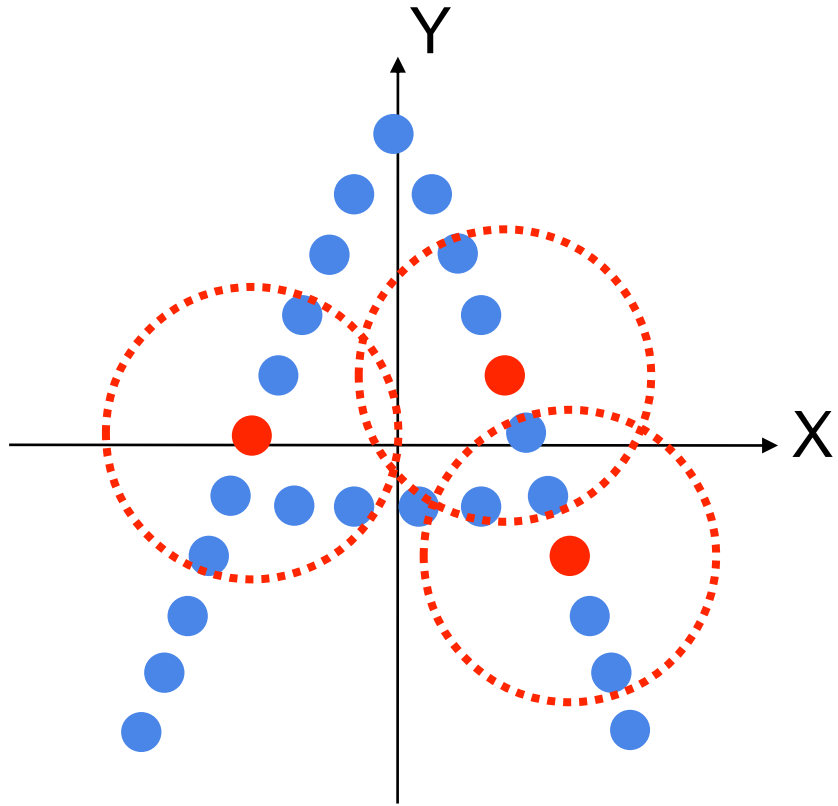


N points in  $(X, Y)$

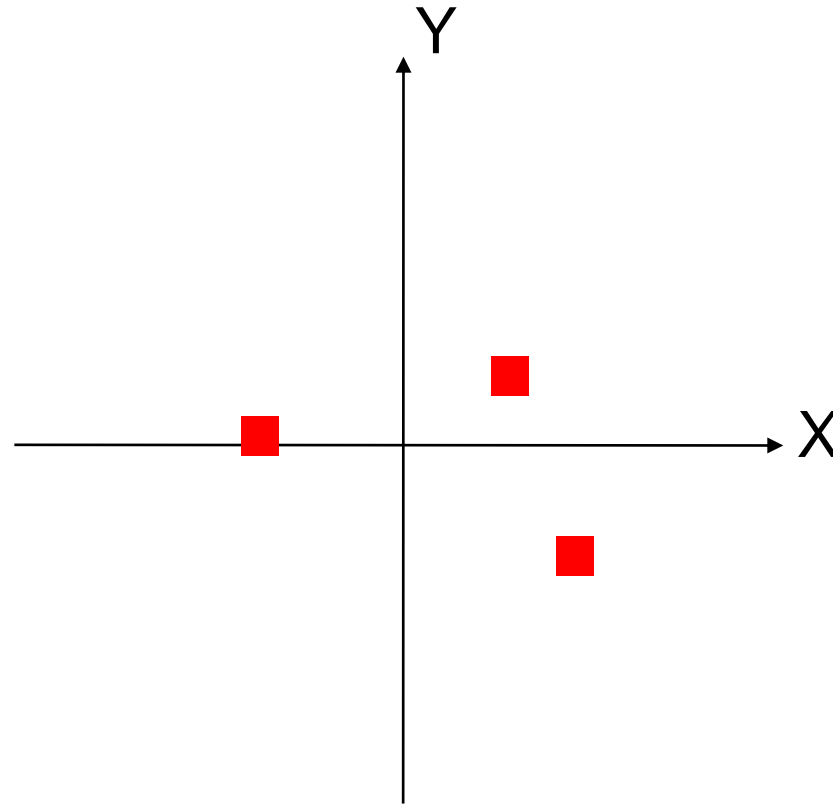


points in  $(X, Y, \mathbf{F})$

# Hierarchical Point Feature Learning

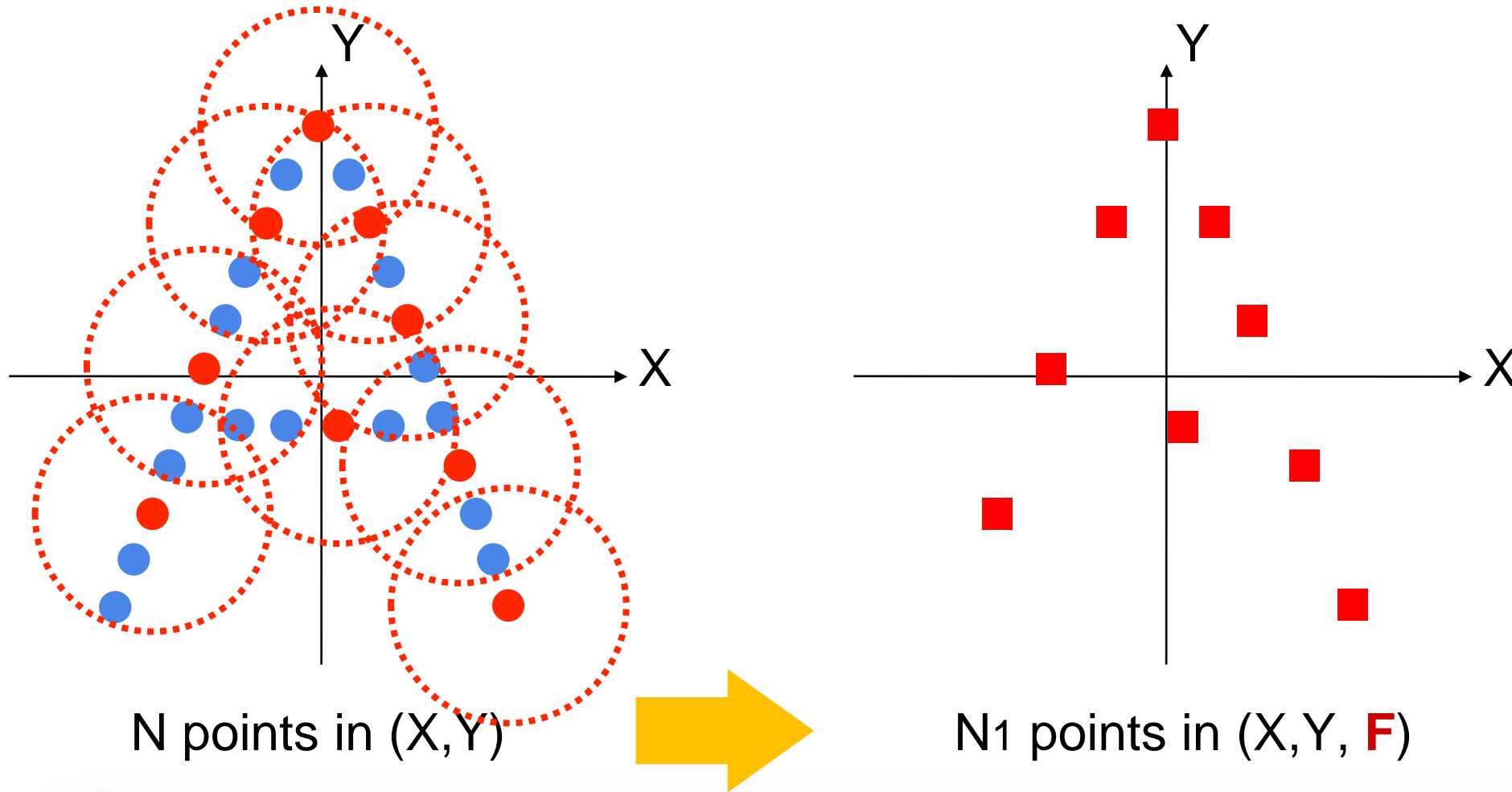


N points in  $(X, Y)$



points in  $(X, Y, \mathbf{F})$

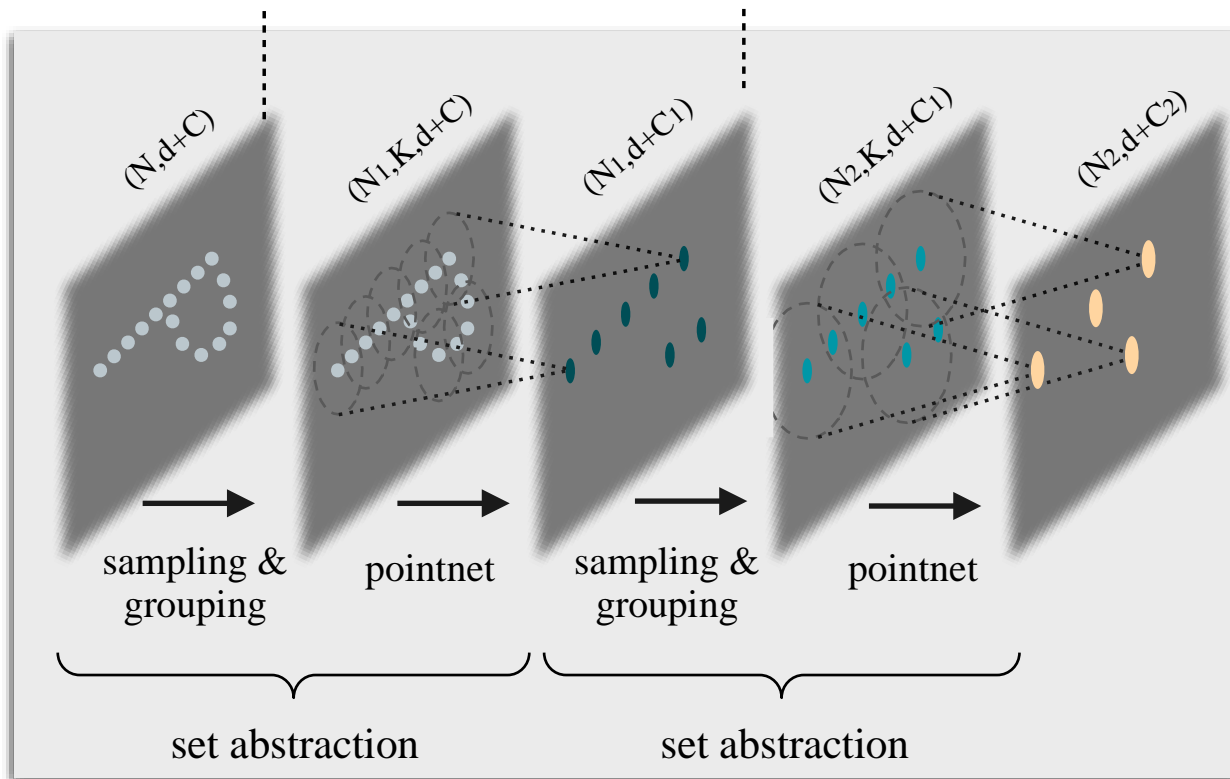
# Hierarchical Point Feature Learning



**Set Abstraction:** farthest point sampling + grouping + pointnet

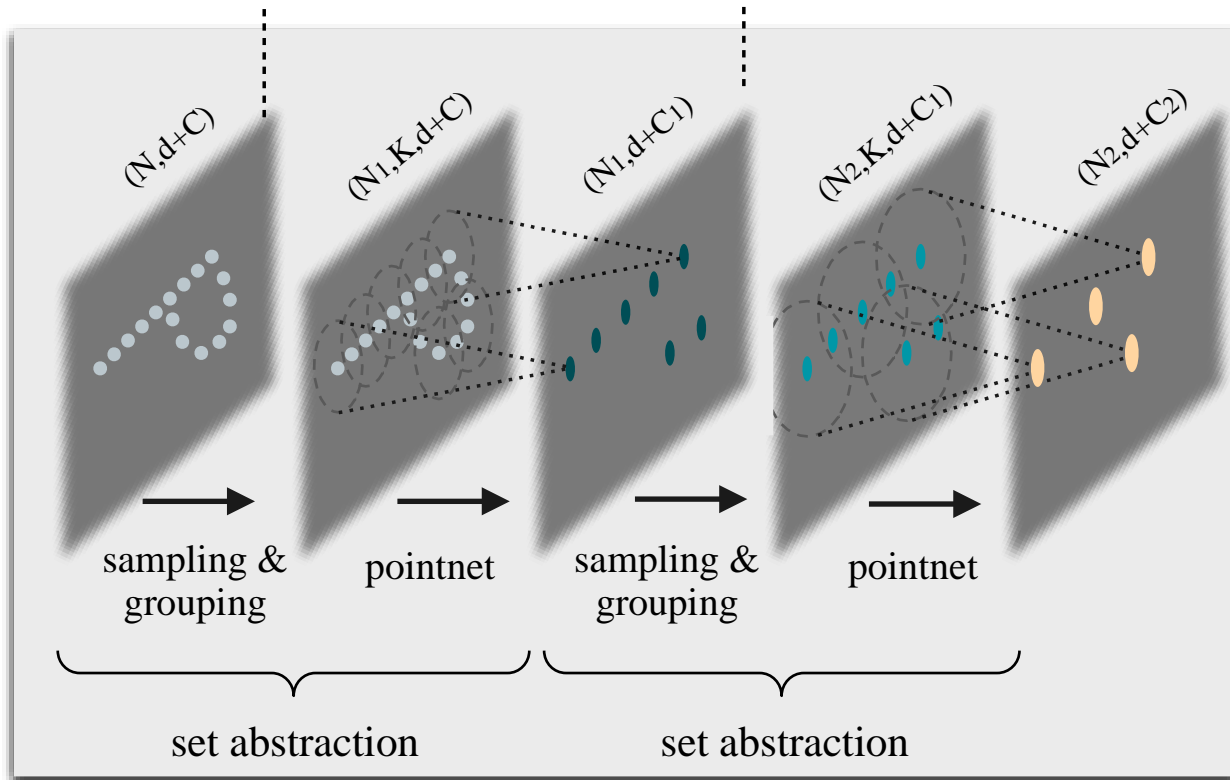
# PointNet++ for Classification and Segmentation

## *Hierarchical point set feature learning*

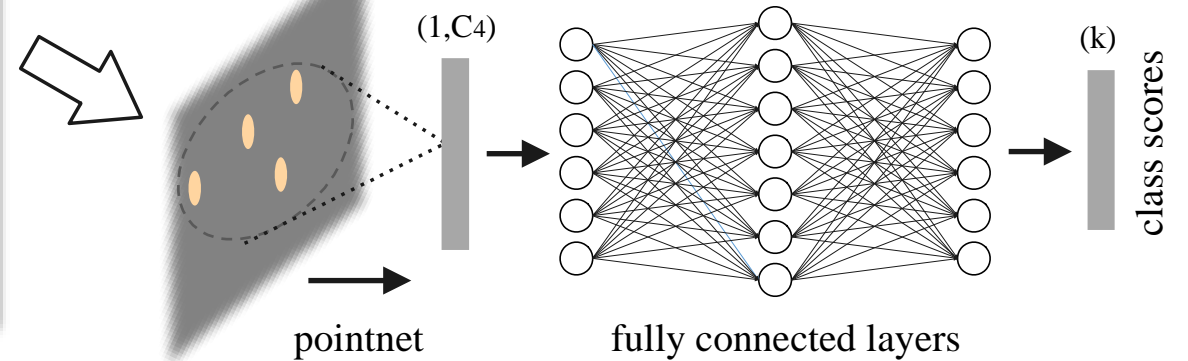


# PointNet++ for Classification and Segmentation

## *Hierarchical point set feature learning*

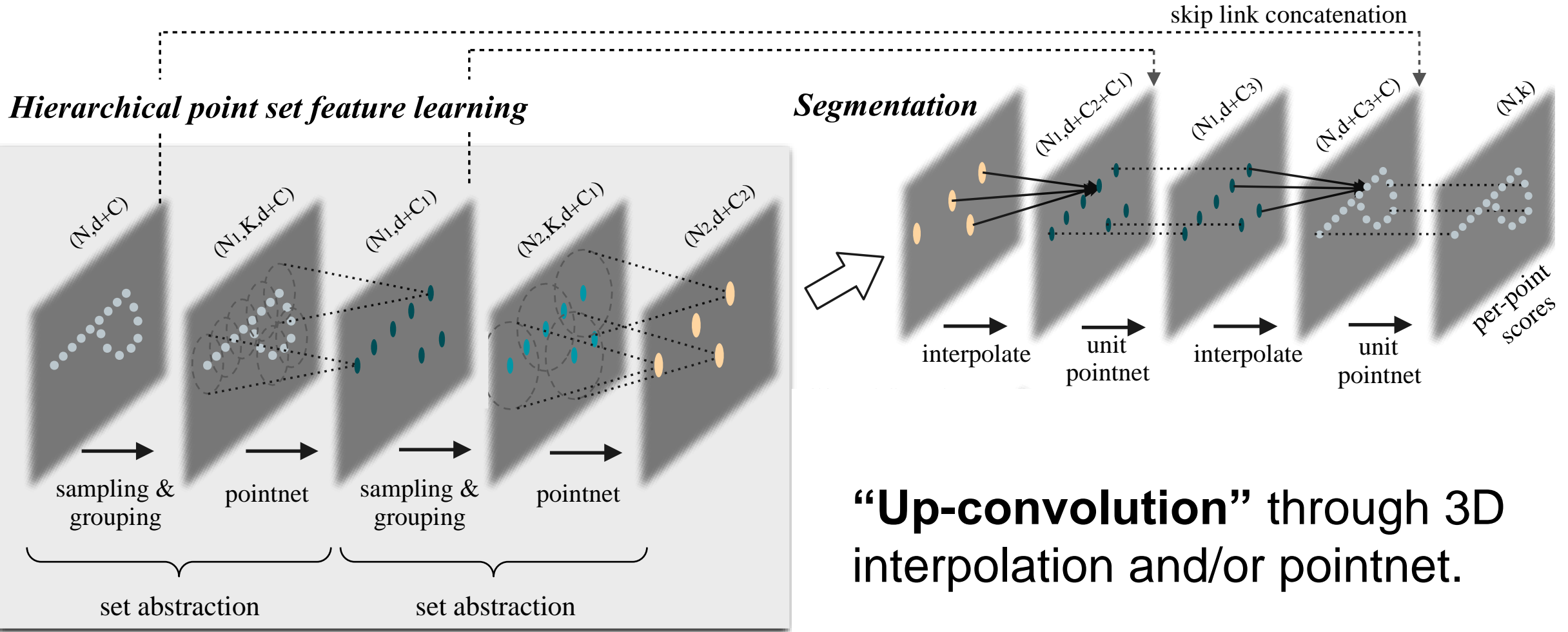


## *Classification*





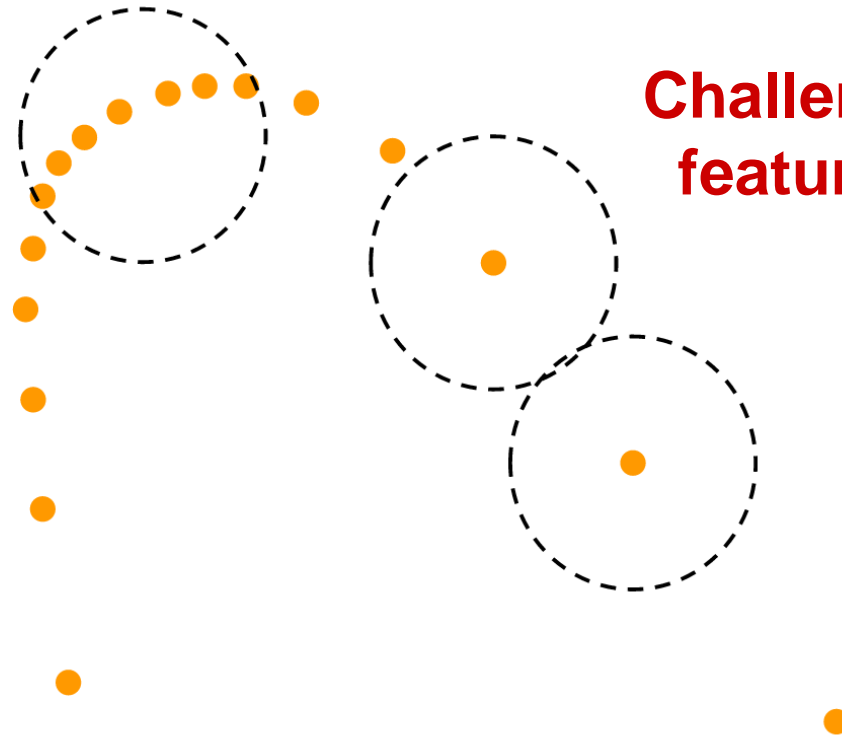
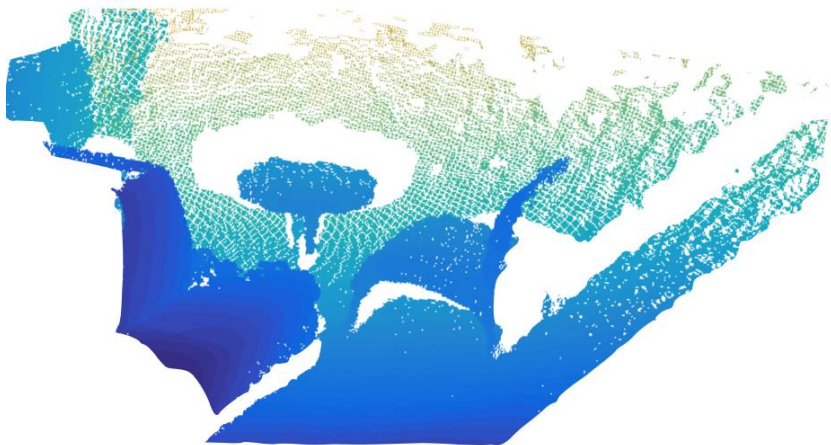
# PointNet++ for Classification and Segmentation



**“Up-convolution”** through 3D interpolation and/or pointnet.

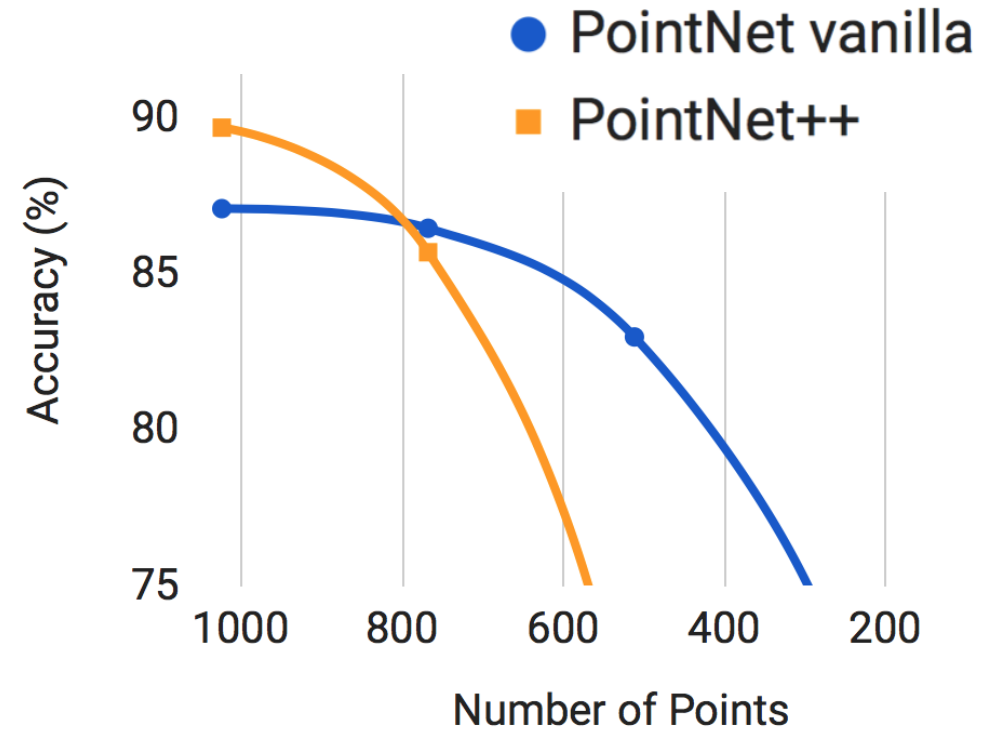
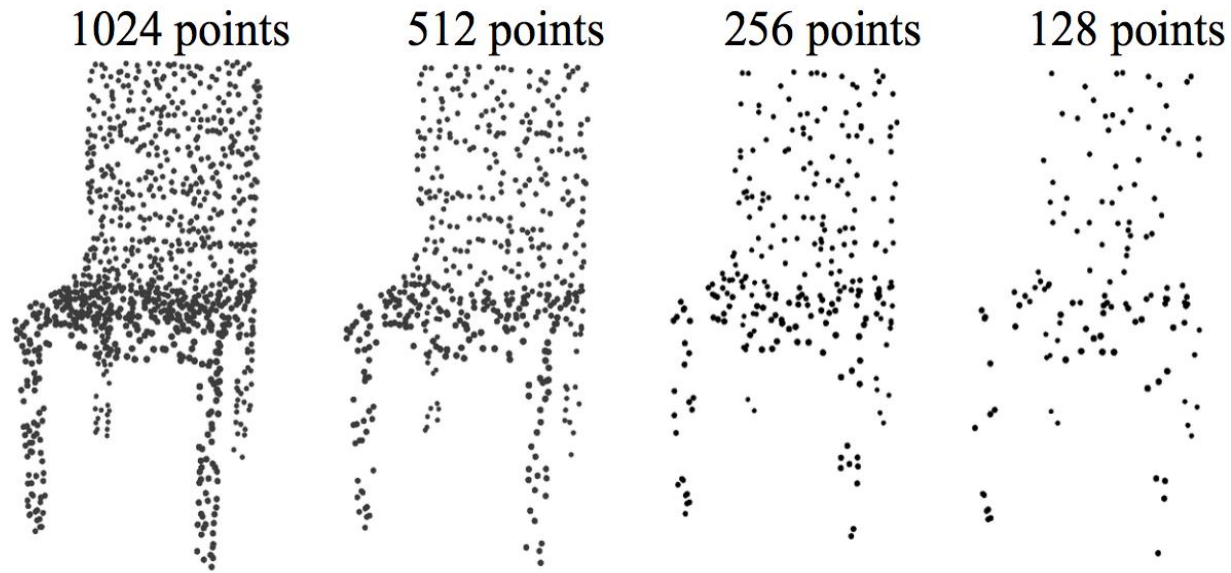
# Non-uniform Sampling Density in Point Clouds

Density variation is a common issue in 3D point cloud processing  
- perspective effect, radial density variation, motion etc.



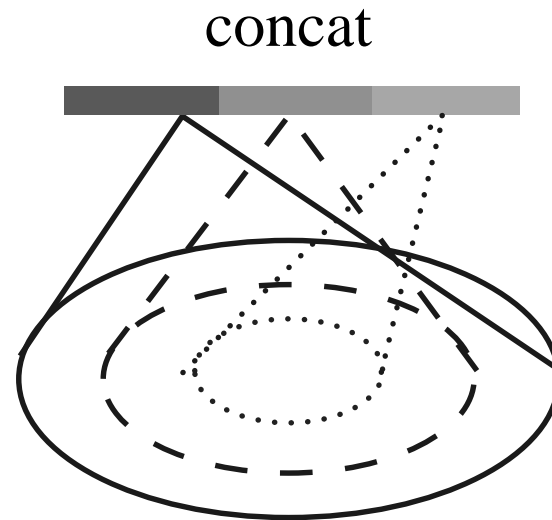
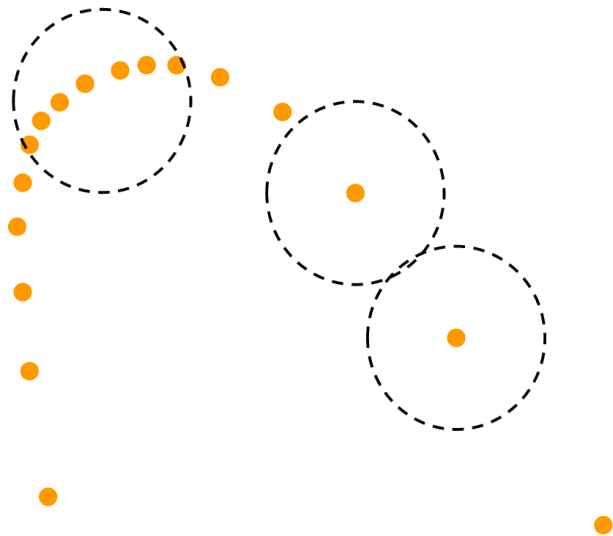
**Challenge for local  
feature learning!**

# Density Variation Affects Hierarchy



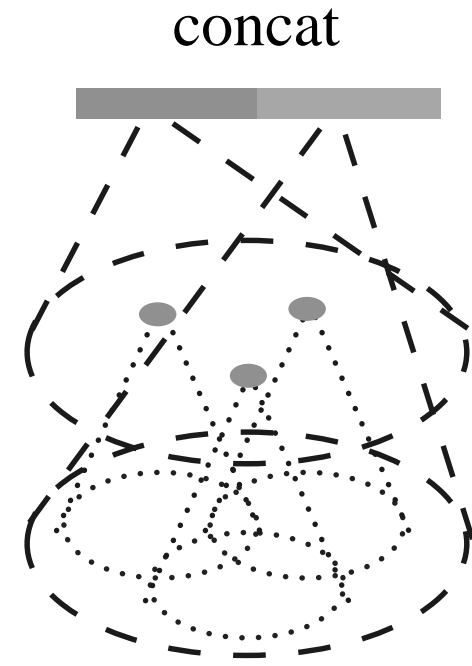
**Small kernels suffer from varying densities!**

# Robust Learning Under Varying Sampling Density



(a)

Multi-scale grouping (MSG)

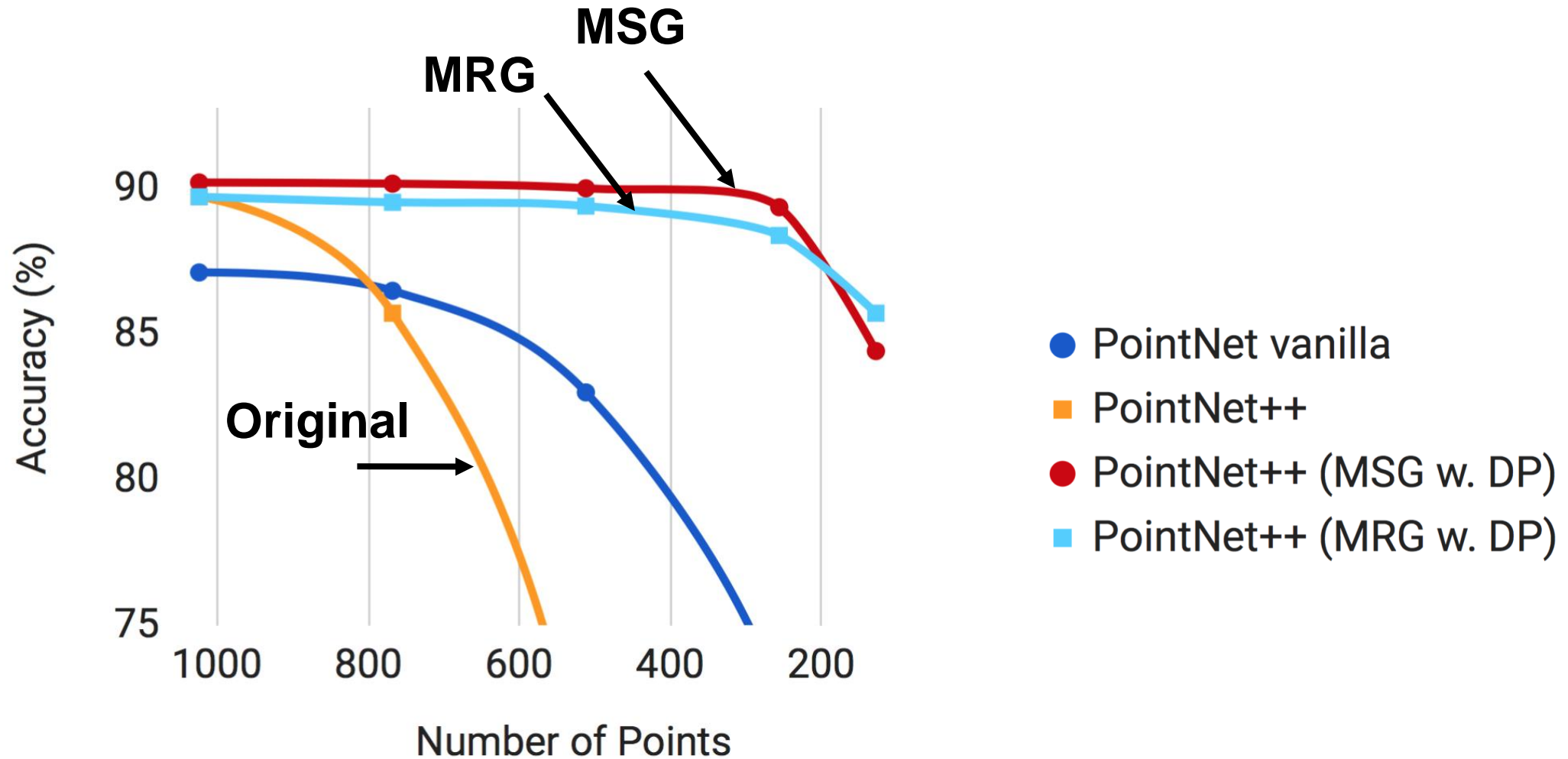


(b)

Multi-res grouping (MRG)

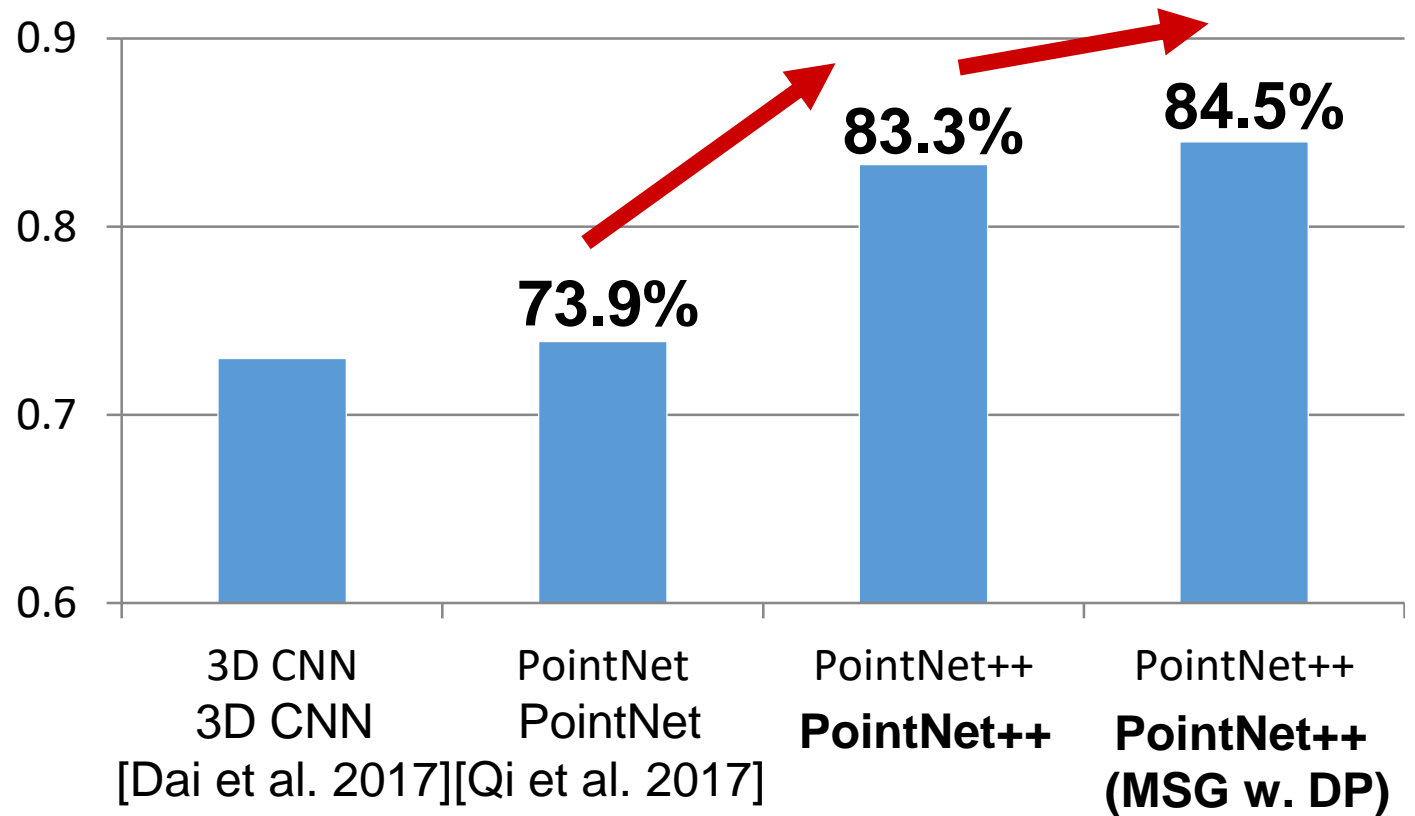
*During Training: input point dropout with random dropout ratio*

# Robust Learning Under Varying Sampling Density



# PointNet++ Results: Scene Parsing

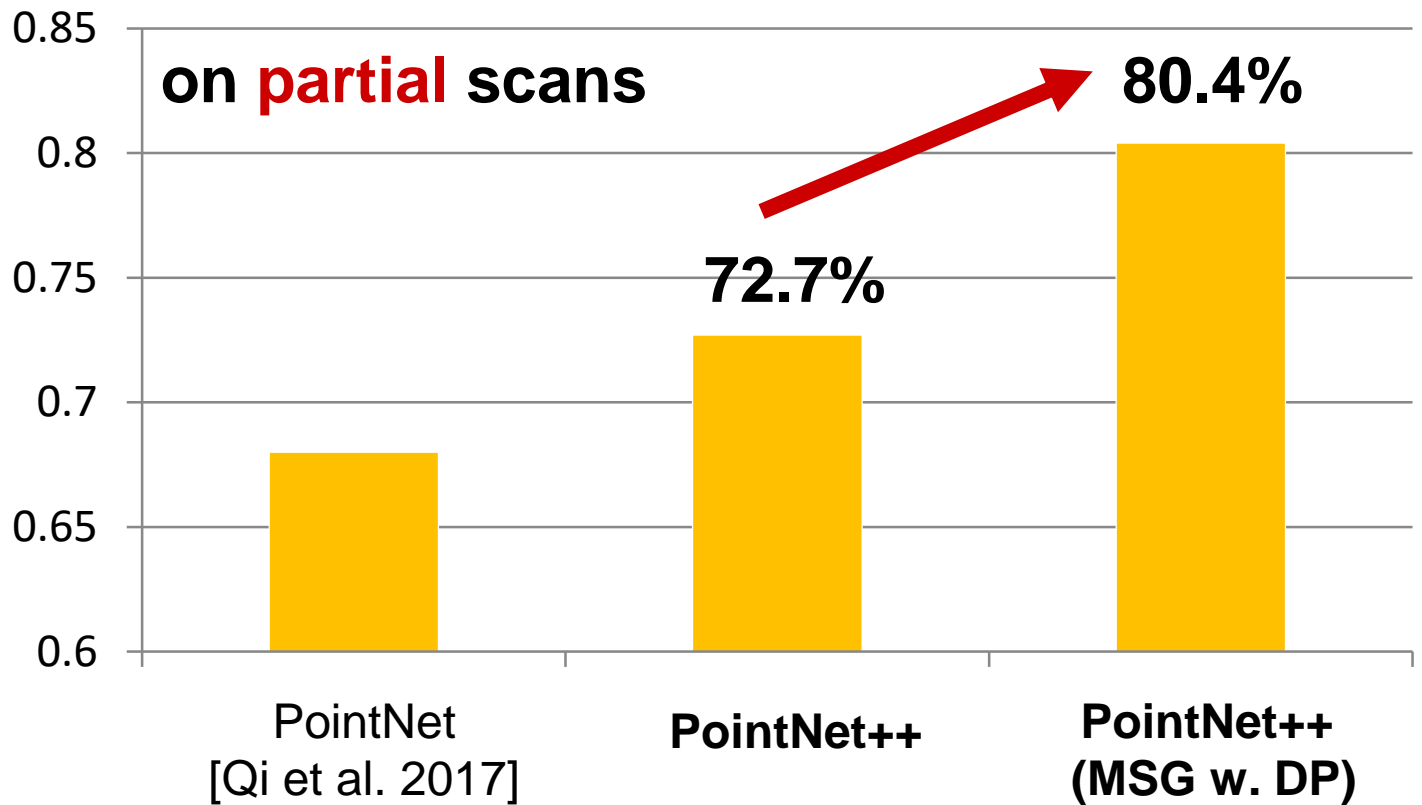
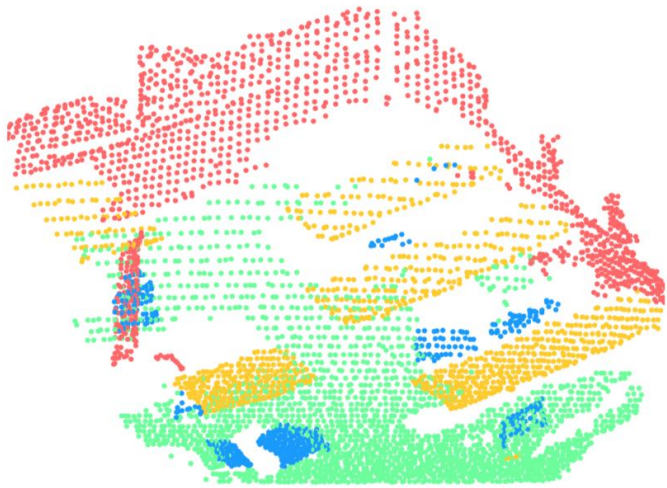
**Better accuracy with hierarchical learning.**



*dataset: ScanNet; metric: per-point semantic classification accuracy (%)* 70

# PointNet++ Results: Scene Parsing

**Robust layers for non-uniform densities (MSG) helps a lot.**

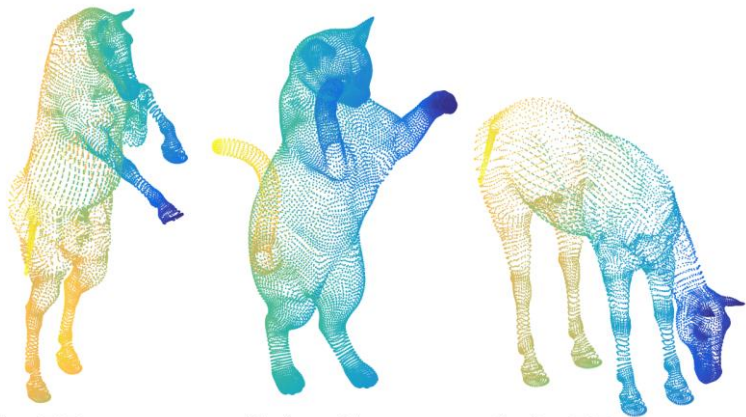


*dataset: ScanNet; metric: per-point semantic classification accuracy (%)*

# PointNet++ Results: Non-Euclidean Space

**For organic shape recognition, PointNet++ can generalize to non-Euclidean space**

- ❖ intrinsic point features (HKS, WKS, Gaussian curvature)
- ❖ intrinsic distance metric (geodesic)



(a) Horse (b) Cat (c) Horse

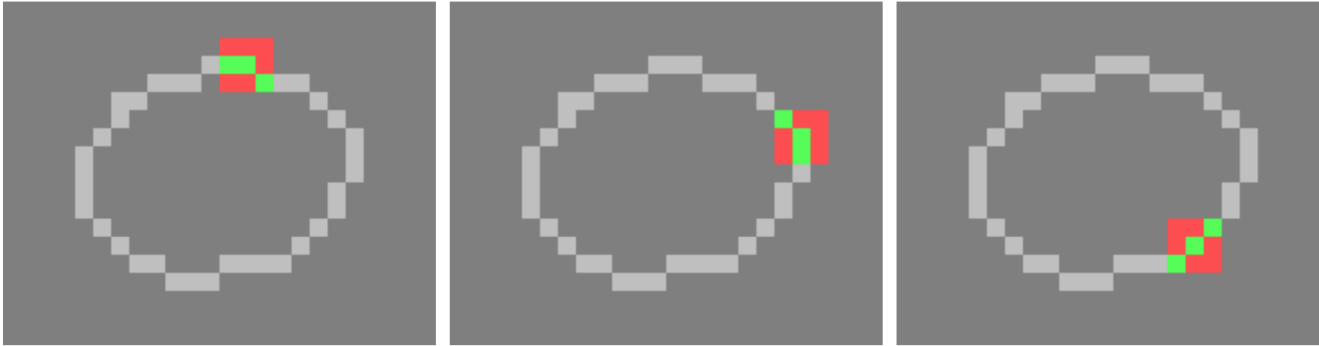
|             | Metric space  | Input feature      | Accuracy (%) |
|-------------|---------------|--------------------|--------------|
| DeepGM [13] | -             | Intrinsic features | 93.03        |
| Ours        | Euclidean     | XYZ                | 60.18        |
|             | Euclidean     | Intrinsic features | 94.49        |
|             | Non-Euclidean | Intrinsic features | <b>96.09</b> |

*dataset: SHREC15; metric: shape classification accuracy (%)*

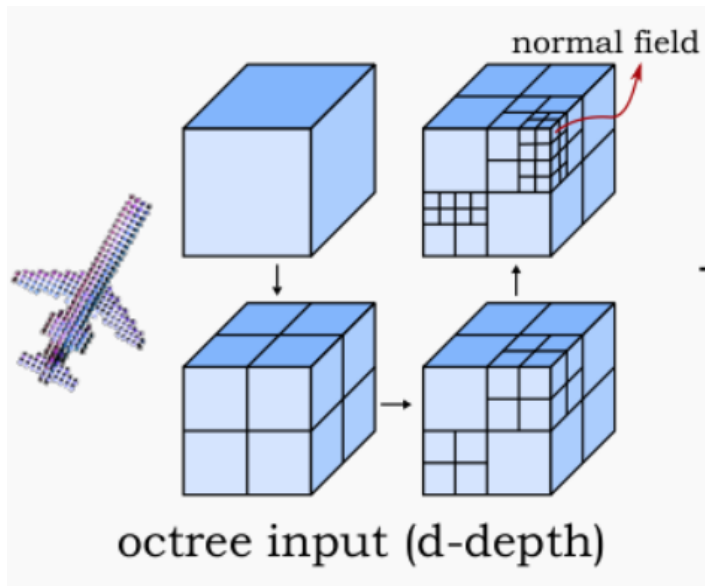


# More Types of Deep Networks Related to Point Clouds

# Sparse 3D CNNs



Submanifold Sparse Convolutional Networks  
[Graham et al. 2017]



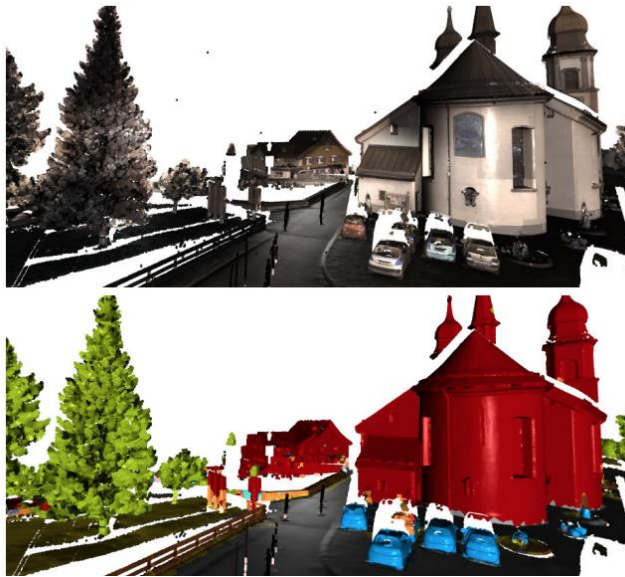
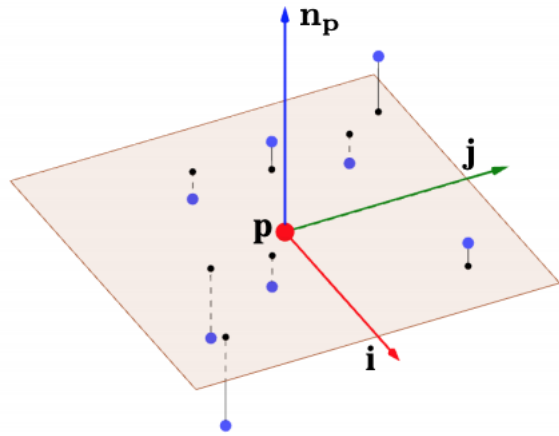
OctNet

[Riegler et al. 2017]

O-CNN: Octree based Convolutional Neural Networks

[Wang et al. 2017]

# Surface-Based Convolutions



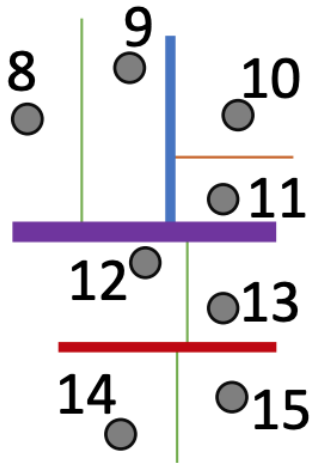
Tangent Convolutions  
[Tatarchenko et al. 2018]



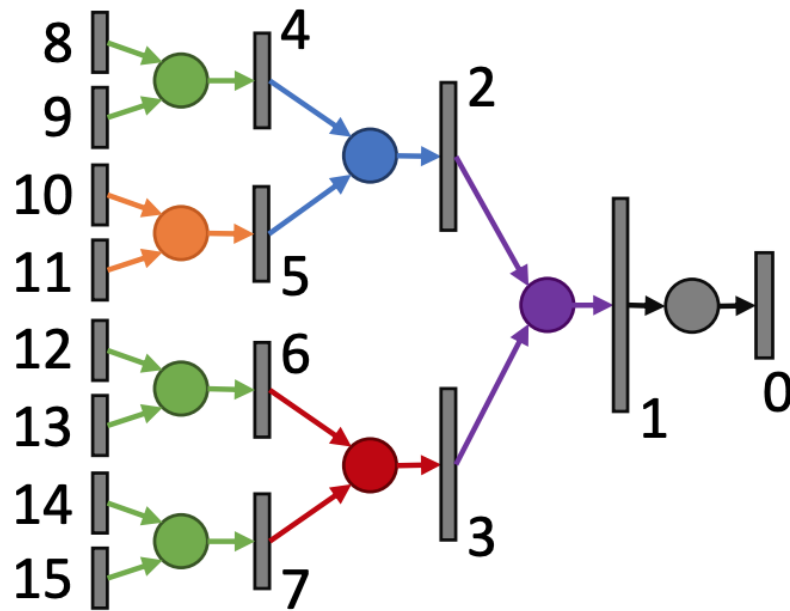
Surface Convolution

SurfConv  
[Chu et al. 2018]

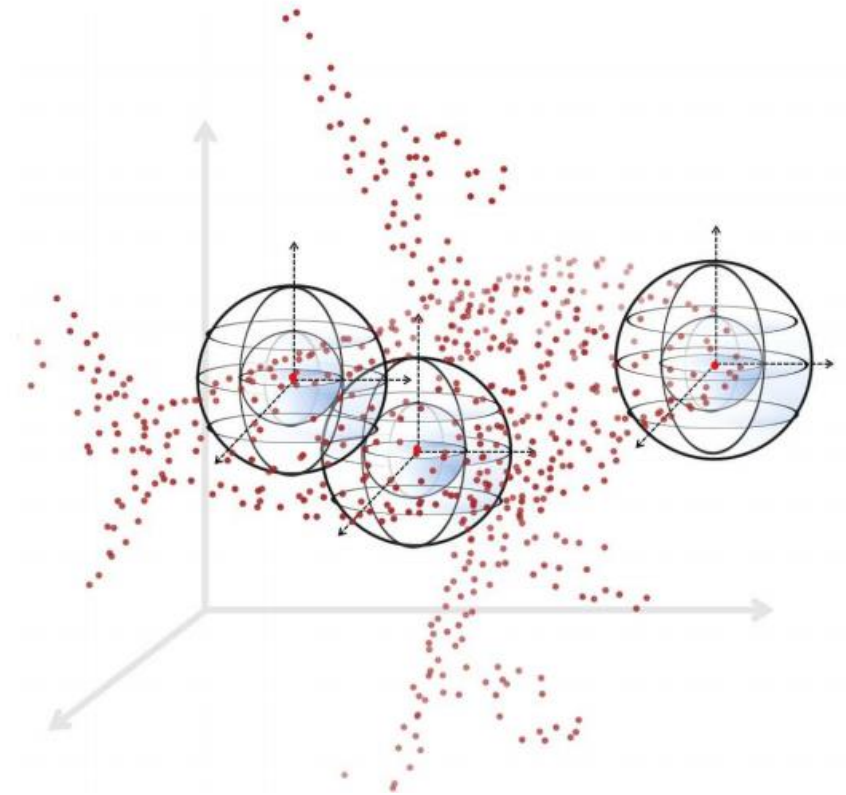
# Classic Spatial Representations + NN



kd-tree



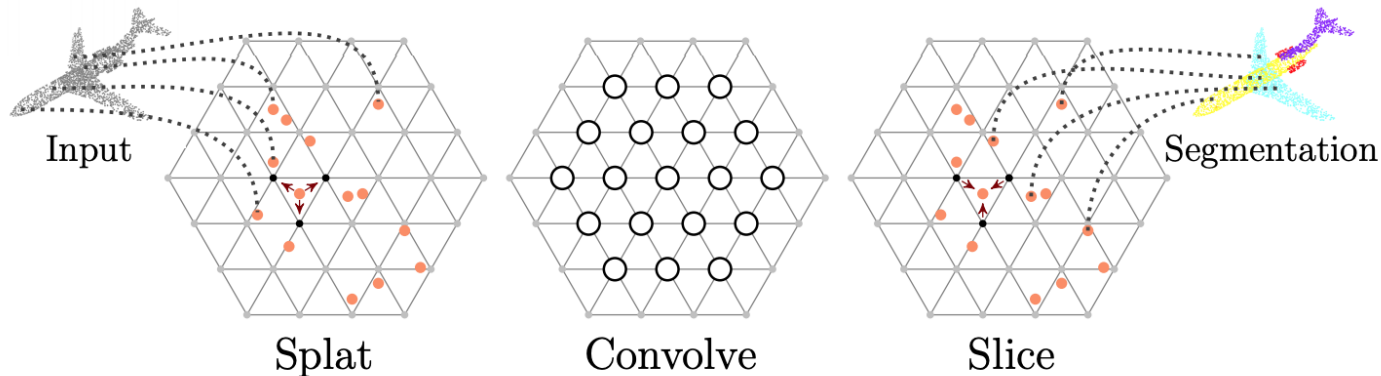
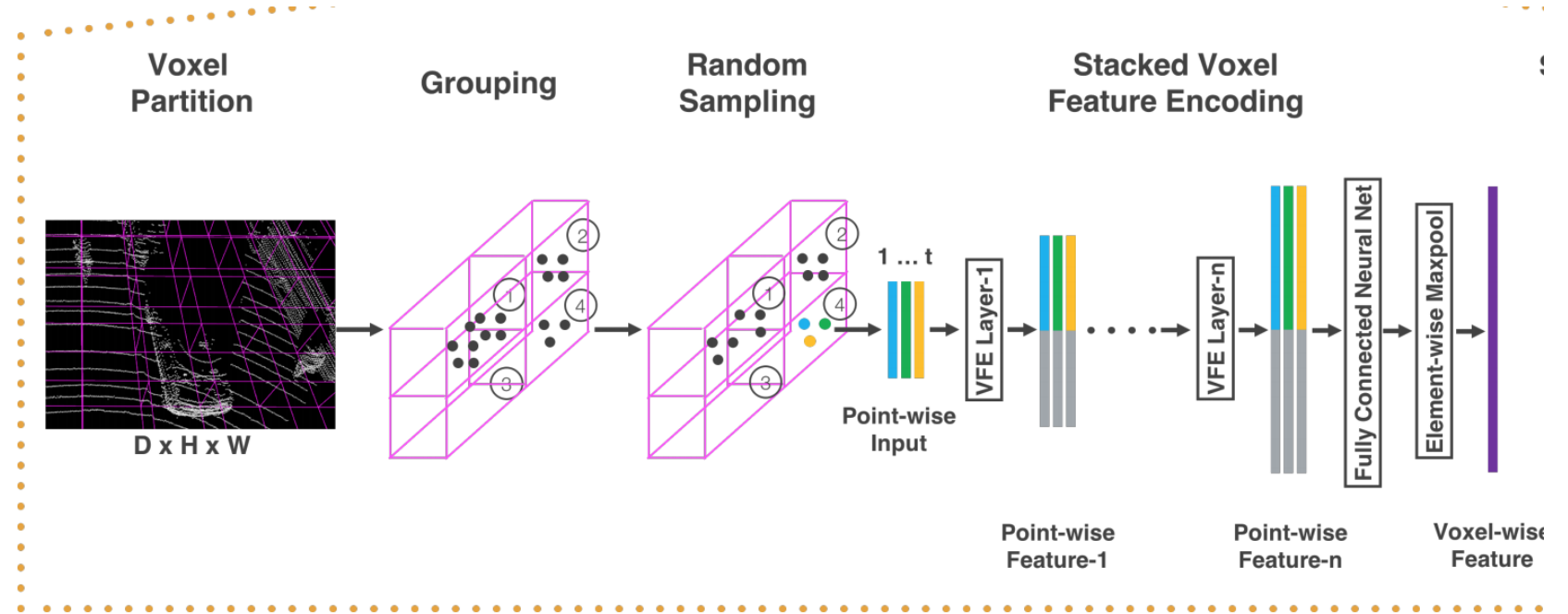
Kd-Net  
[Klokov et al. 2017]



ShapeContextNet  
[Xie et al. 2018]

# Hybrid Networks: Grids + Points

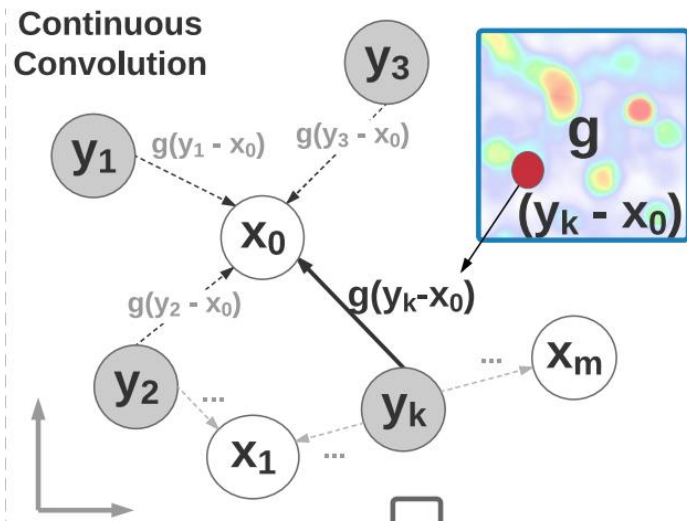
VoxelNet  
[Zhou et al. 2018]



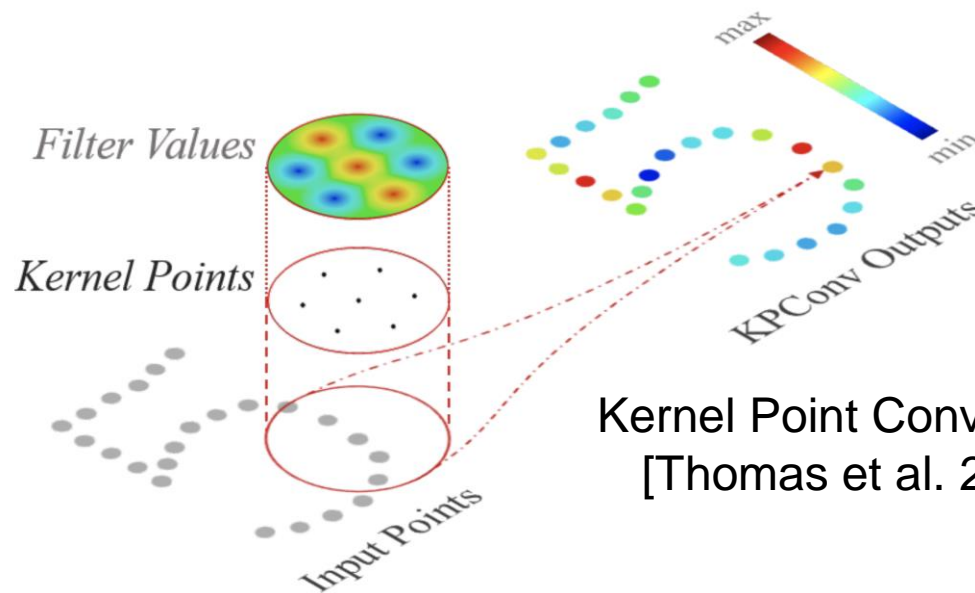
Bilateral convolution layers on a sparse lattice

SPLATNet  
[Su et al. 2018]

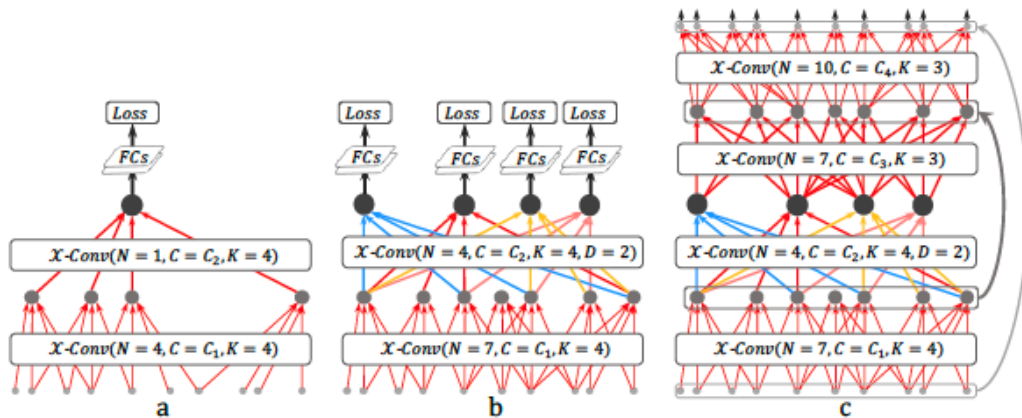
# Point Cloud Convolution Variants



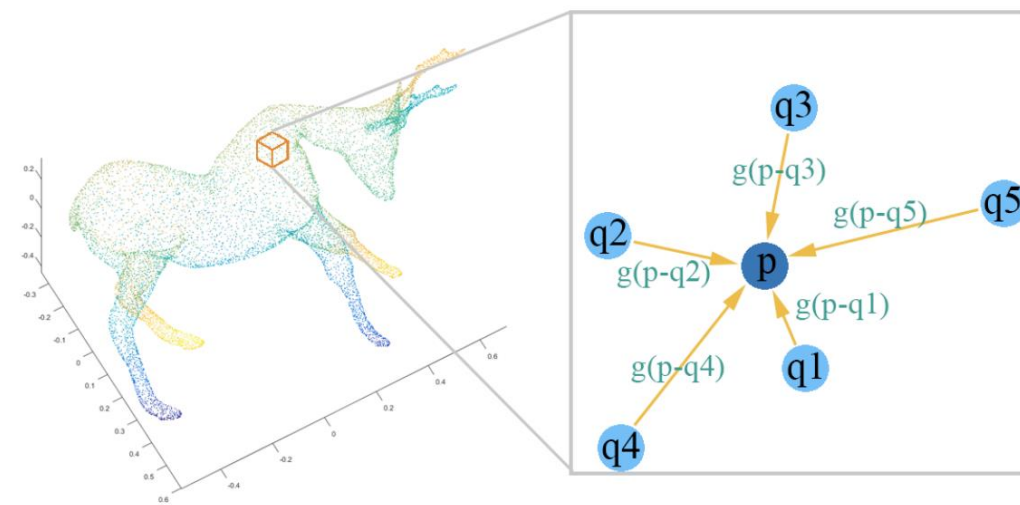
Deep Parametric Continuous Convolution  
[Wang et al. 2018]



Kernel Point Convolution  
[Thomas et al. 2019]

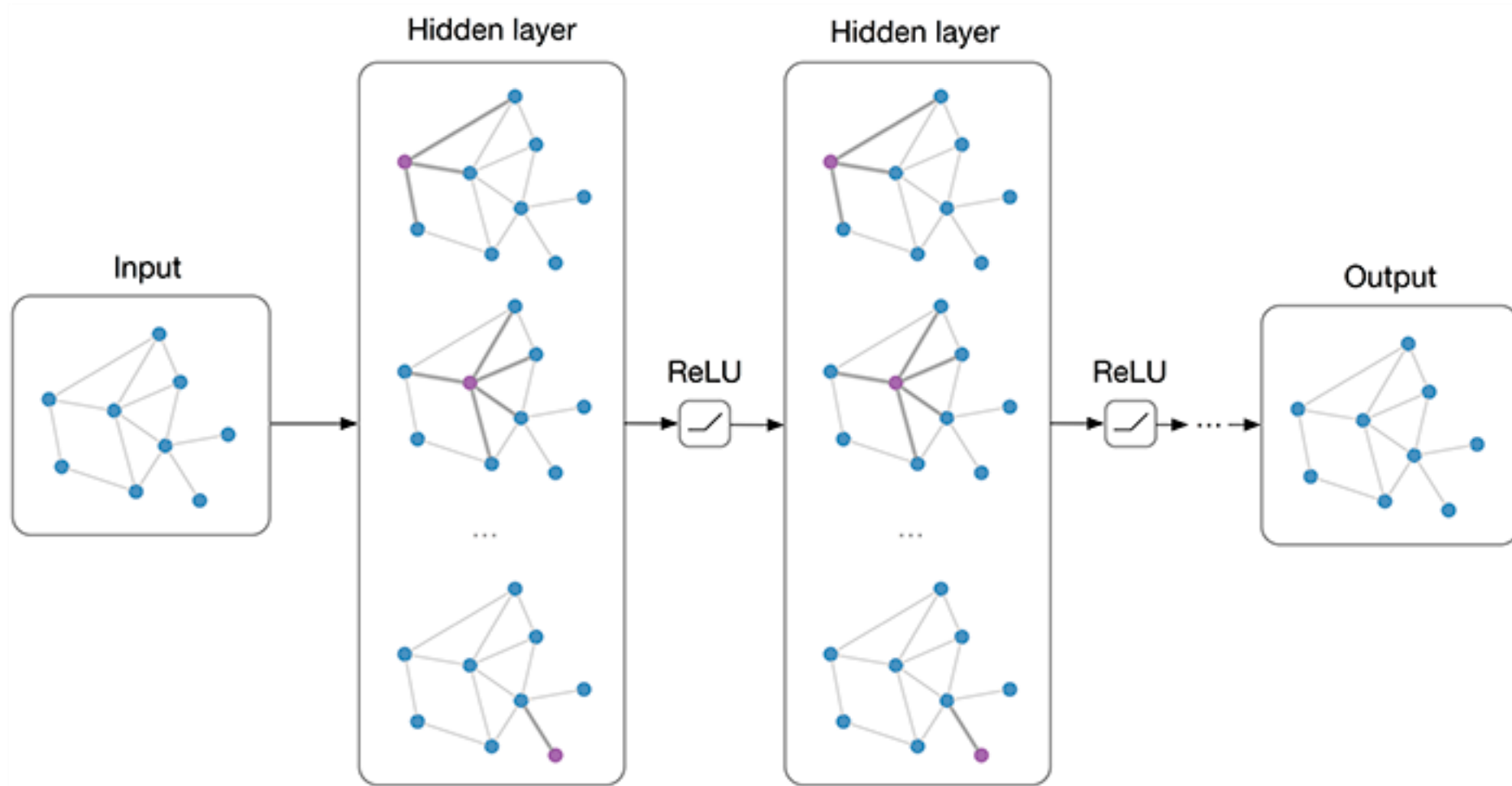


PointCNN  
[Li et al., 2018]



SpiderCNN  
[Xu et al. 2018]

# Graph Neural Networks



# Which Network Architecture Is Best?

- Any distance metric among points?
- 3D points or higher-dim points?
- Single object or multi-object?
- Depth image or fused point clouds?
- Care about efficiency?

Is there a universally best architecture?



# 3D Scene Understanding with PointNet and PointNet++

# 3D Scene Understanding with PointNets

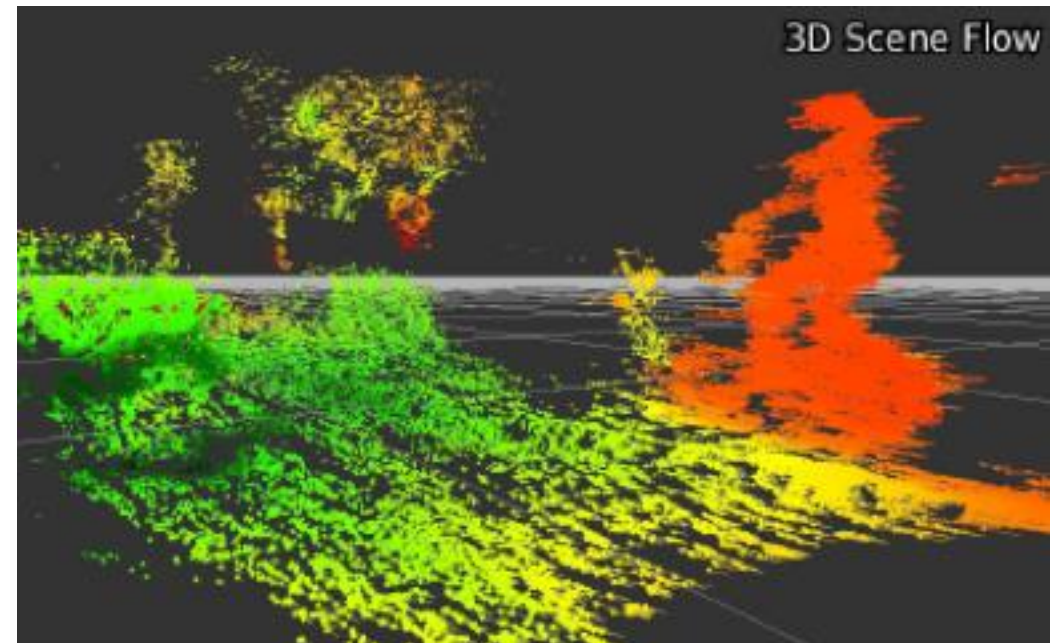
- PointNet and PointNet++ lead to new **3D centric approaches** to scene understanding

## 3D Object Detection



source: SUN RGB-D by Song et al.

## 3D Scene Flow



source: Wedel et al.

# 3D Scene Understanding with PointNets

- PointNet and PointNet++ lead to new **3D centric approaches** to scene understanding

## 3D Object Detection



source: SUN RGB-D by Song et al.

## 3D Scene Flow

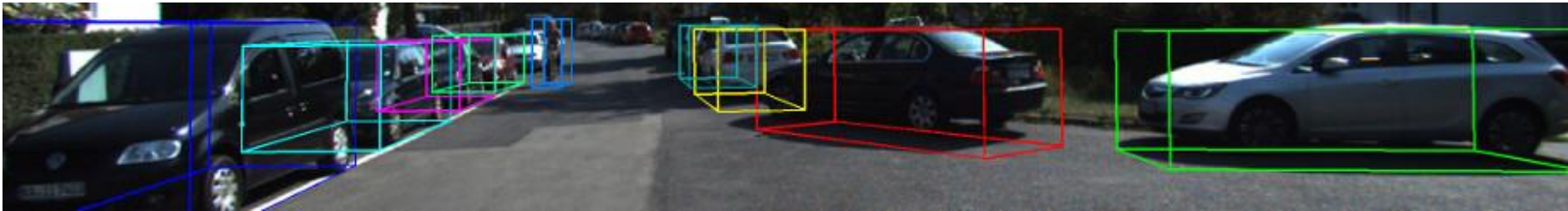


source: Wedel et al.

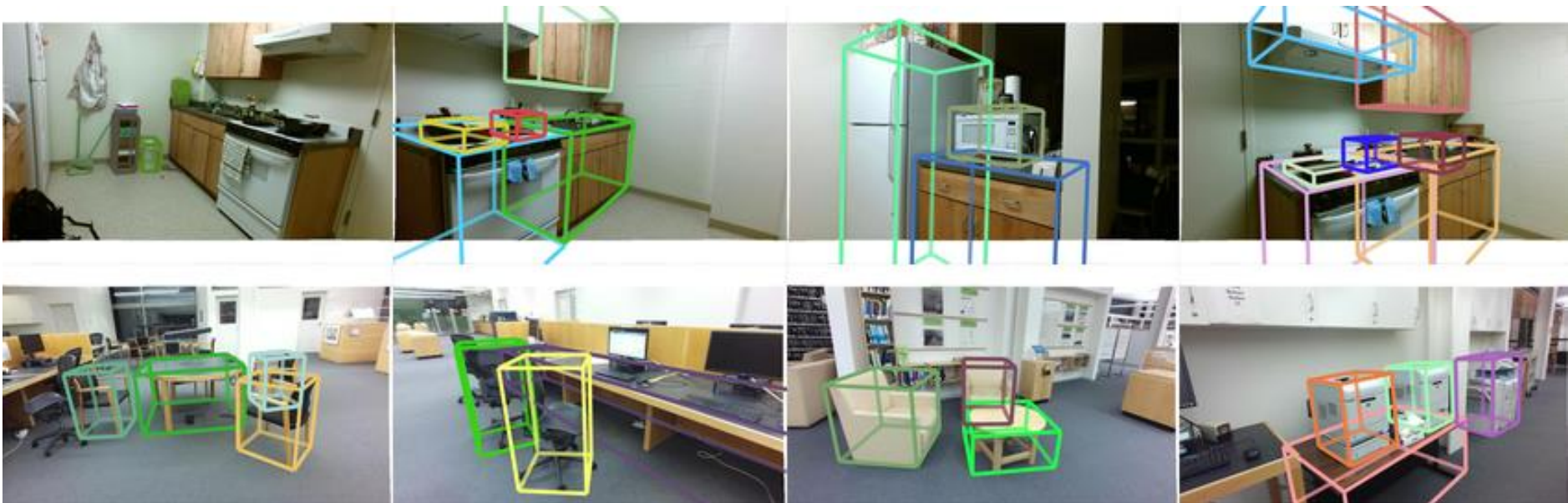
# 3D Object Detection

- Input: RGB-D data
- Output: 3D bounding boxes of objects

*KITTI:*



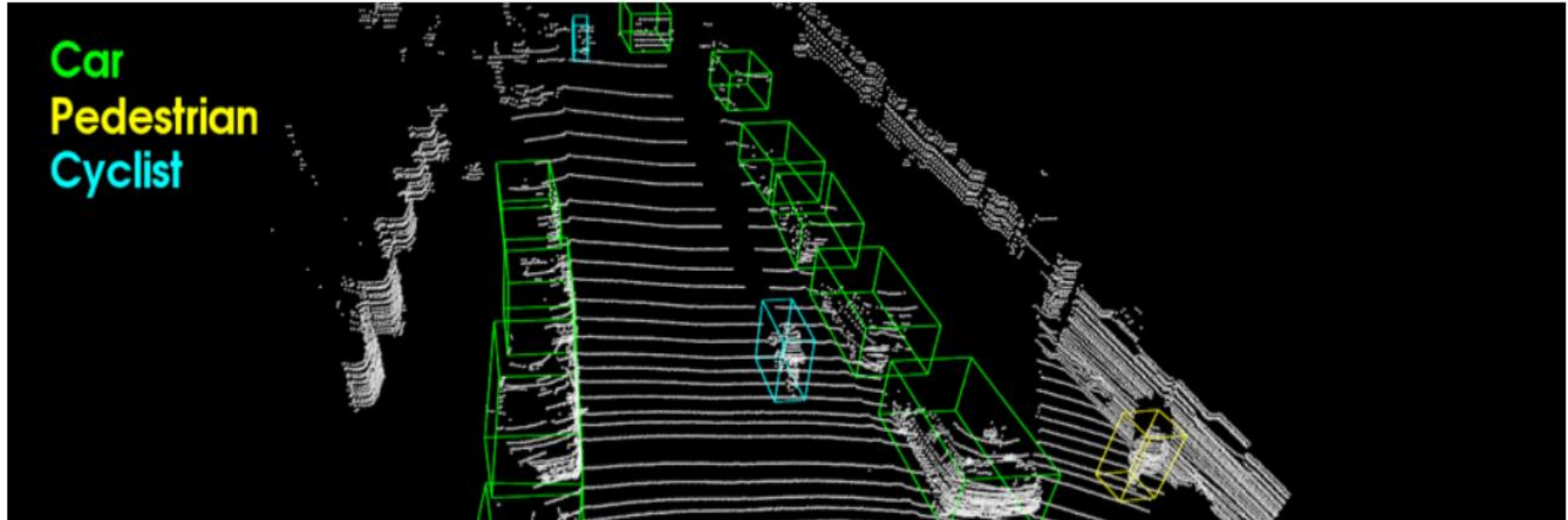
*SUN RGB-D:*



# 3D Object Detection

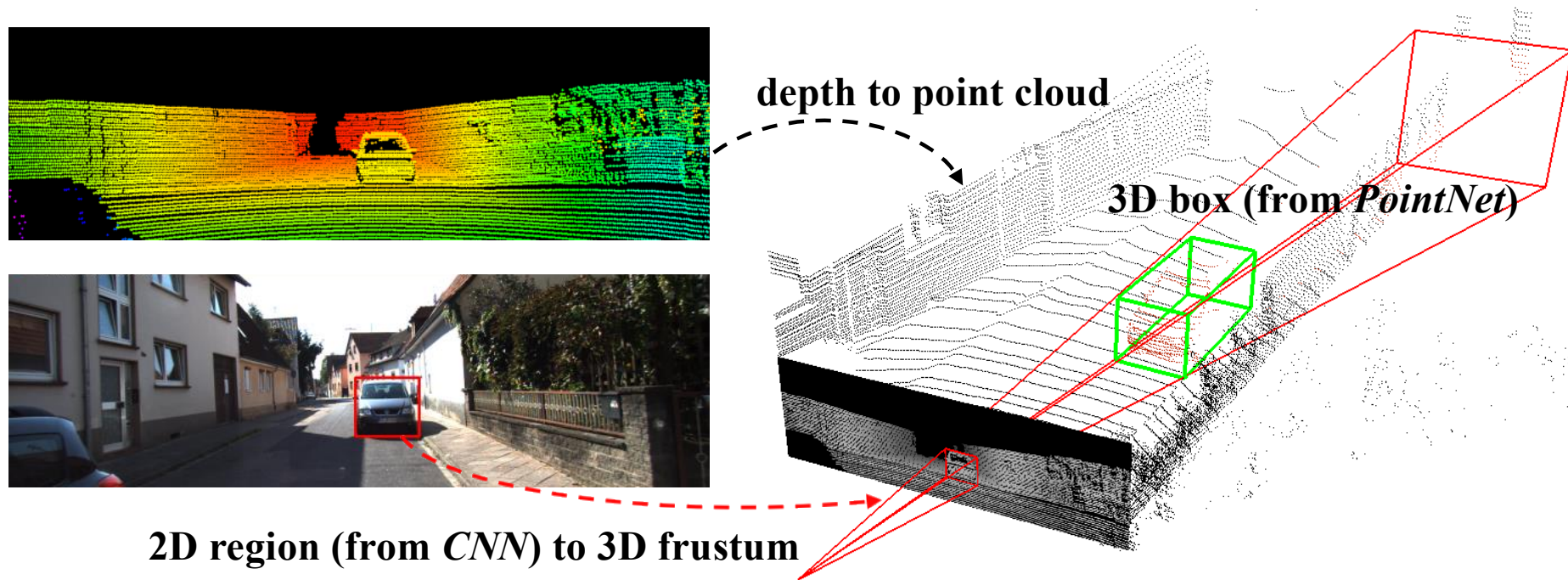
- Input: RGB-D data
- Output: 3D (amodal) bounding boxes of objects

*KITTI:*



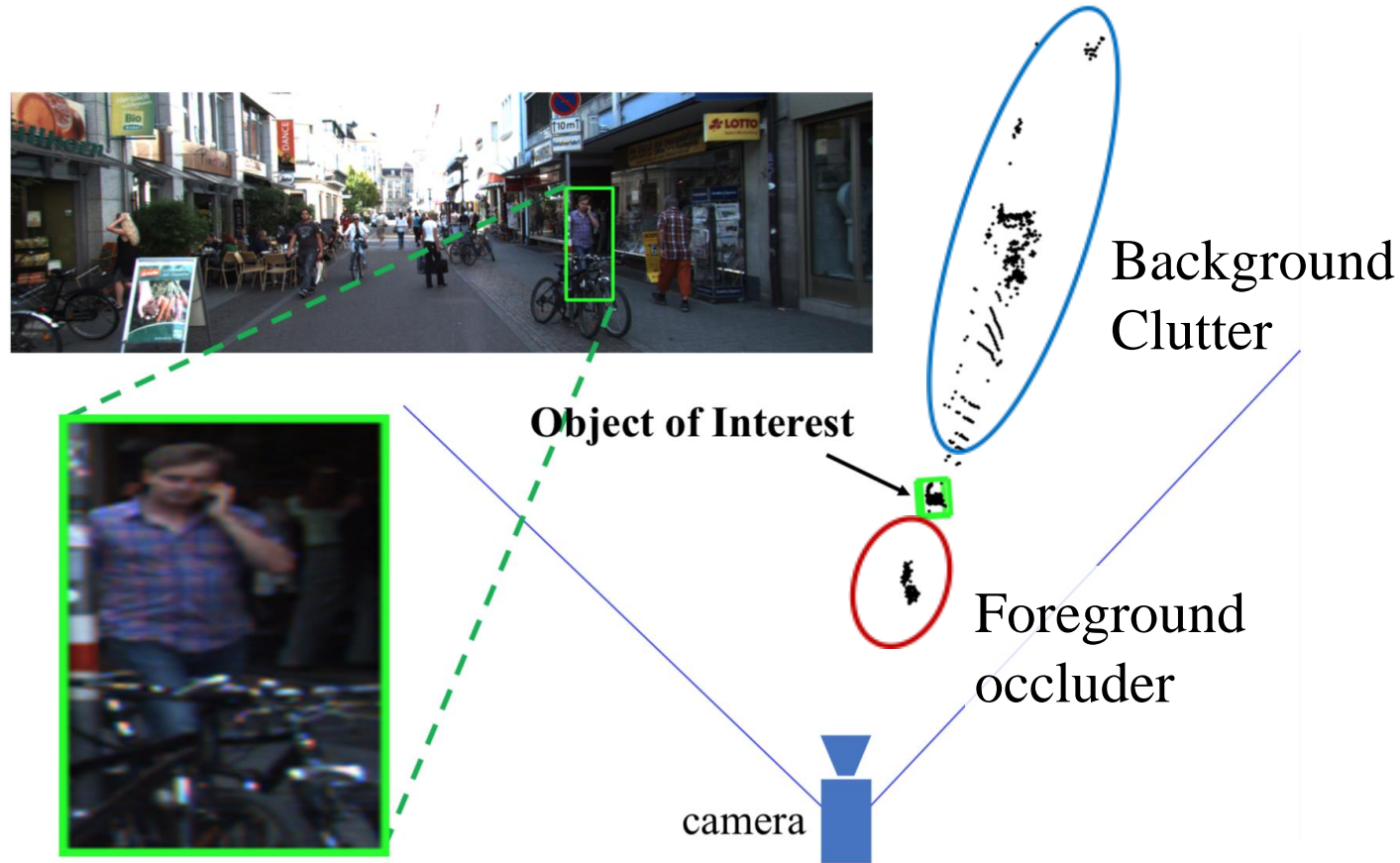
*Figure from VoxelNet [Zhou et al. 2018]*

# Frustum PointNets for 3D Object Detection



- + **Leveraging mature 2D detectors** for region proposal. greatly reducing 3D search space.
- + **Solving 3D detection problem with 3D data and 3D deep learning.**

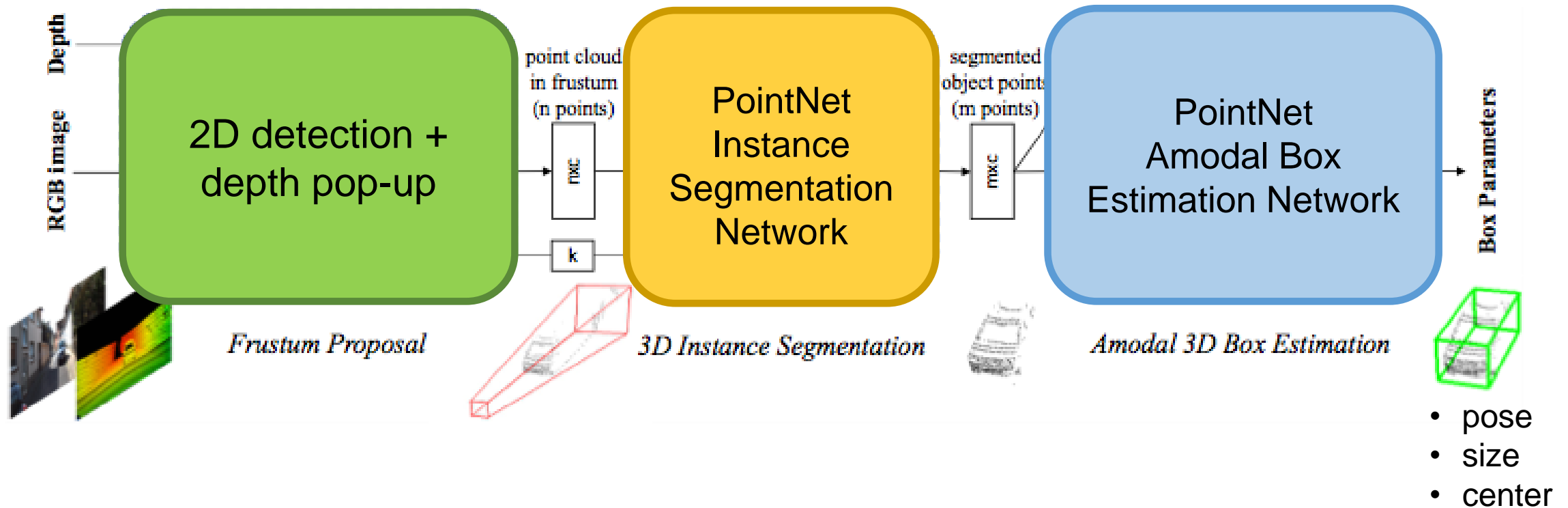
# Frustum-based 3D Object Detection: Challenges



- Occlusion and clutter is common in frustum point clouds
- Large range of point depths

# Frustum PointNets

Use **PointNets** for **data-driven** object detection in frustums.





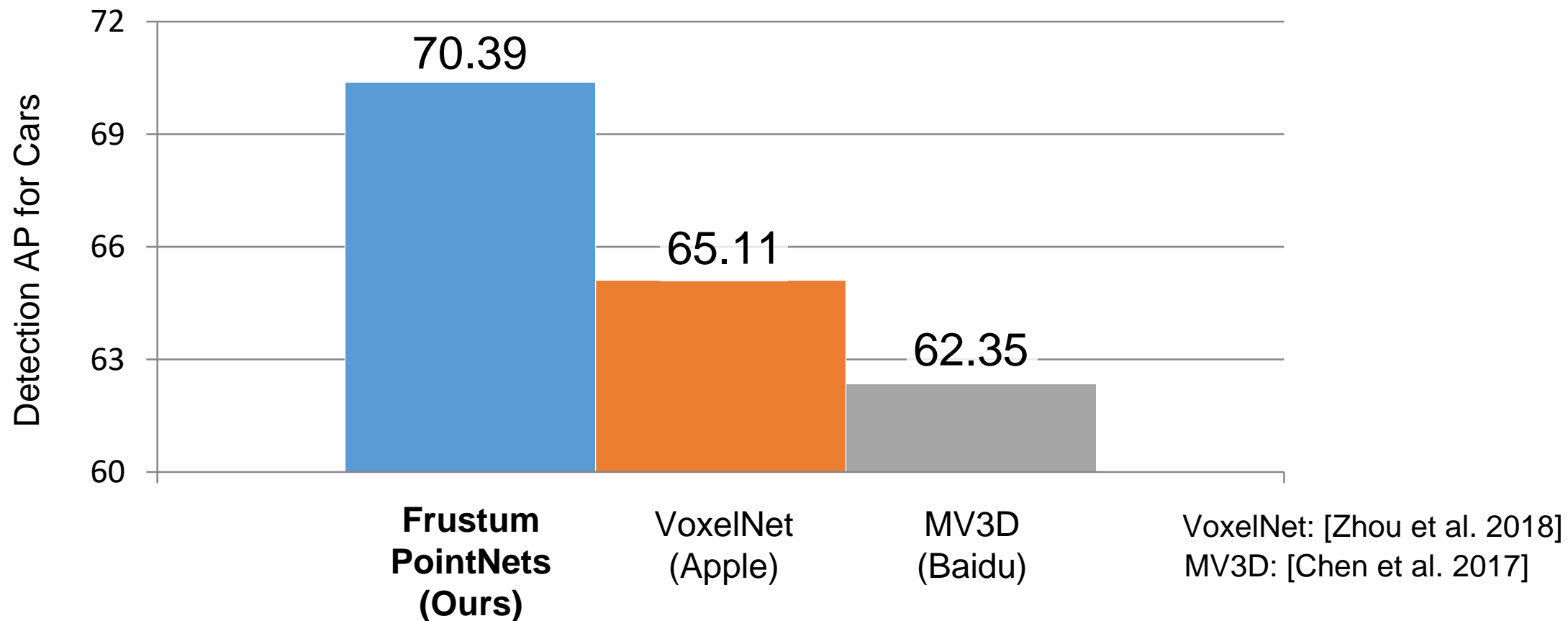
# Frustum PointNets: Key to Success

## *Respect and exploit 3D*

- **Use each modality (image, points) for what it's best at** — using 3D representation and 3D deep learning for the 3D problem.
- **Canonicalize the problem** — exploiting geometric transformations in point clouds.

# KITTI Results: Quantitative

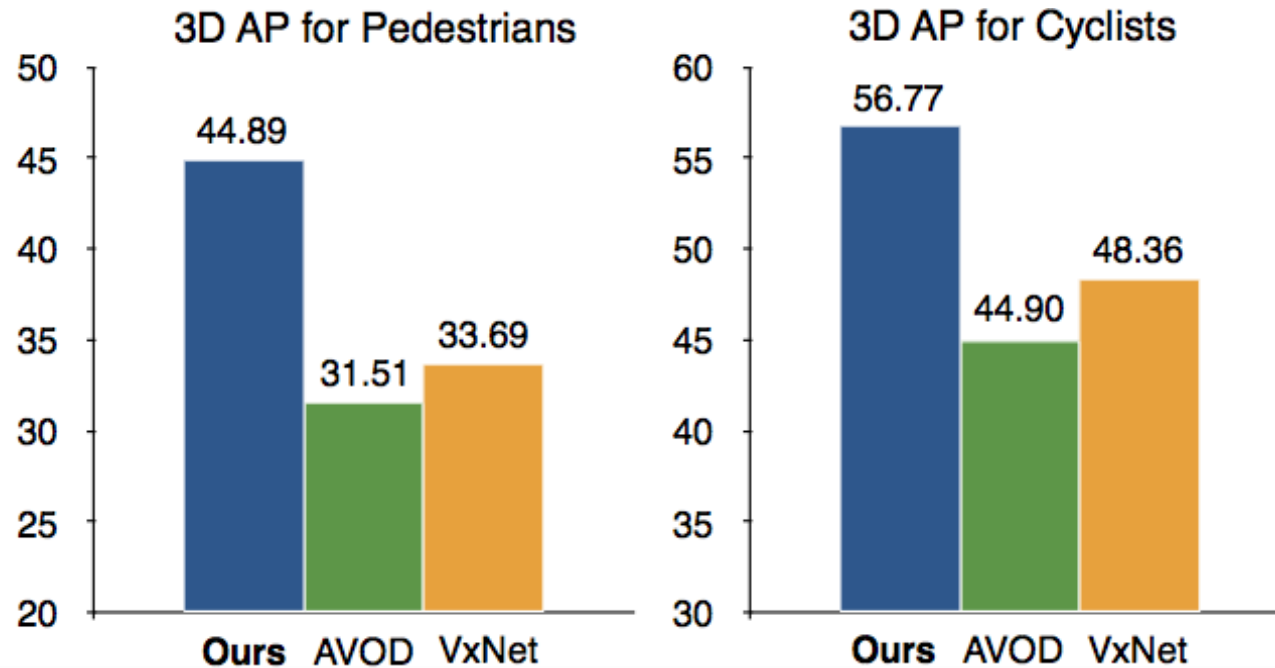
*Leading performance on KITTI benchmark*



# KITTI Results: Quantitative

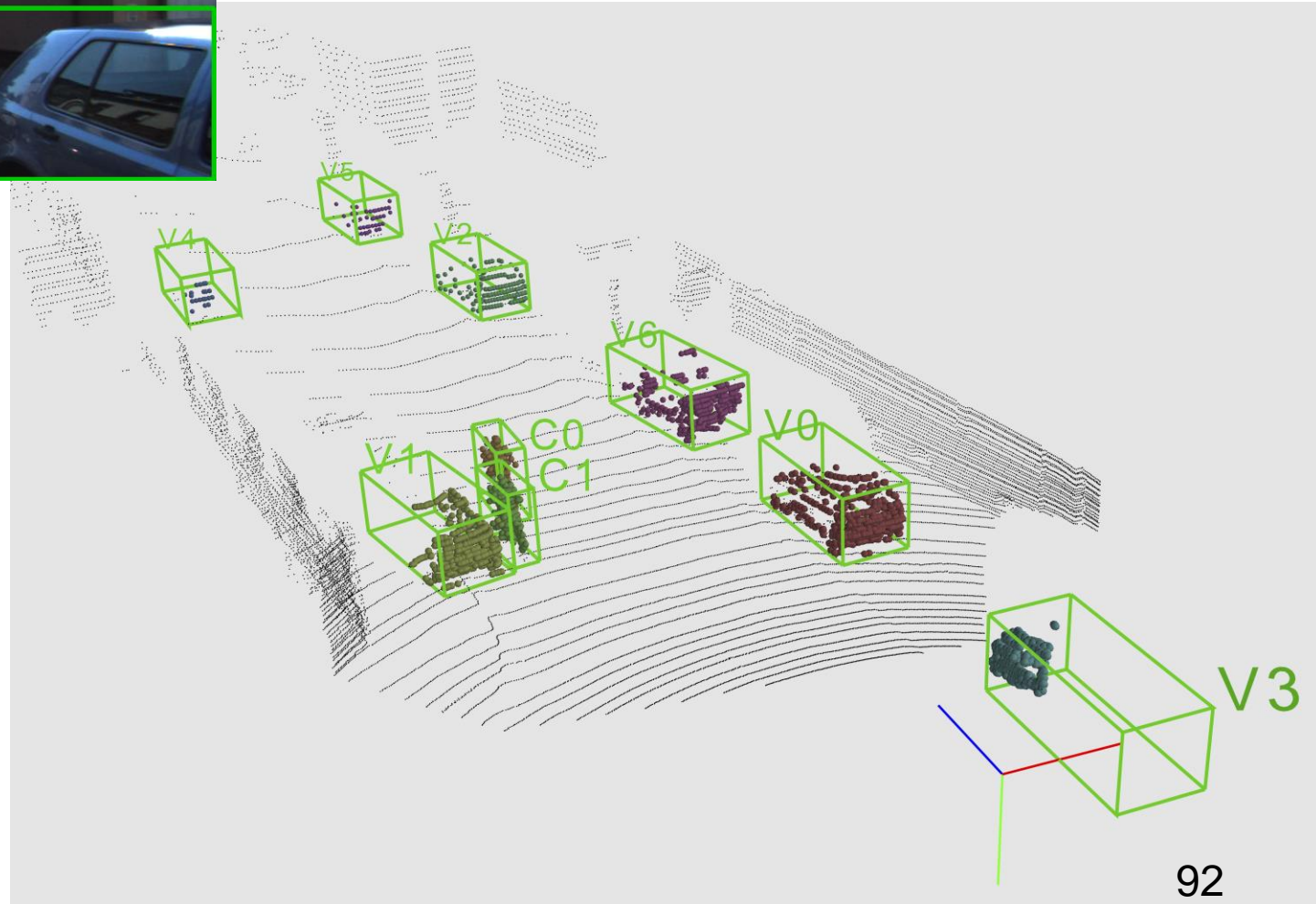
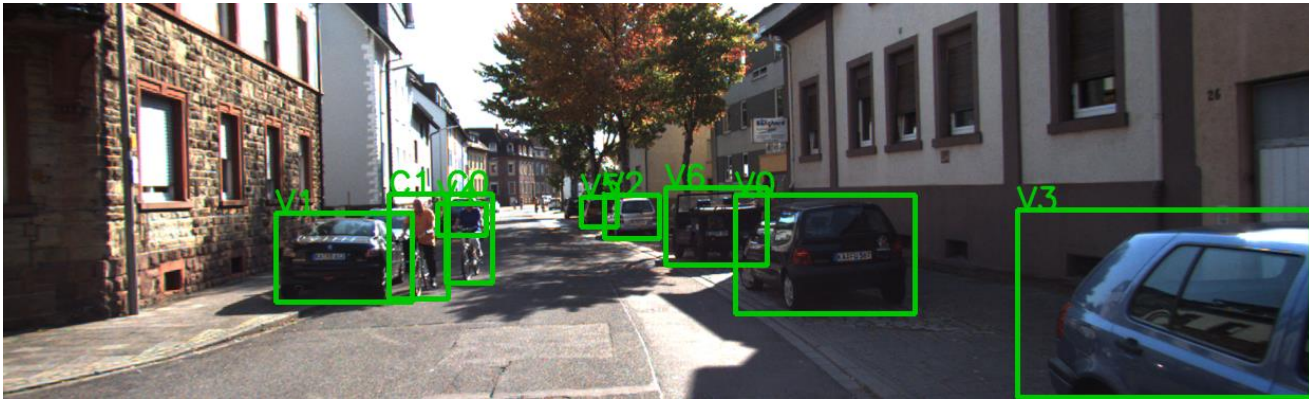
## *Leading performance on KITTI benchmark*

Especially leading at smaller objects (pedestrians and cyclists)  
– hard to localize with 3D proposals only.



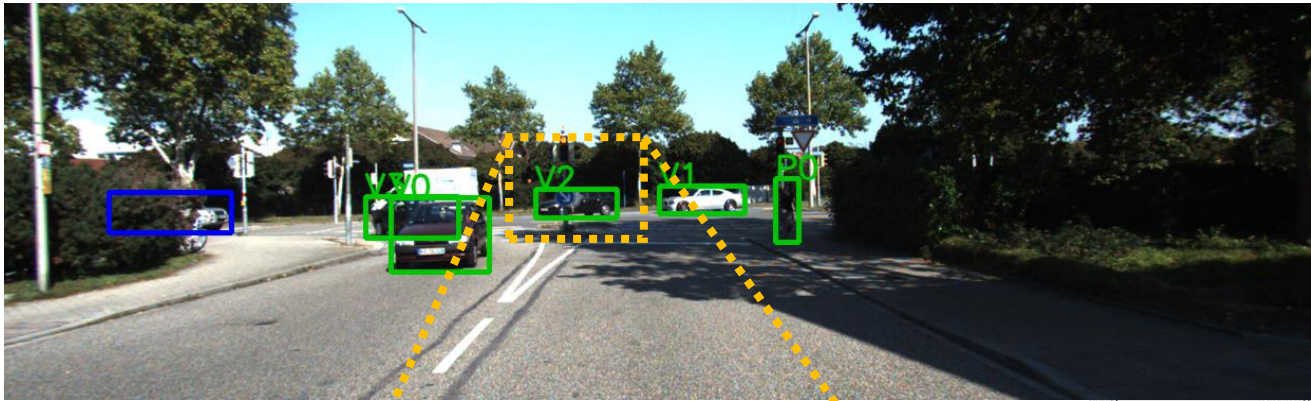
AVOD: [Ku et al. 2018]  
VxNet: [Zhou et al. 2017]

# KITTI Results: Qualitative

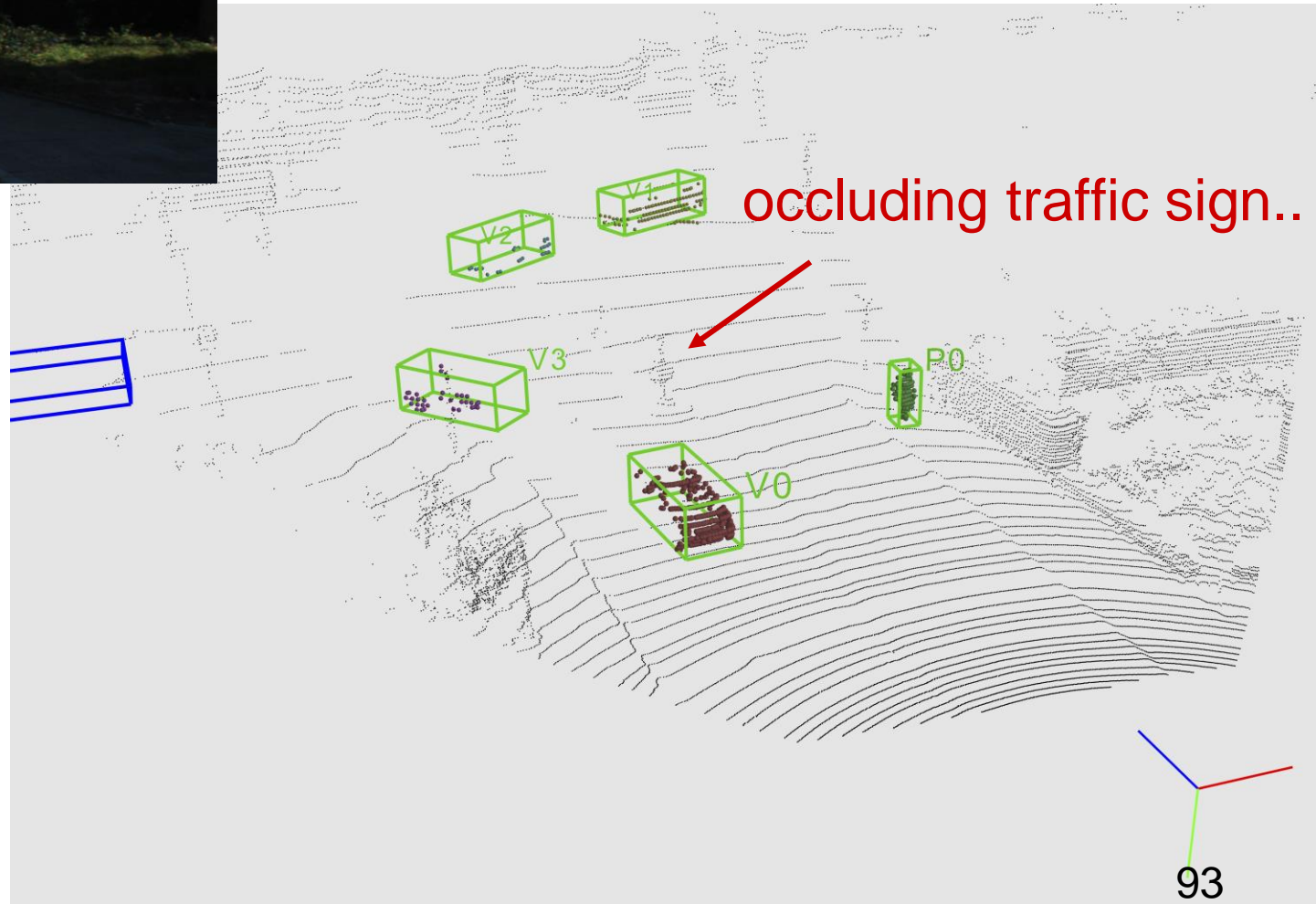


Remarkable box estimation accuracy even with a dozen of points or with very partial point clouds.

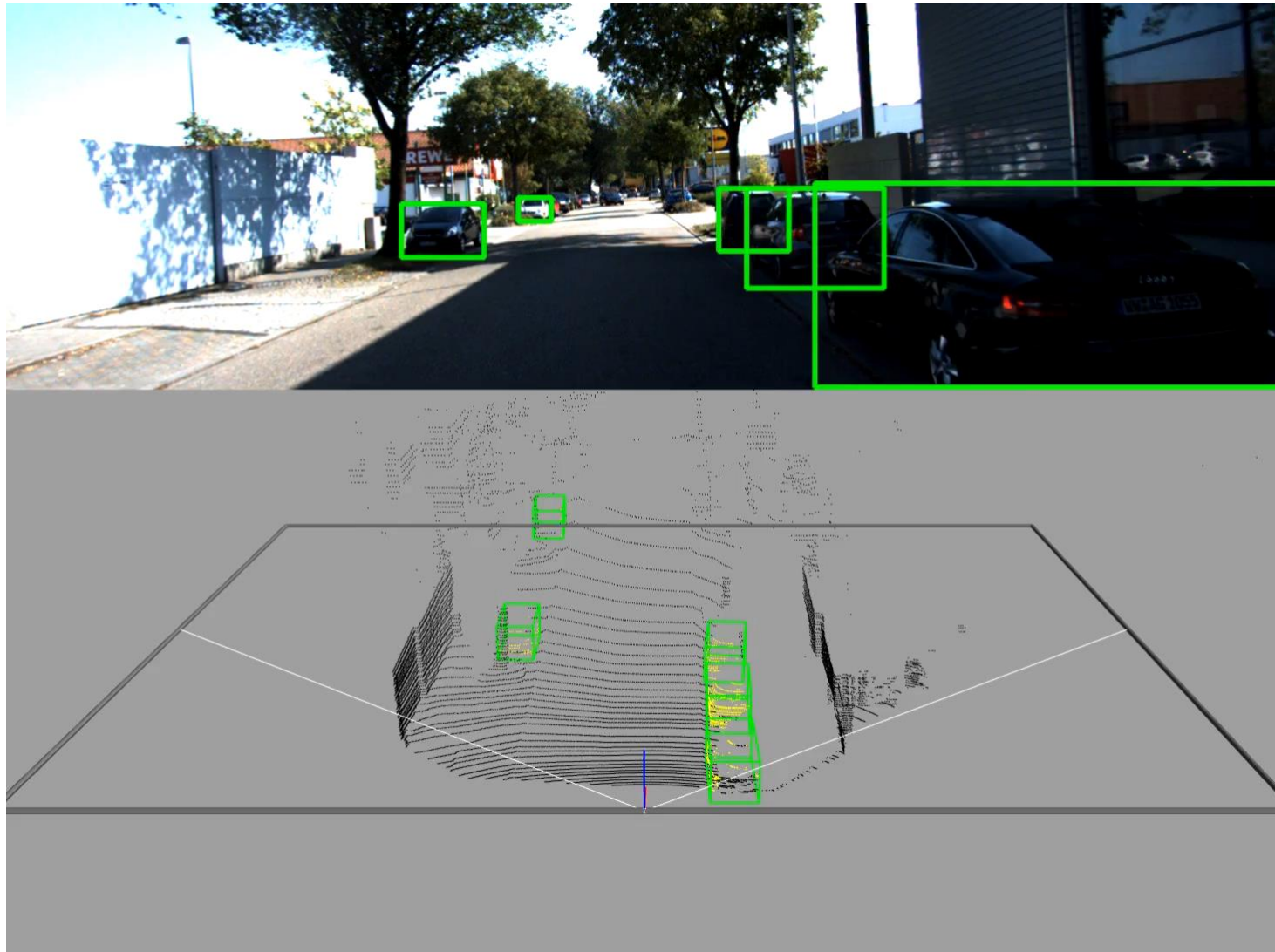
# KITTI Results: Qualitative



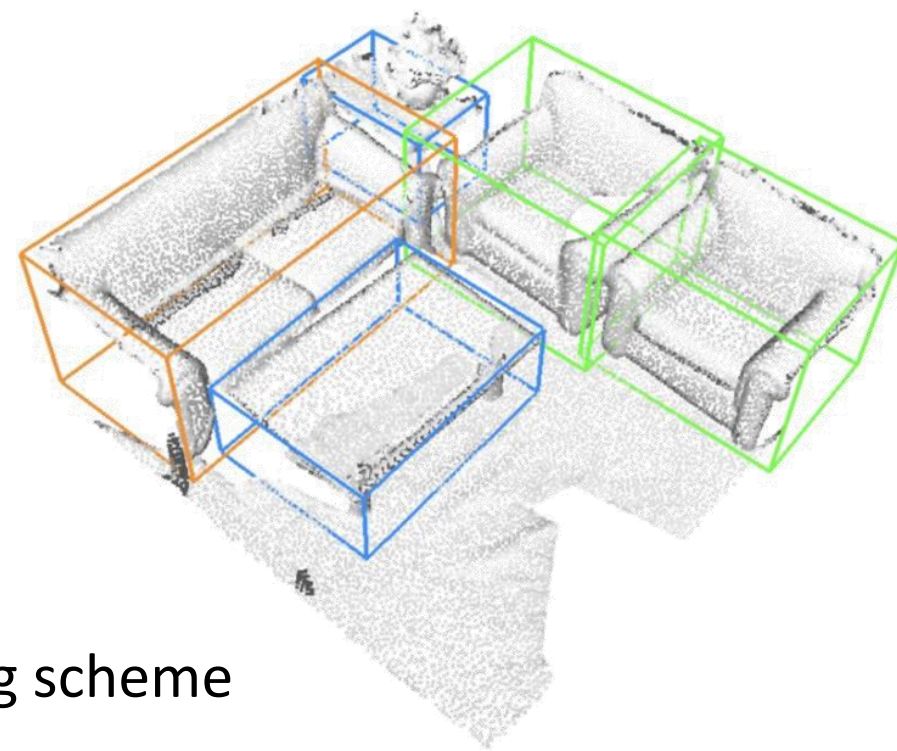
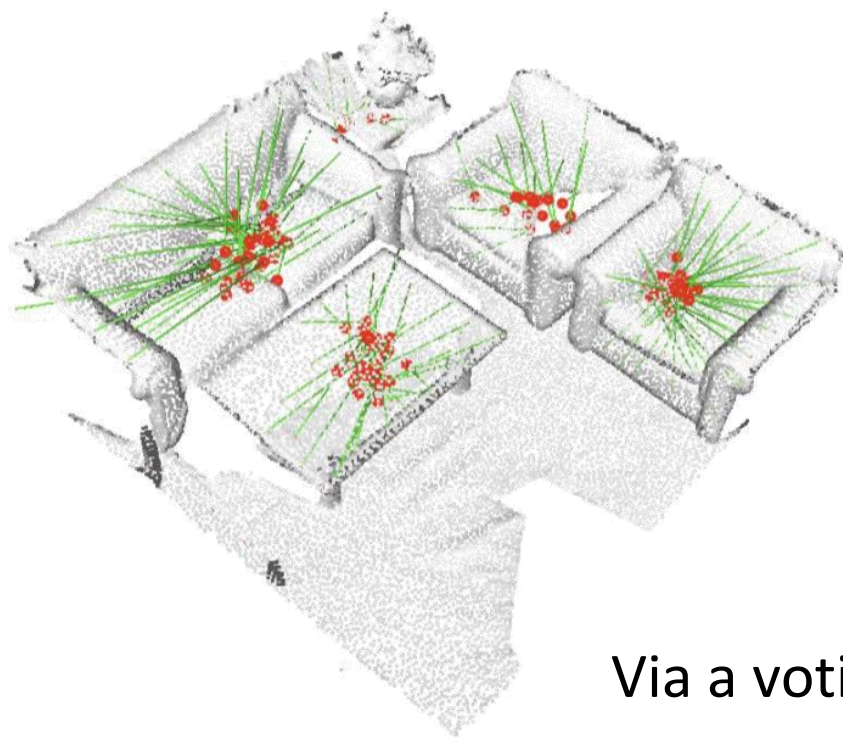
Correct segmentation in point clouds with heavy occlusion.



# KITTI Results: Example

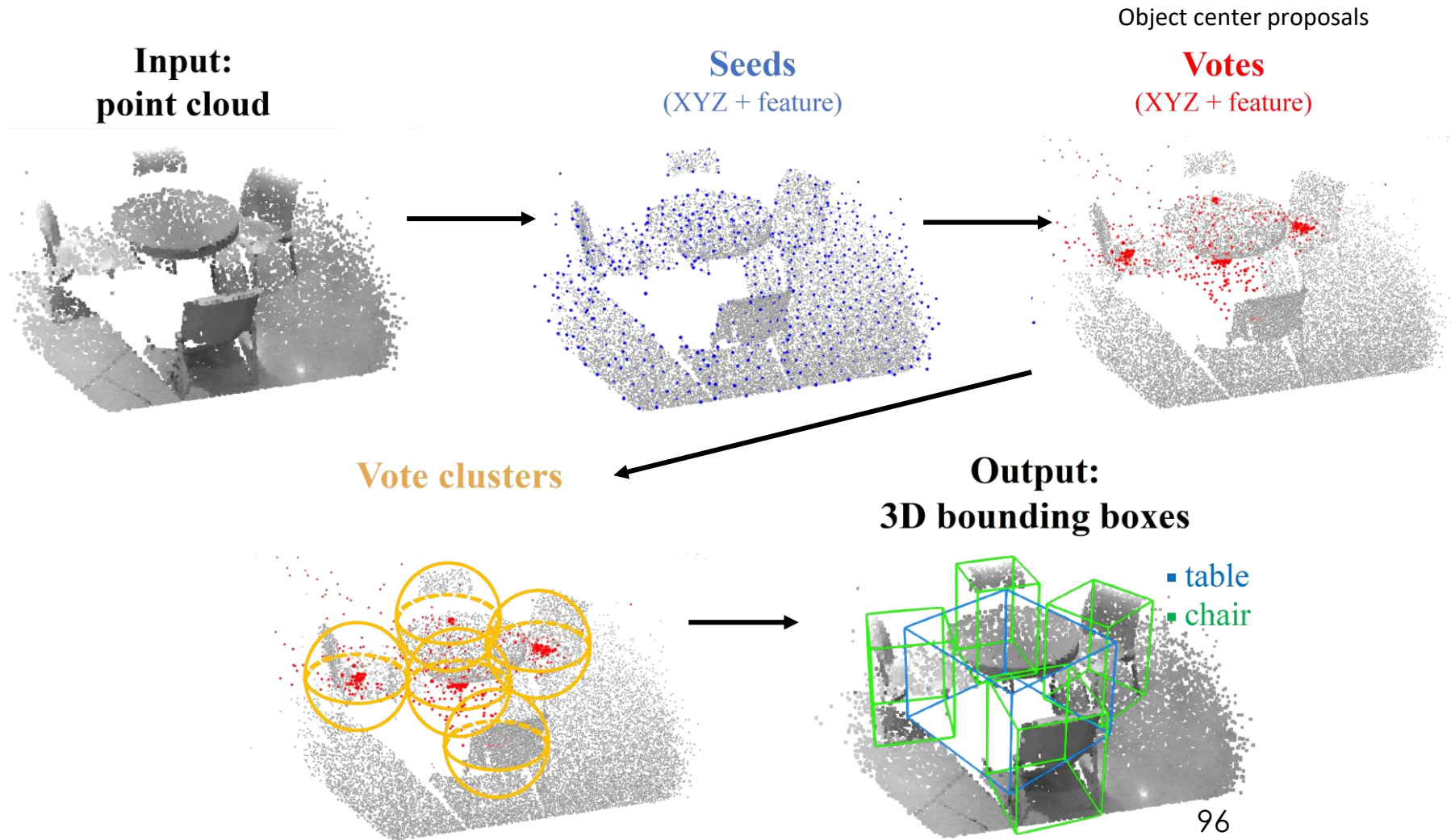


# Point Cloud Amodal Bounding Box Detection (Indoor)



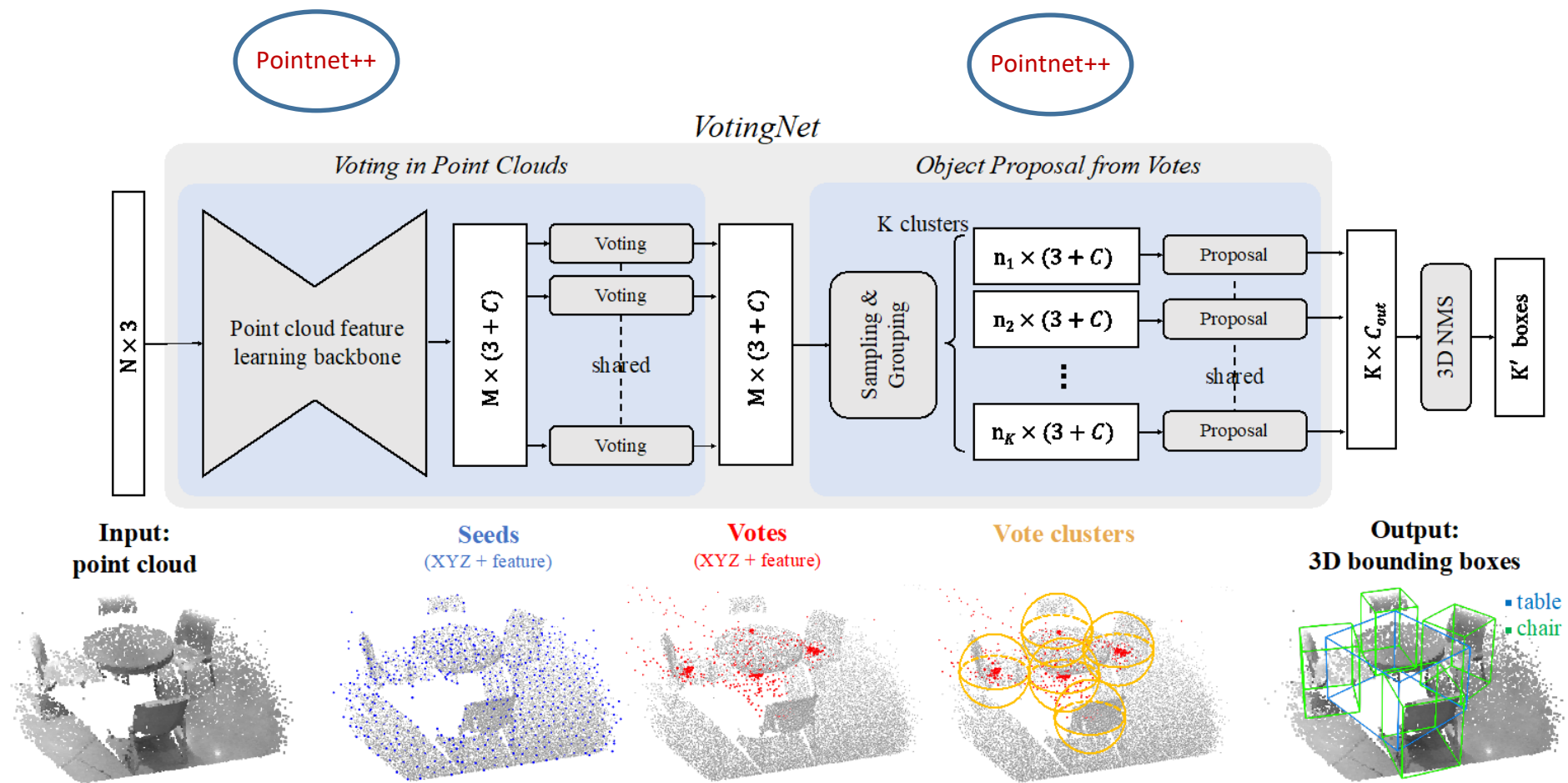
Via a voting scheme

# Deep Hough Voting





# Deep Hough Voting

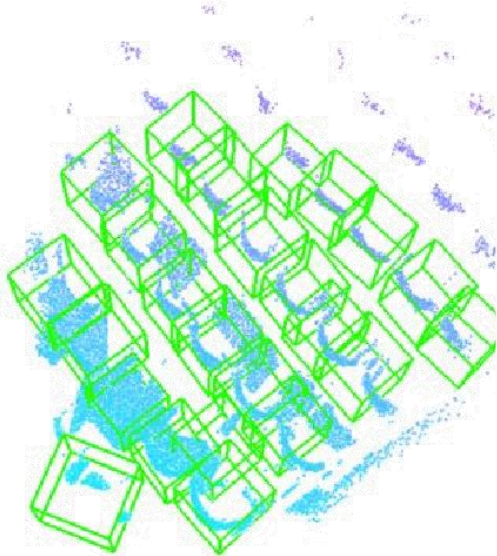


# Results on SUN RGB-D

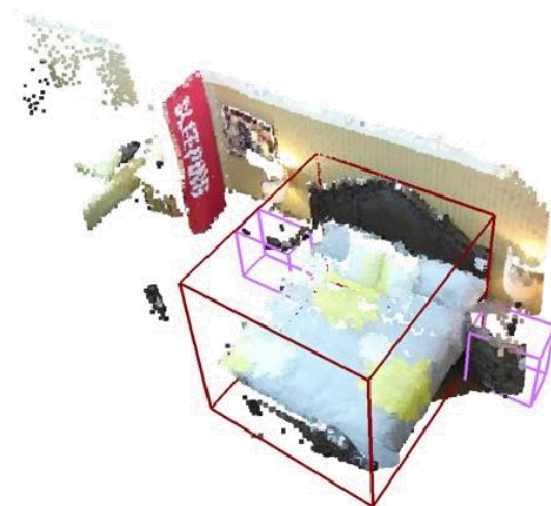
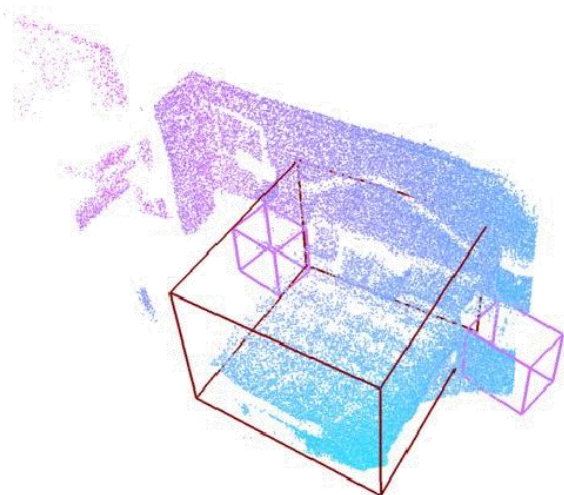
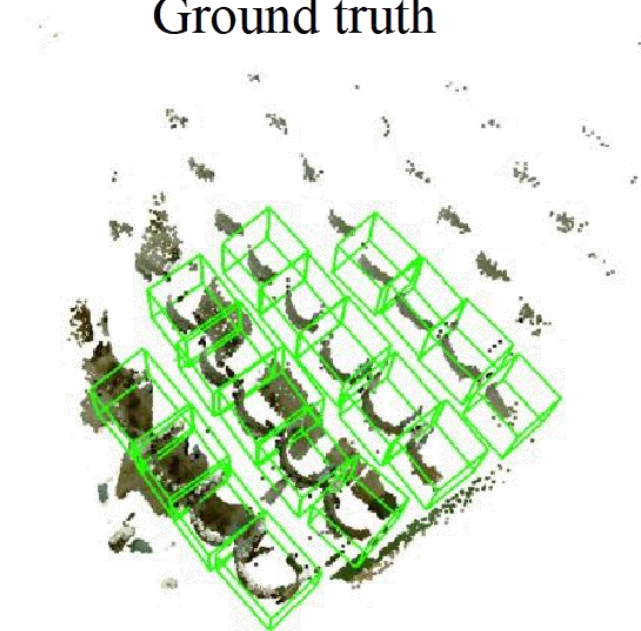
Image of the scene



VotingNet prediction

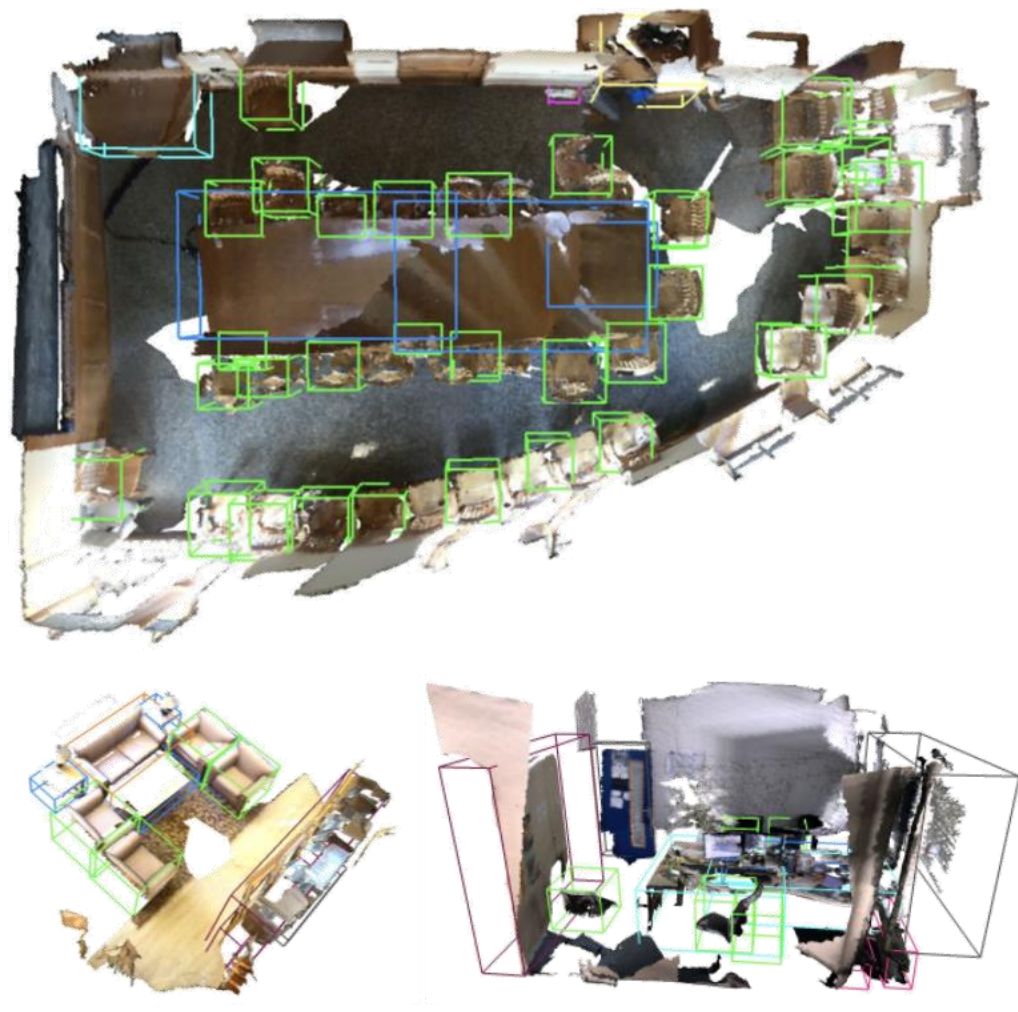


Ground truth

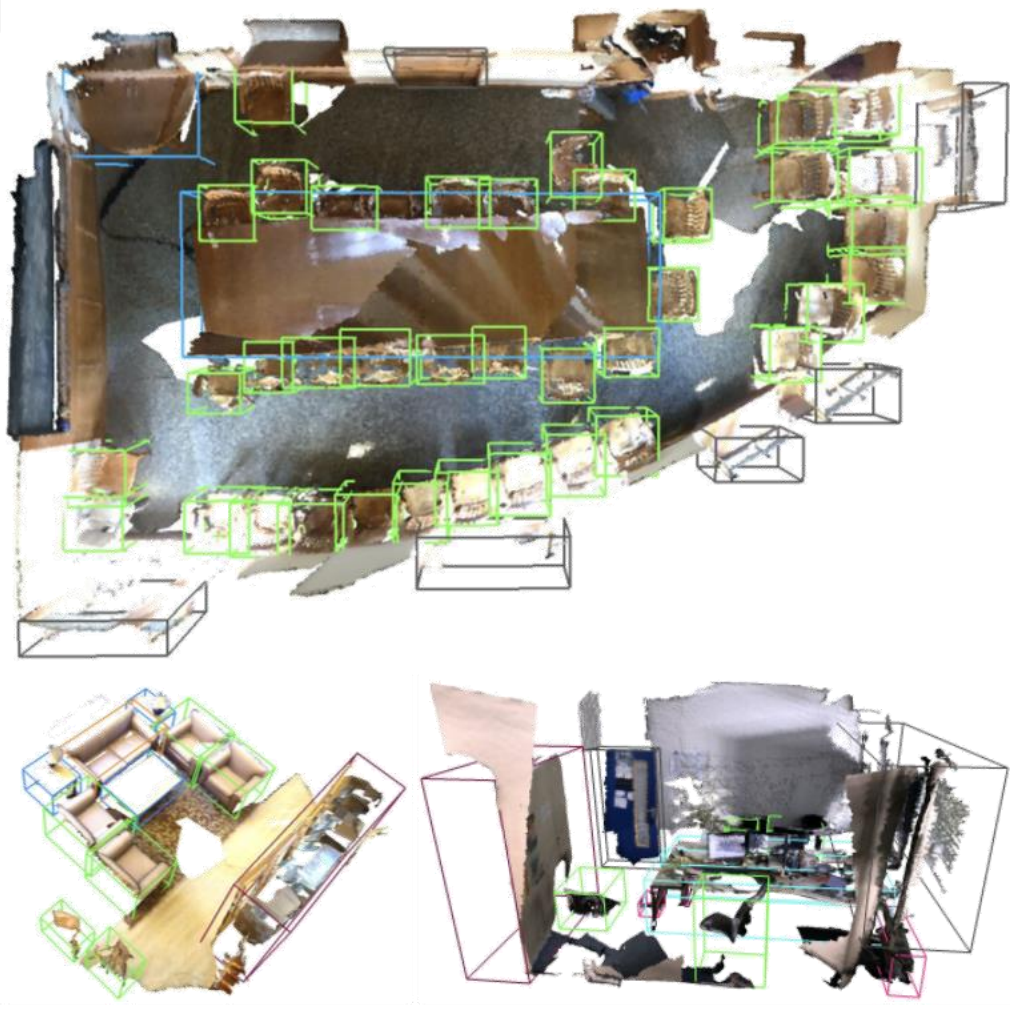


# Results on ScanNet

VotingNet prediction



Ground truth



# Quantitative Results

## SUN RGB-D

|                  | Input     | bathhtub    | bed         | bookshelf   | chair       | desk        | dresser     | nightstand  | sofa        | table       | toilet      | mAP         |
|------------------|-----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| DSS [37]         | Geo + RGB | 44.2        | 78.8        | 11.9        | 61.2        | 20.5        | 6.4         | 15.4        | 53.5        | 50.3        | 78.9        | 42.1        |
| COG [33]         | Geo + RGB | 58.3        | 63.7        | 31.8        | 62.2        | <b>45.2</b> | 15.5        | 27.4        | 51.0        | <b>51.3</b> | 70.1        | 47.6        |
| 2D-driven [17]   | Geo + RGB | 43.5        | 64.5        | 31.4        | 48.3        | 27.9        | 25.9        | 41.9        | 50.4        | 37.0        | 80.4        | 45.1        |
| F-PointNet [30]  | Geo + RGB | 43.3        | 81.1        | <b>33.3</b> | 64.2        | 24.7        | <b>32.0</b> | 58.1        | 61.1        | 51.1        | <b>90.9</b> | 54.0        |
| VotingNet (ours) | Geo only  | <b>74.4</b> | <b>83.0</b> | 28.8        | <b>75.3</b> | 22.0        | 29.8        | <b>62.2</b> | <b>64.0</b> | 47.3        | 90.1        | <b>57.7</b> |

## ScanNetV2

|                  | Input         | mAP@0.25     | mAP@0.5      |
|------------------|---------------|--------------|--------------|
| DSS [37]         | Geo + RGB     | 15.2         | 6.8          |
| MRCNN 2D-3D [10] | Geo + RGB     | 17.3         | 10.5         |
| F-PointNet [30]  | Geo + RGB     | 19.8         | 10.8         |
| GSPN [47]        | Geo + RGB     | 30.6         | 17.7         |
| 3D-SIS [11]      | Geo + 1 view  | 35.09        | 18.66        |
| 3D-SIS [11]      | Geo + 3 views | 36.64        | 19.04        |
| 3D-SIS [11]      | Geo + 5 views | 40.22        | 22.53        |
| 3D-SIS [11]      | Geo only      | 25.36        | 14.60        |
| VotingNet (ours) | Geo only      | <b>46.75</b> | <b>24.65</b> |

# 3D Scene Understanding with PointNets

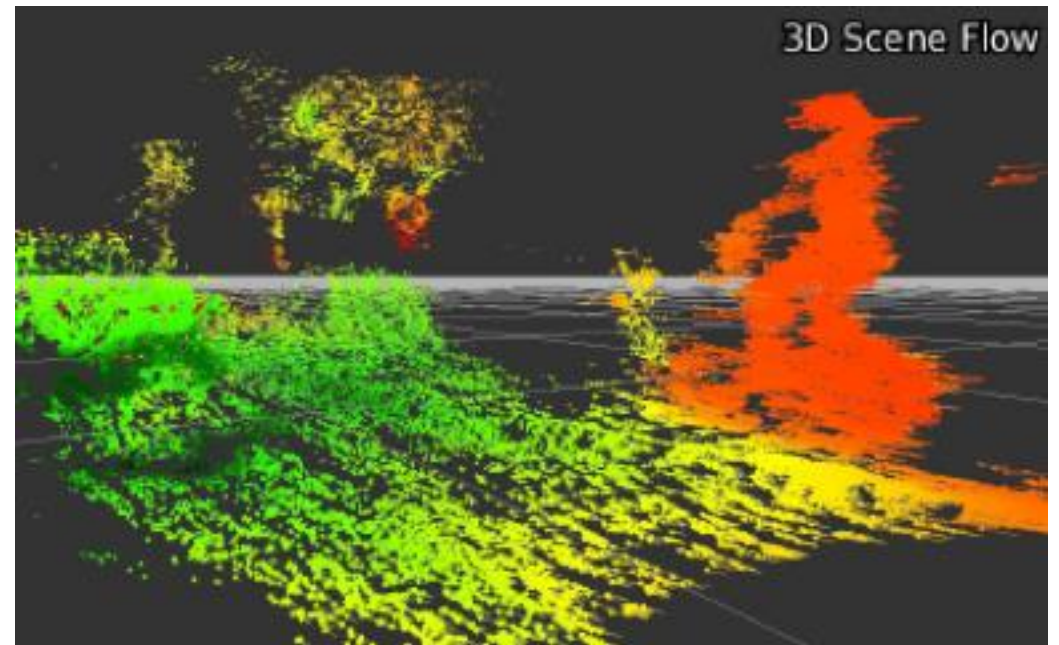
- PointNet and PointNet++ lead to new **3D centric approaches** to scene understanding

3D Object Detection



source: SUN RGB-D by Song et al.

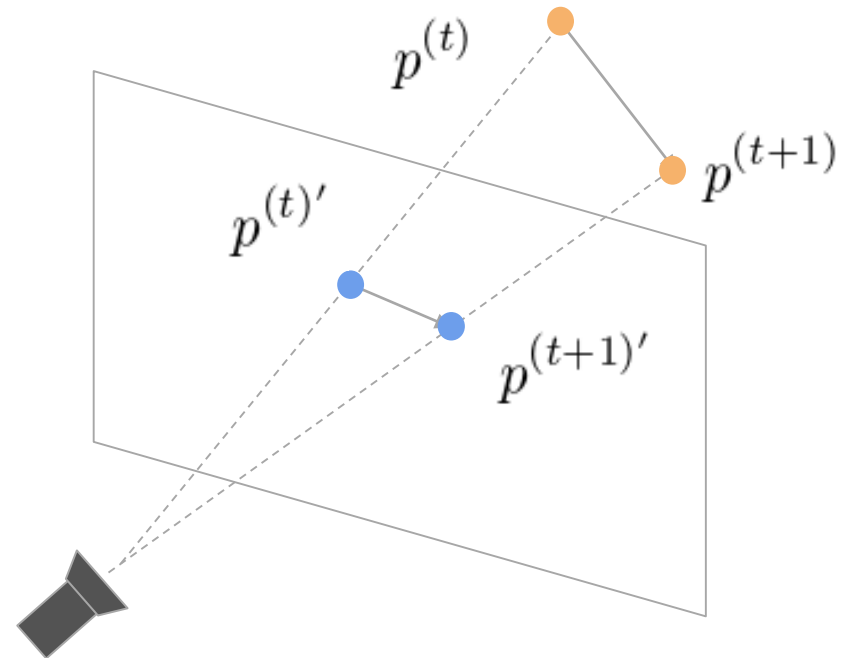
3D Scene Flow



source: Wedel et al.

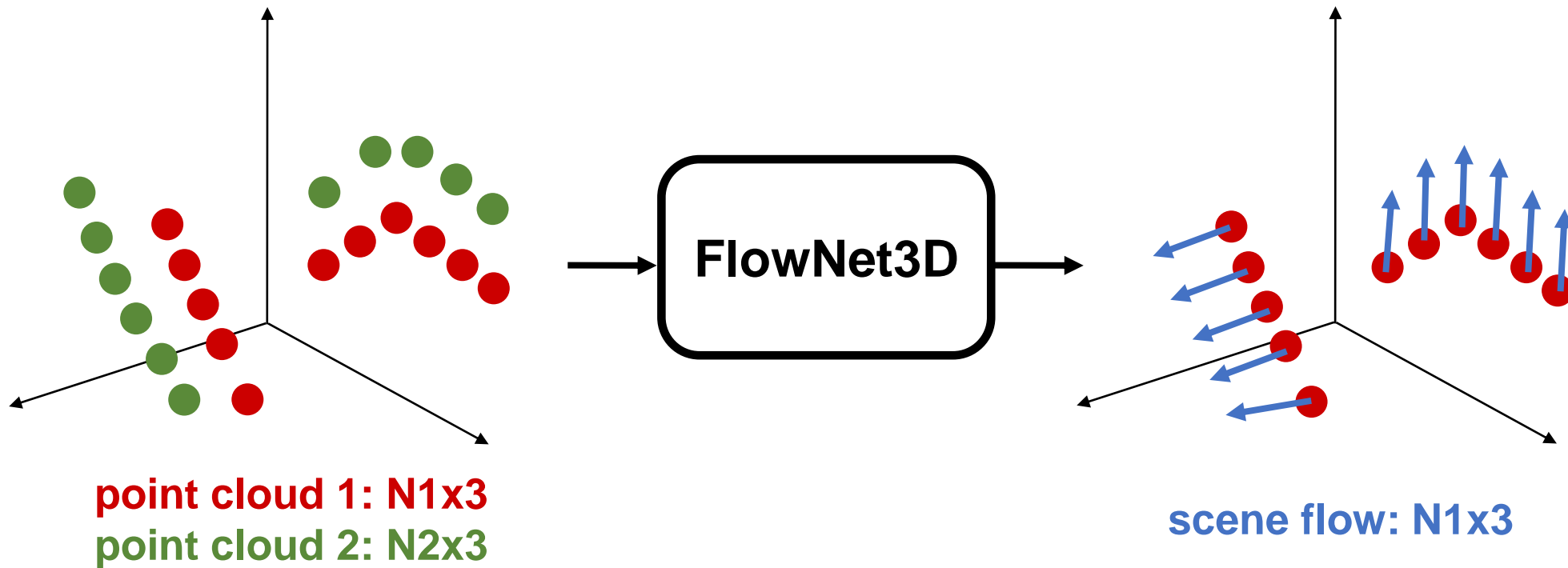
# Scene Flow [Vedula et al. 1999]

- Scene flow: 3D motion field of points
- Optical flow is its projection to 2D image plane.
- Low-level understanding of a dynamic environment



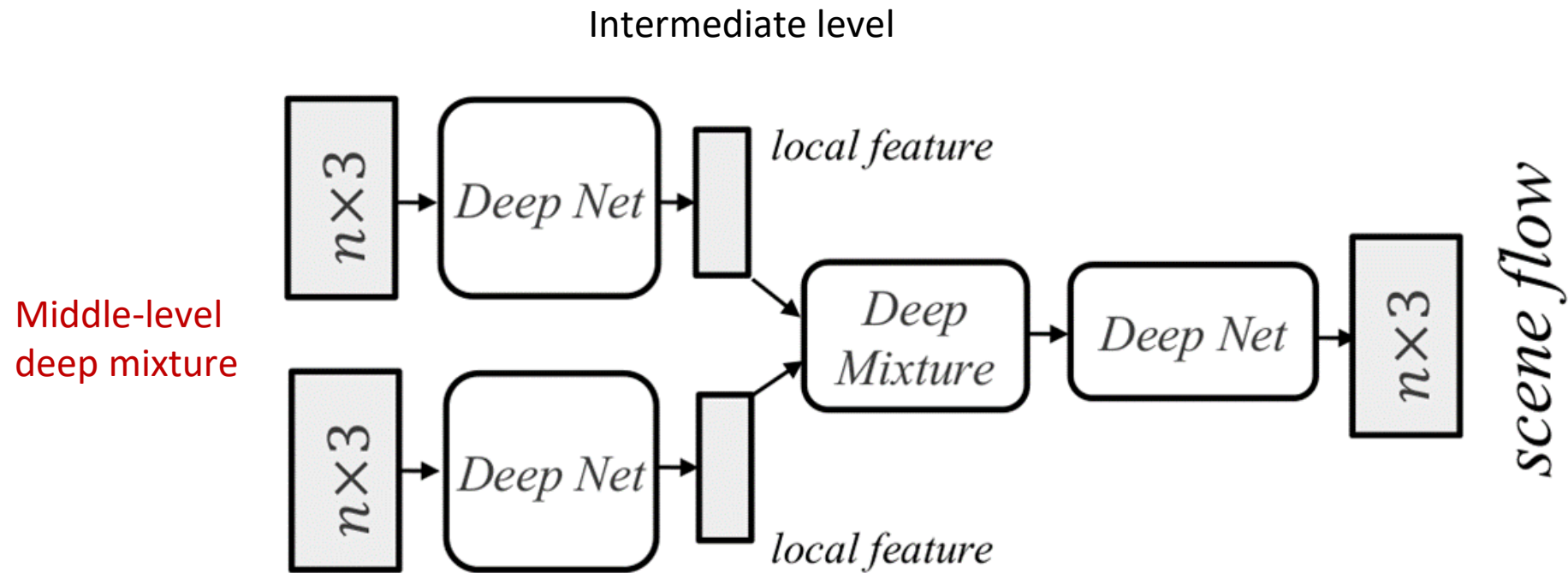
# Our Approach: FlowNet3D

- Directly learning scene flow in 3D point clouds, with 3D deep learning architectures.



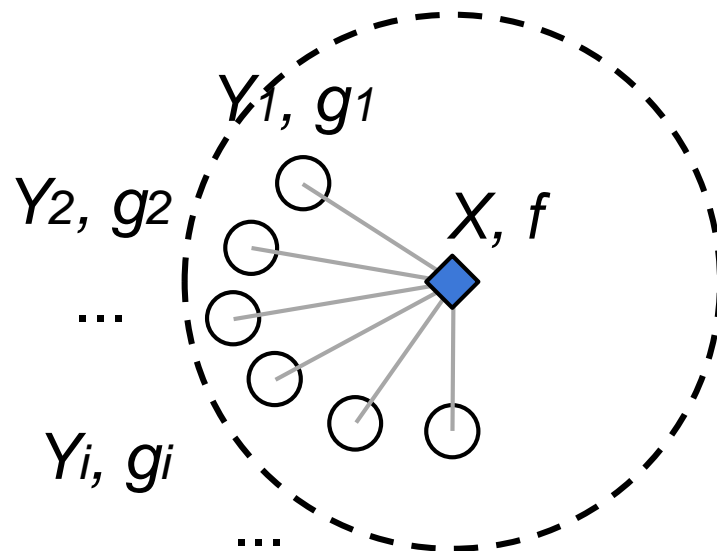
# Deep Net Architecture

- How to learn point cloud features?
- Where in the network architecture to mix point features from consecutive frames?
- How to mix them?





# Point Attributes

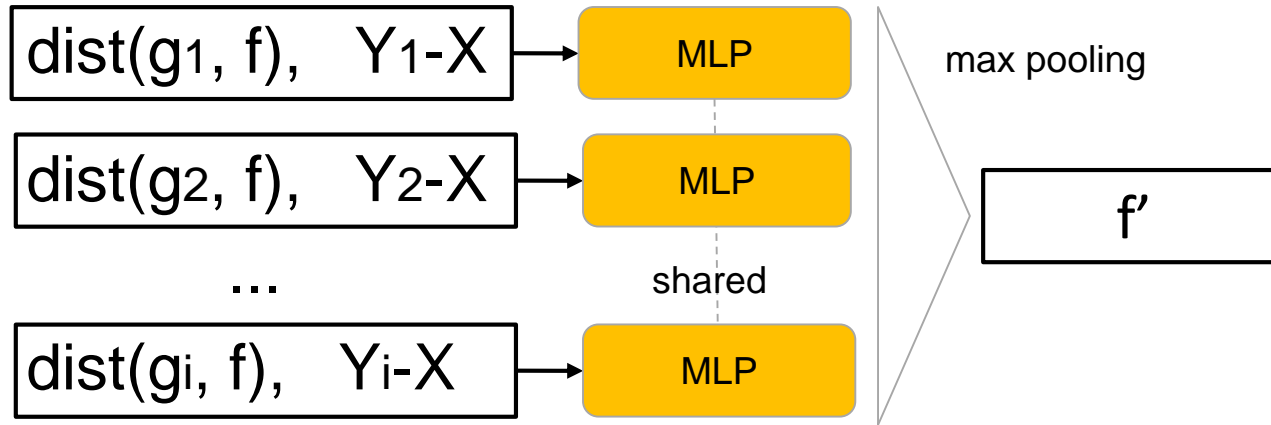


$\text{dist}(g_1, f), Y_1-X$   
 $\text{dist}(g_2, f), Y_2-X$   
 $\vdots$   
 $\text{dist}(g_i, f), Y_i-X$   
 $\vdots$

*Naive approach: concatenation*

|                              |                              |     |
|------------------------------|------------------------------|-----|
| $\text{dist}(g_1, f), Y_1-X$ | $\text{dist}(g_2, f), Y_2-X$ | ... |
|------------------------------|------------------------------|-----|

# A More Structured Approach



$\text{dist}(g_i, f)$

“Distance” functions:

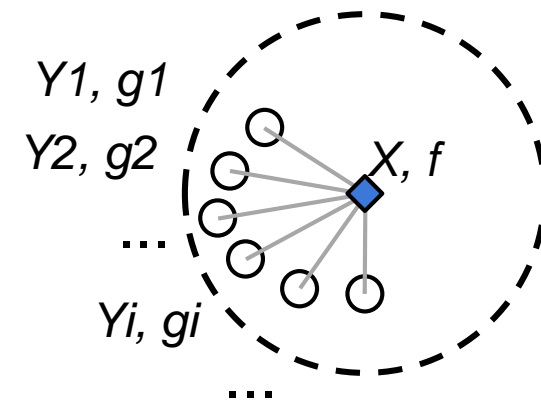
Euclidean distance (scalar)

Cosine distance (scalar)

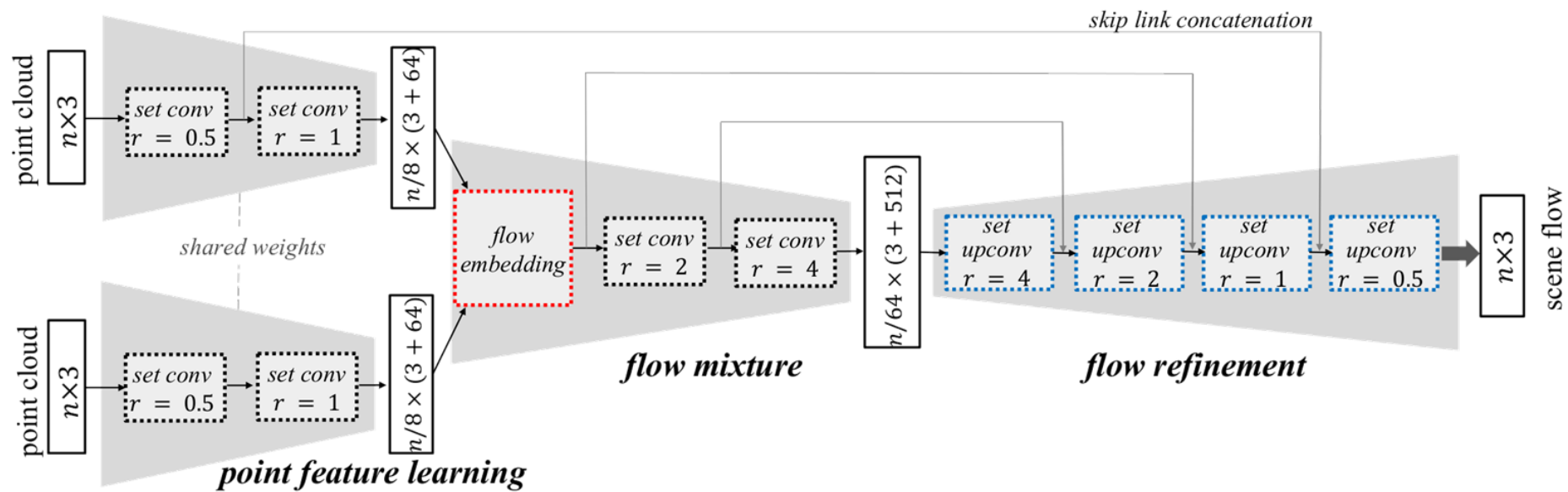
Element-wise product (vector)

Simple concatenation — let the network learn the distance function (vector)

...



# FlowNet3D



Composed of many many mini-pointnet++ modules ...

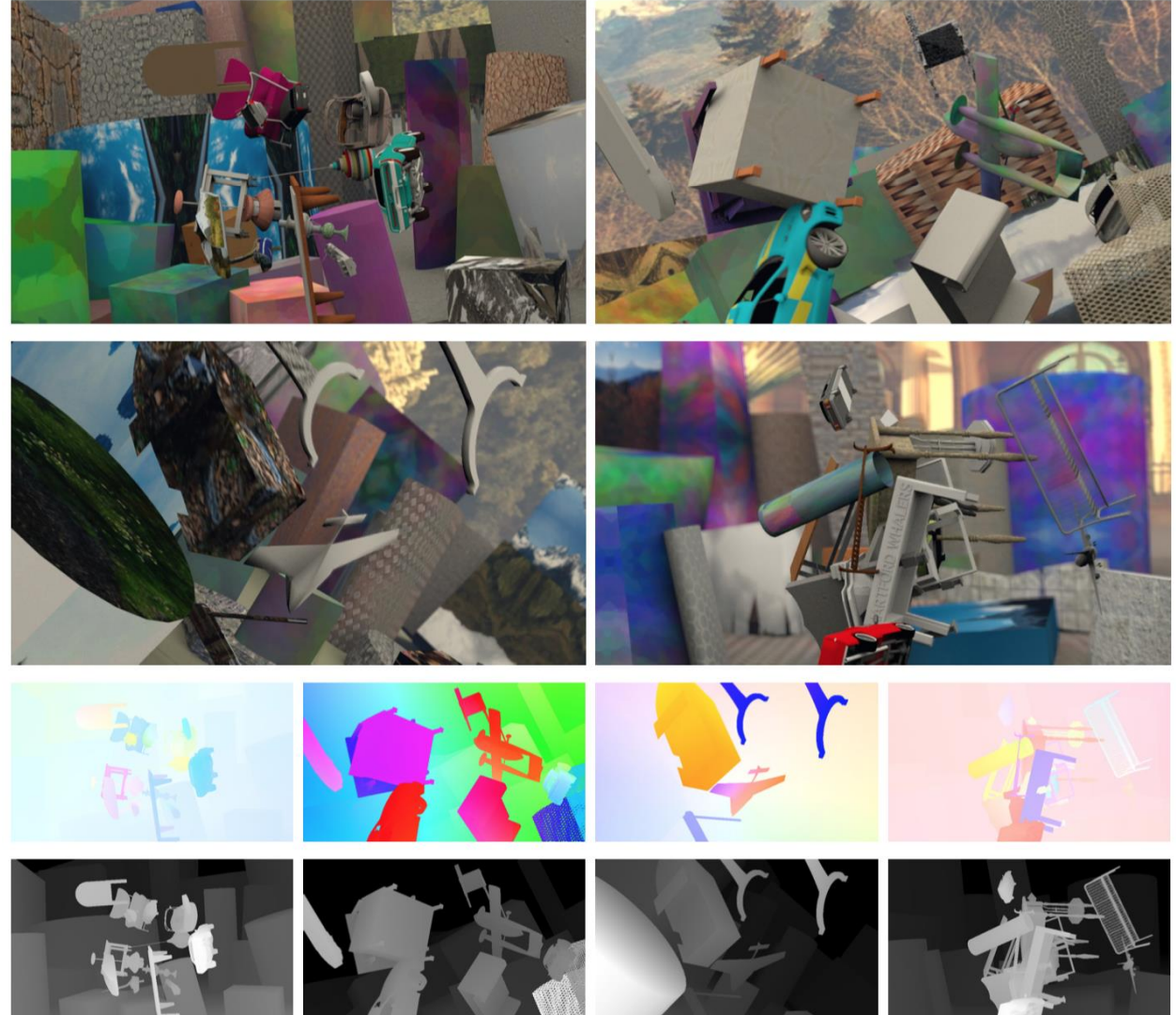
Pointnet++

# Training on Synthetic Data

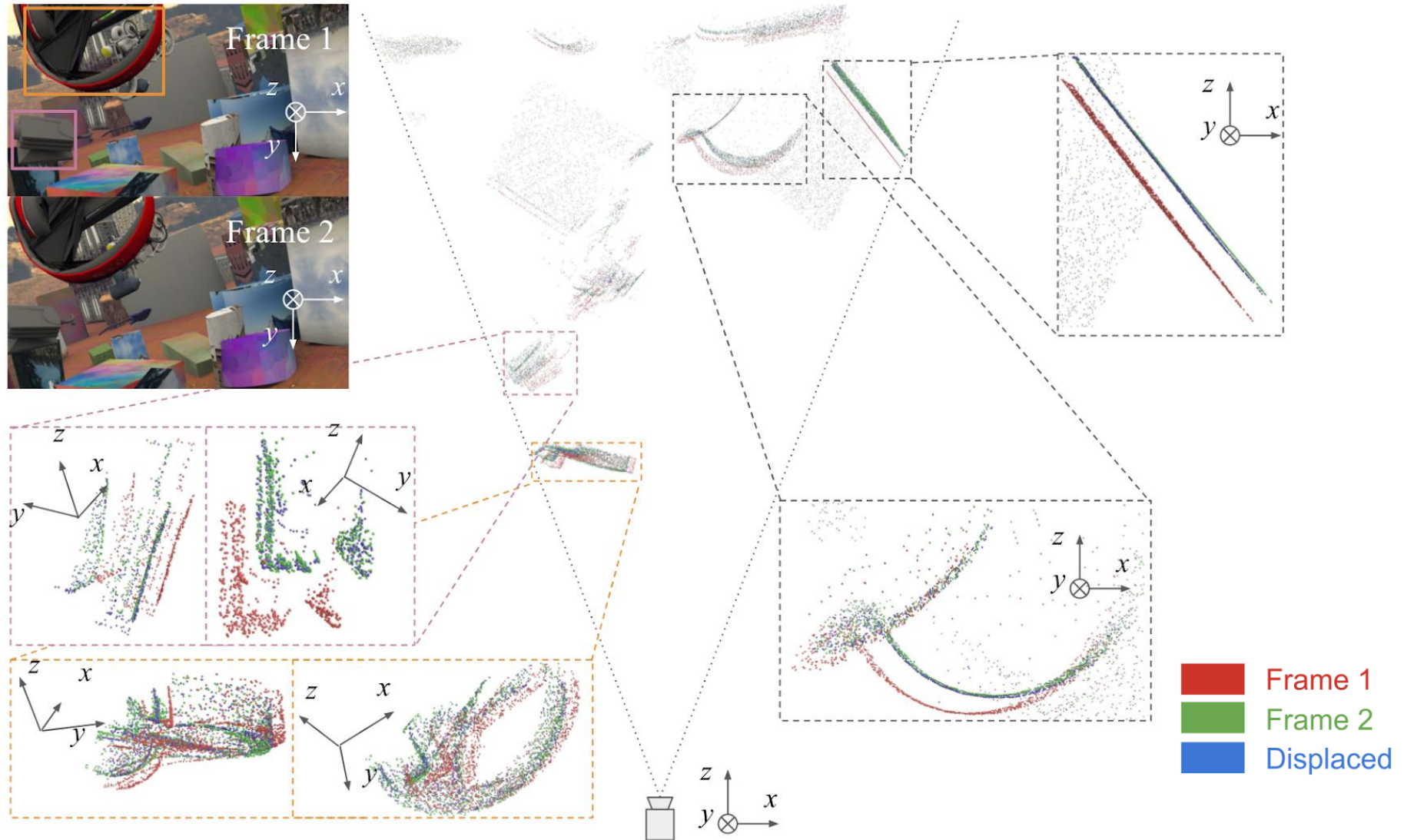
FlyingThings3D [Mayer et al. 2016]  
dataset from MPI

Random ShapeNet objects

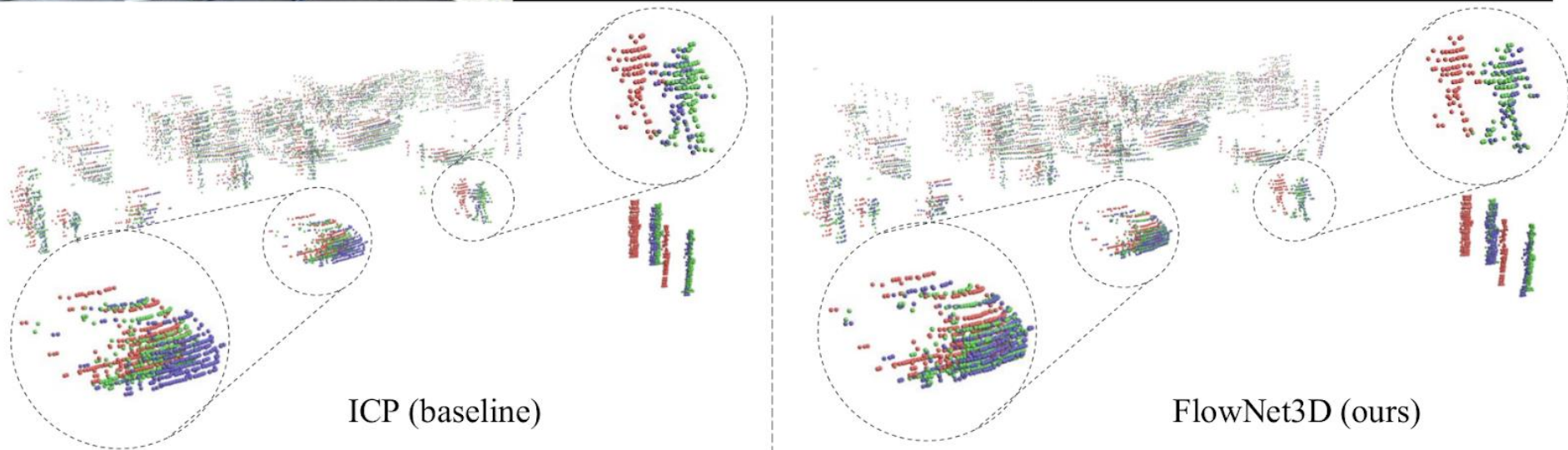
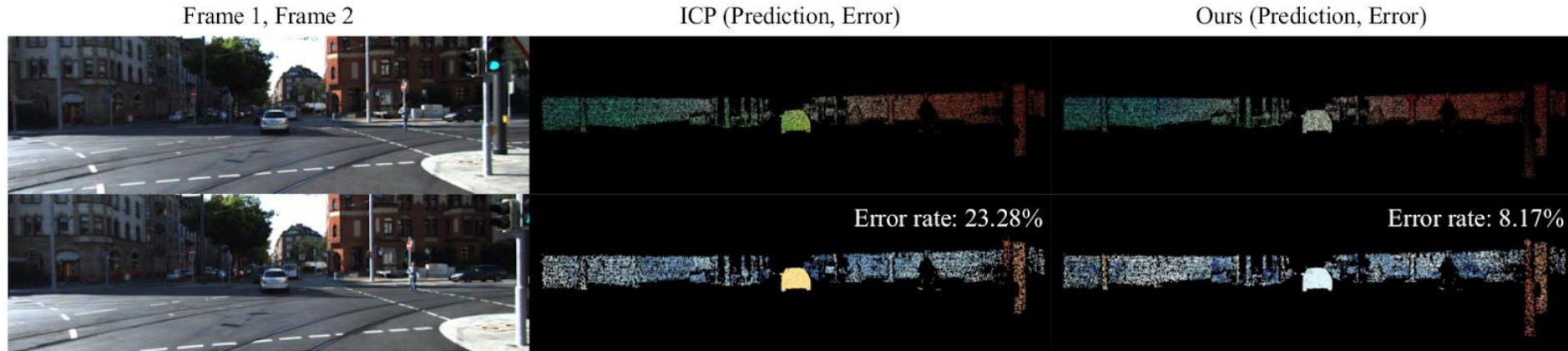
Very challenging dataset with  
strong occlusions and large  
motions.



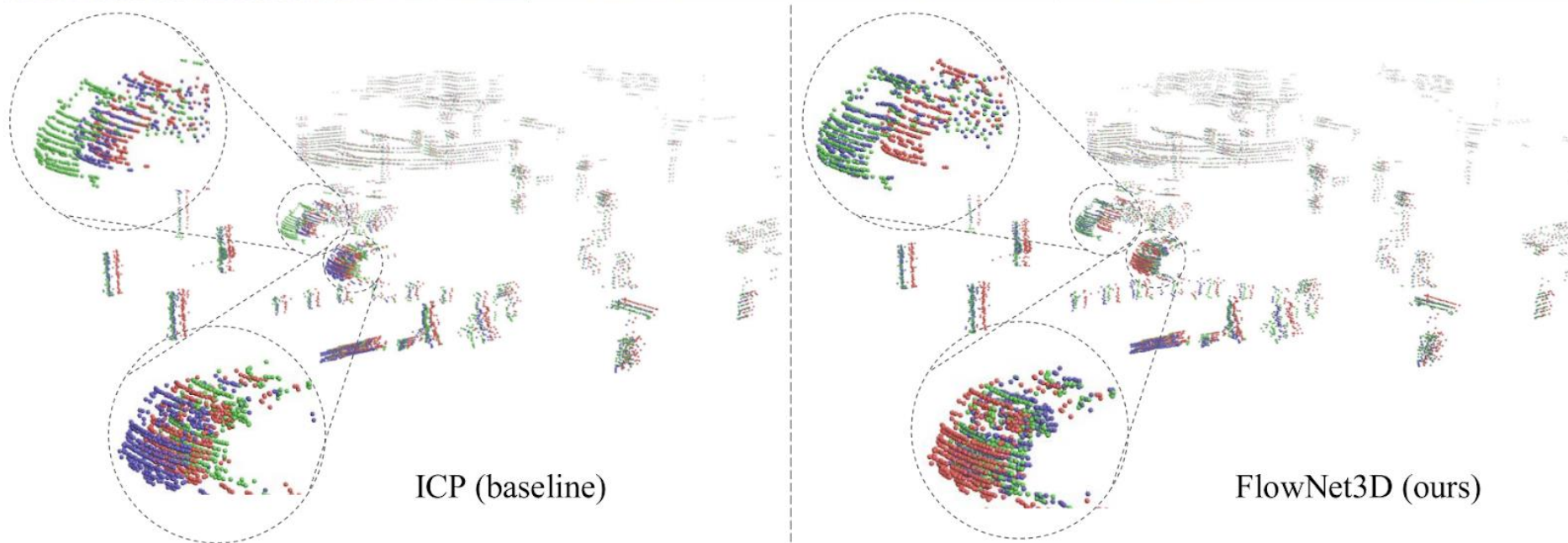
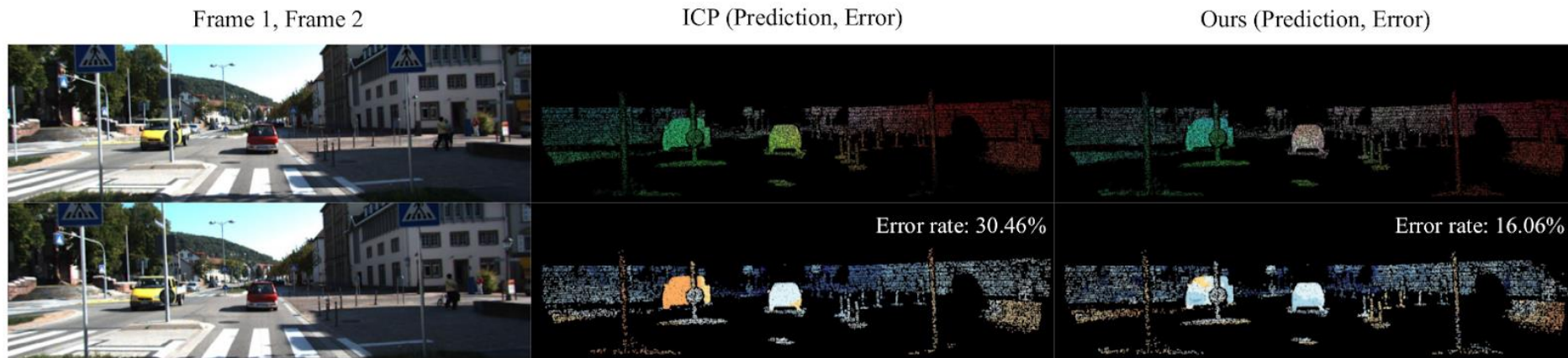
# FlyingThings3D Results



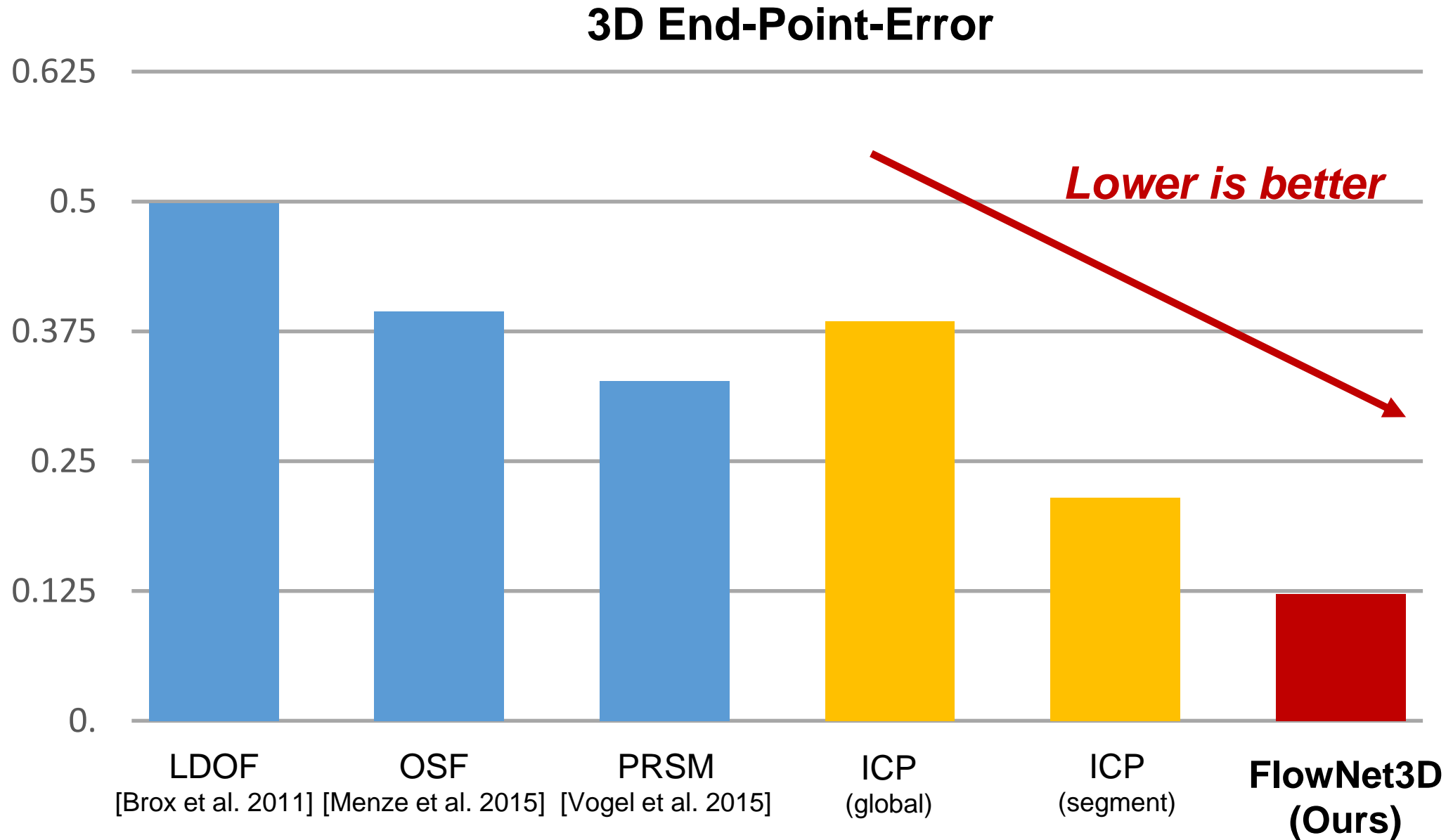
# KITTI Results



# KITTI Results



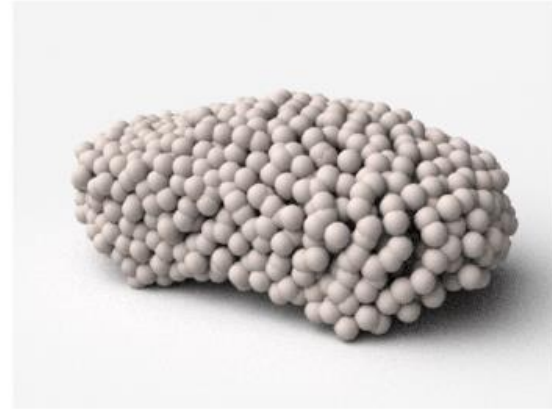
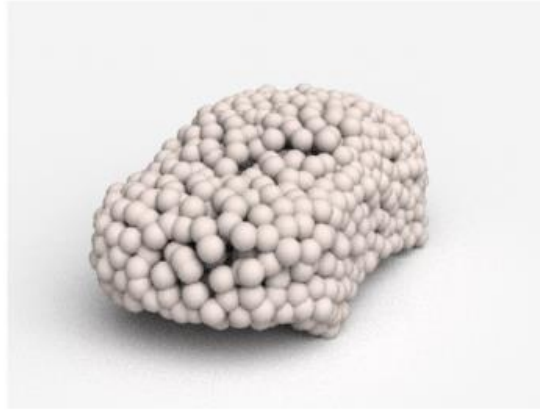
# Generalizing to KITTI: Quantitative





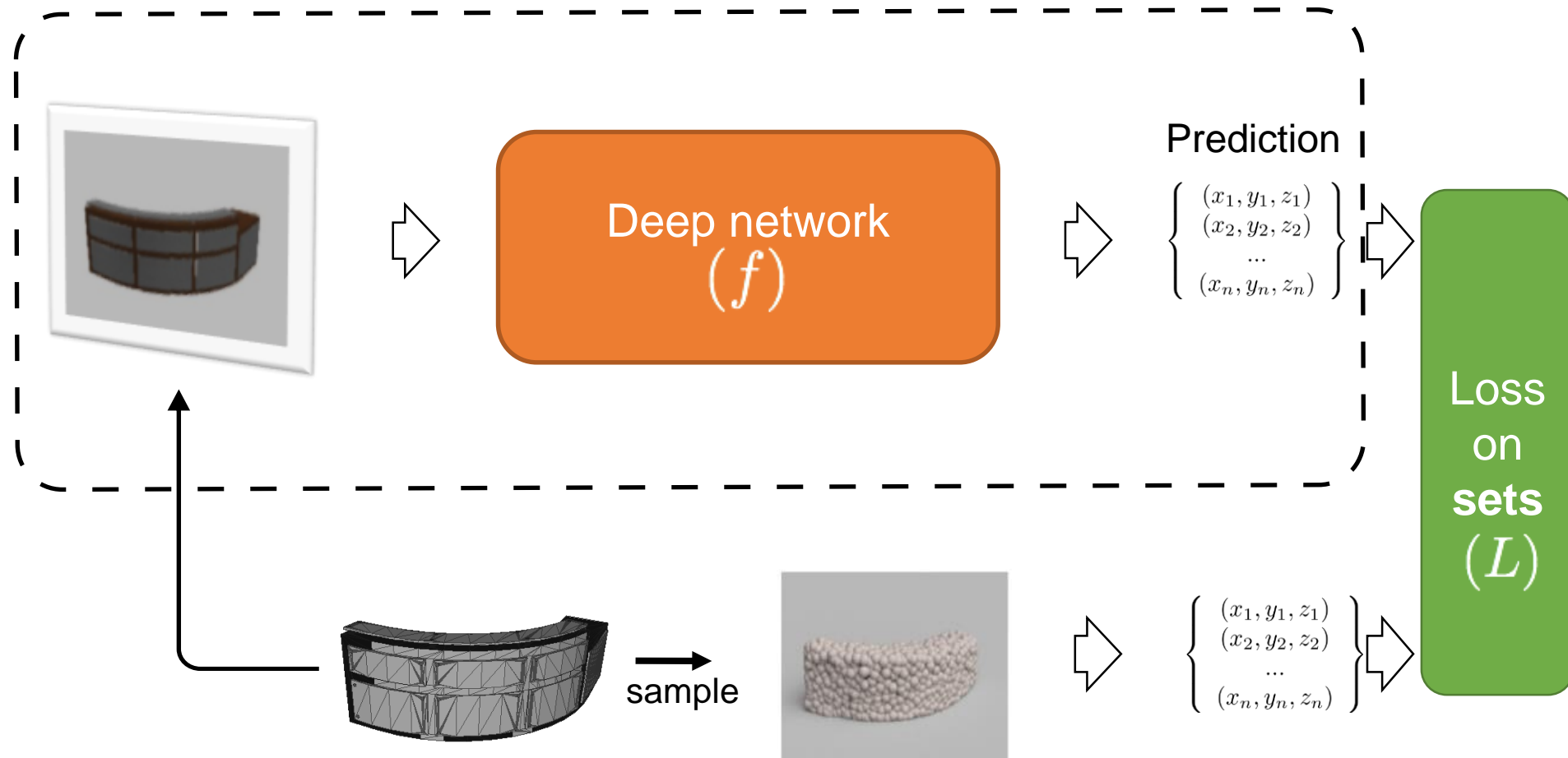
# Point Cloud Synthesis

# Point Cloud Synthesis from a Single Image

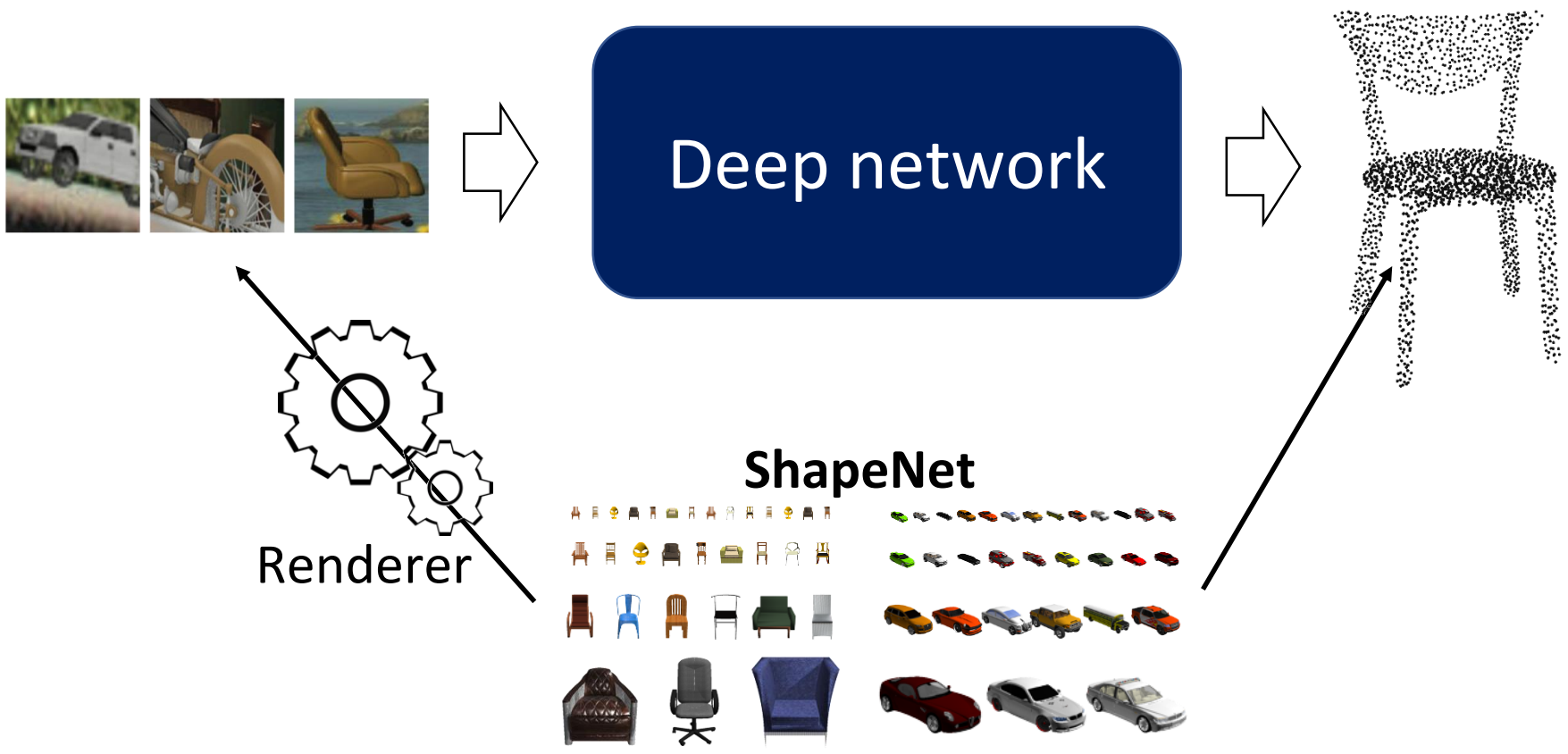


Hao Su, Haoqiang Fan, Leonidas Guibas  
*Learning Shape Abstractions by Assembling Volumetric Primitives*  
CVPR 2017

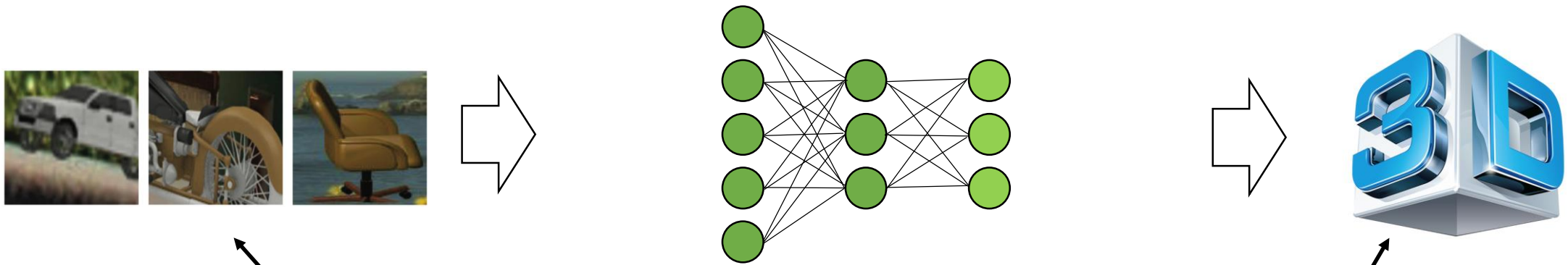
# End-to-End Learning



# Synthesize for Learning



# Supervision from “Synthesize for Learning”



- **200K shapes from 2K categories**
- **10M images with ground truth**

# Point Cloud Distance Metrics

Worst case: Hausdorff distance (HD)

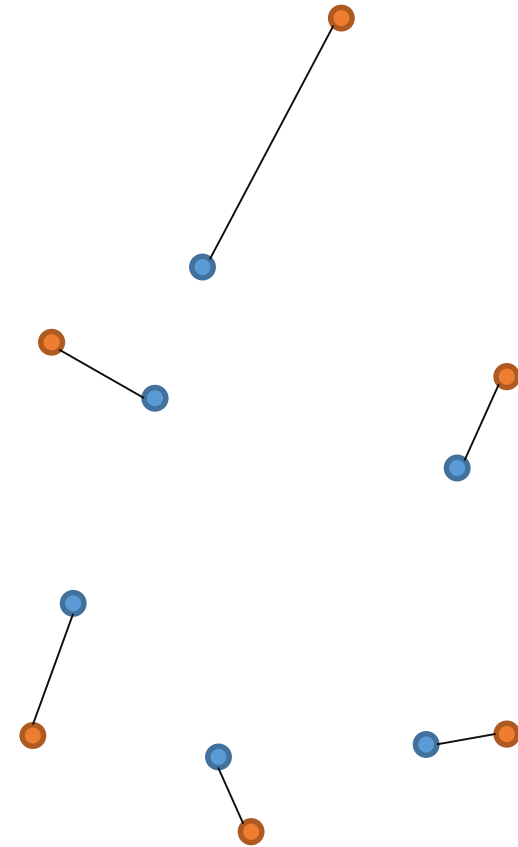
Average case: Chamfer distance (CD)

Optimal case: Earth Mover's distance (EMD)

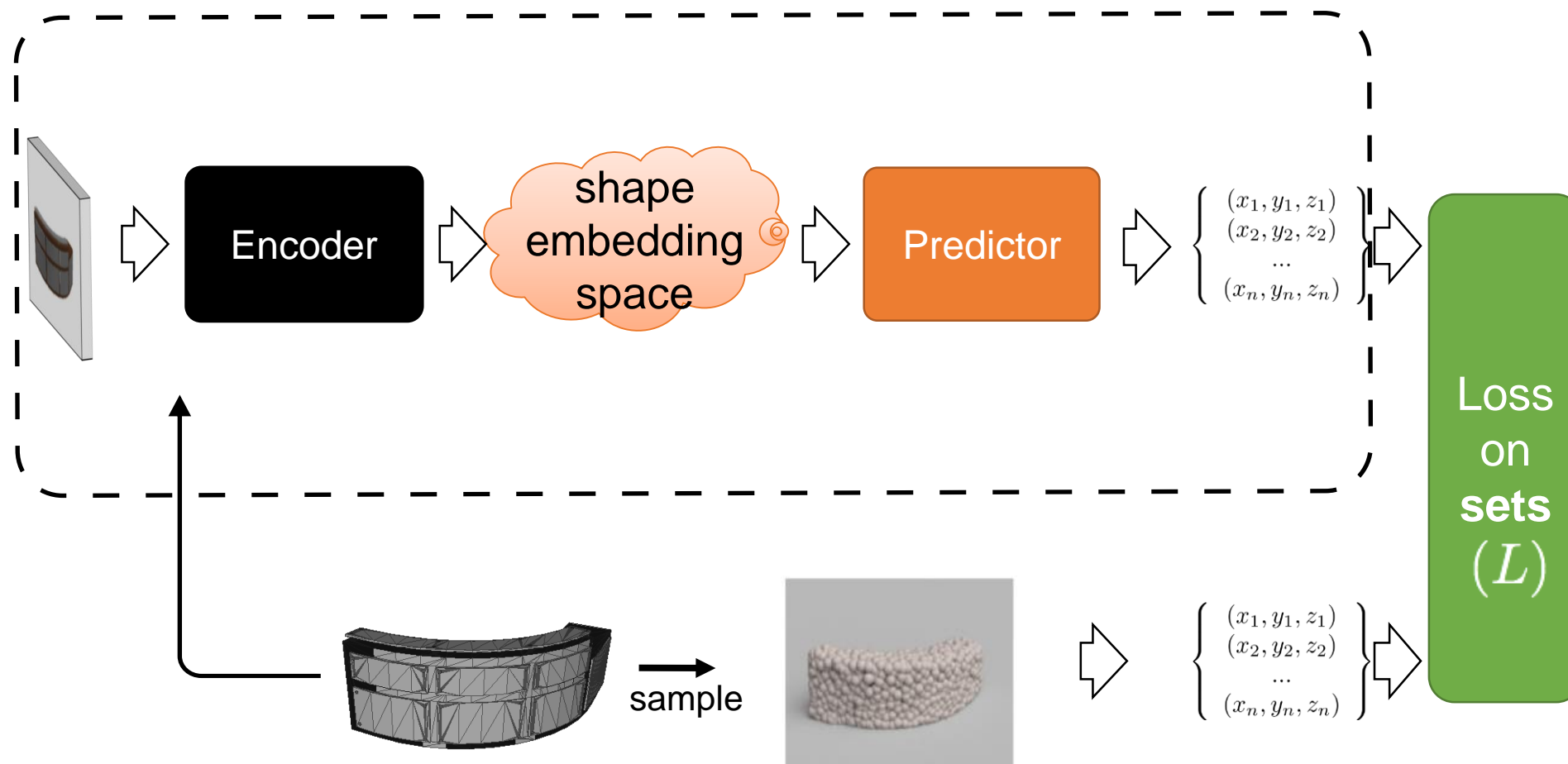
$$d_{EMD}(S_1, S_2) = \min_{\phi: S_1 \rightarrow S_2} \sum_{x \in S_1} \|x - \phi(x)\|_2$$

where  $\phi : S_1 \rightarrow S_2$  is a bijection.

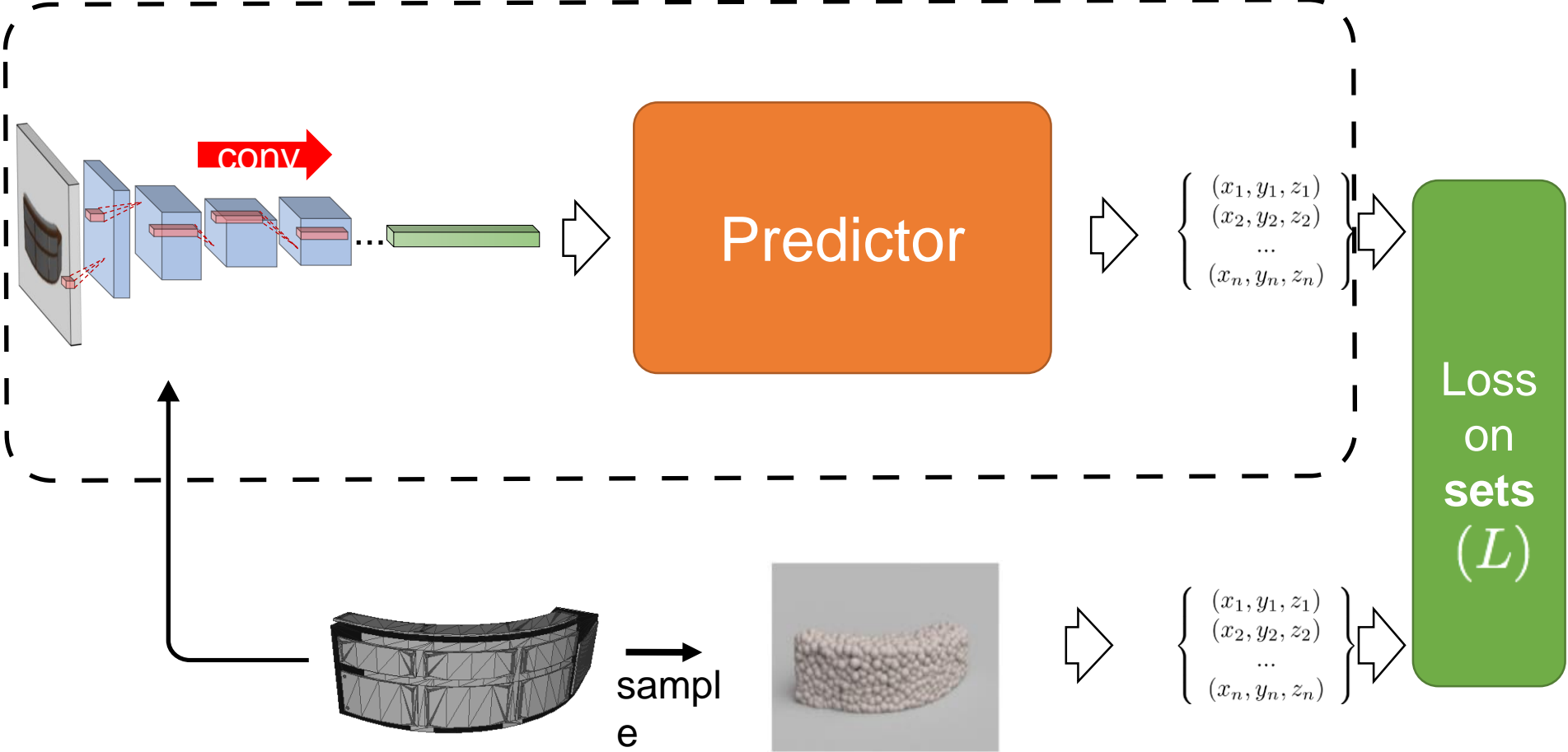
*Solves the optimal transportation (bipartite matching) problem!*



# End-to-End Learning

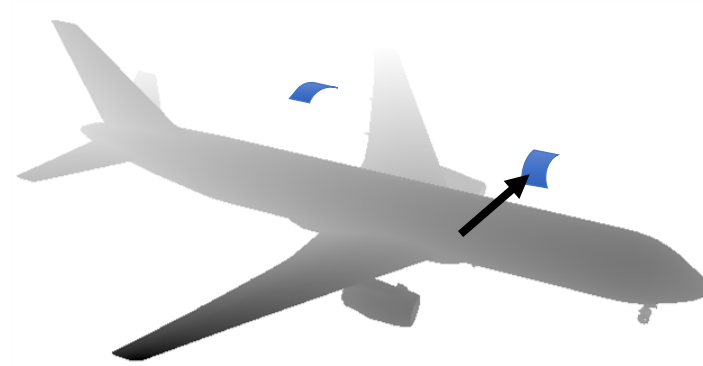
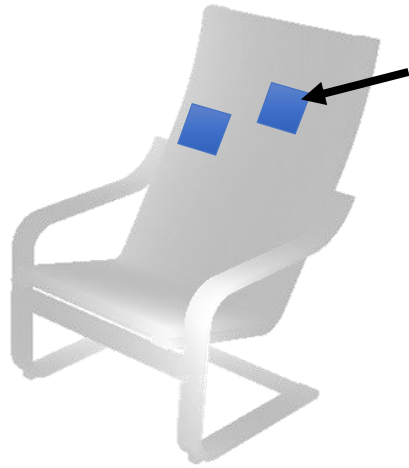


# End-to-End Learning



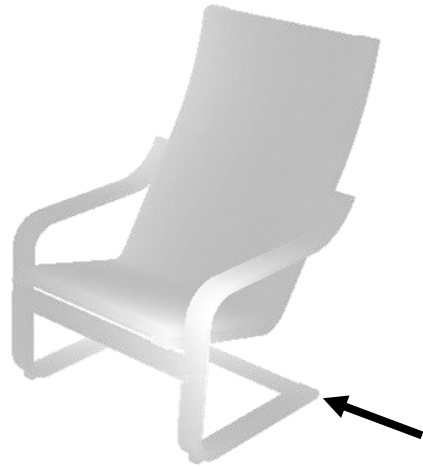


# Natural Statistics of Object Geometry



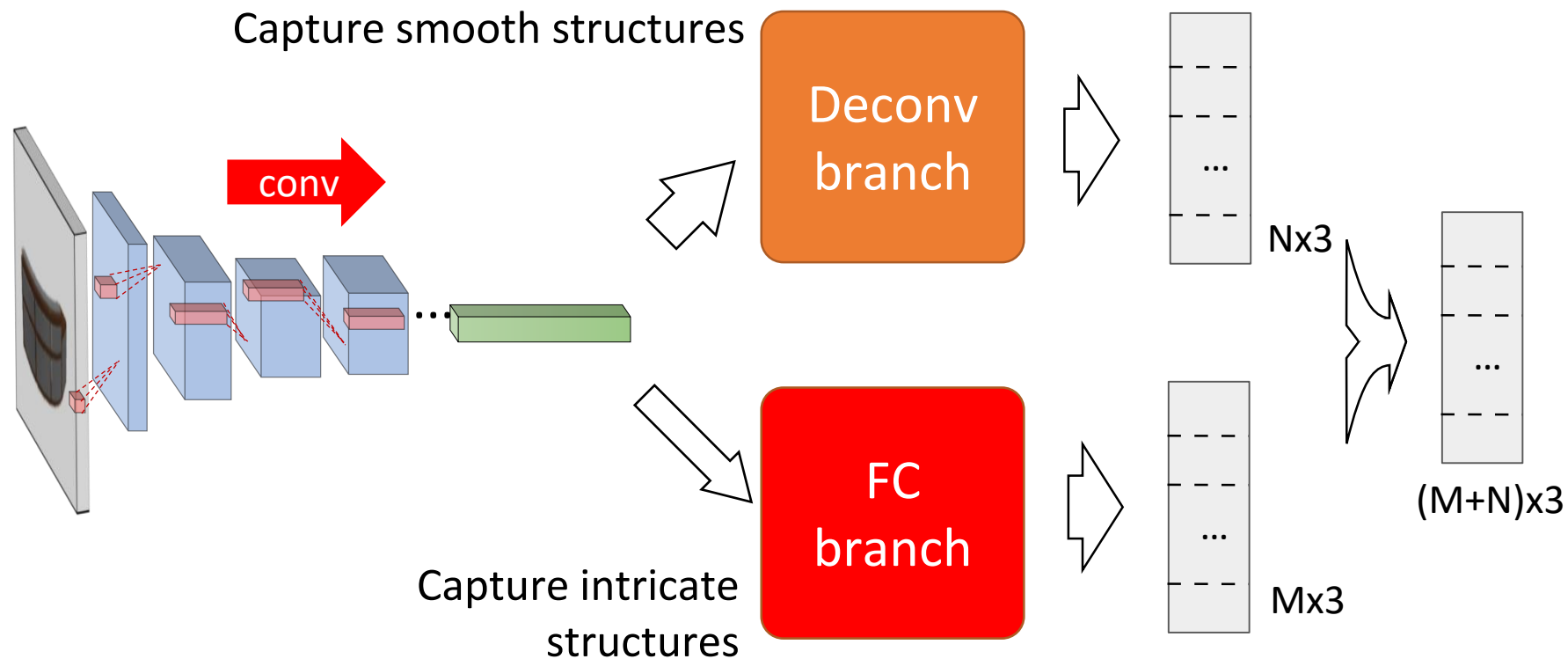
- Many local smooth structures are common
  - e.g., planar patches, cylindrical patches
  - **strong local correlation** among point coordinates

# Natural Statistics of Object Geometry



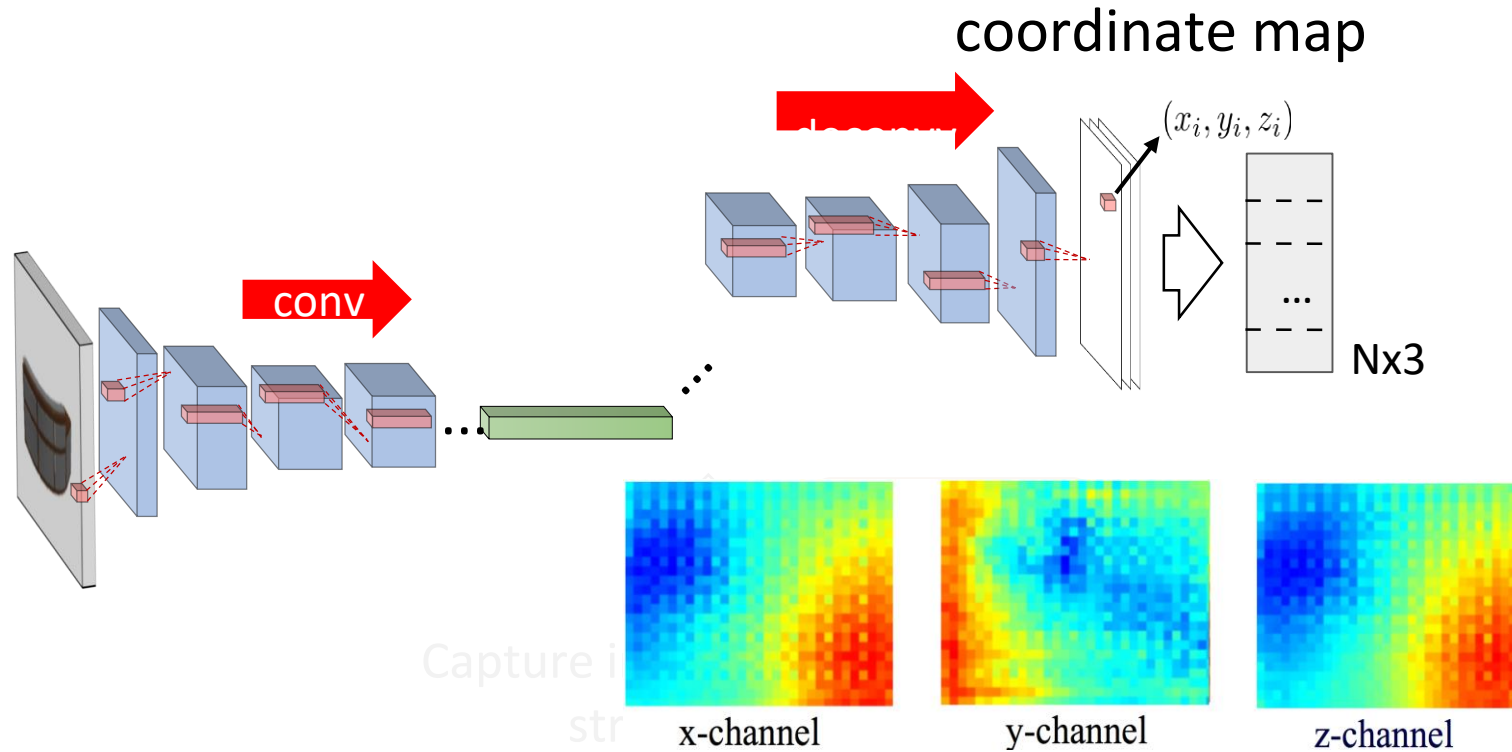
- But also some sharp/intricate local structures
  - some points have **high variability** neighborhoods

# Two-Branch Architecture



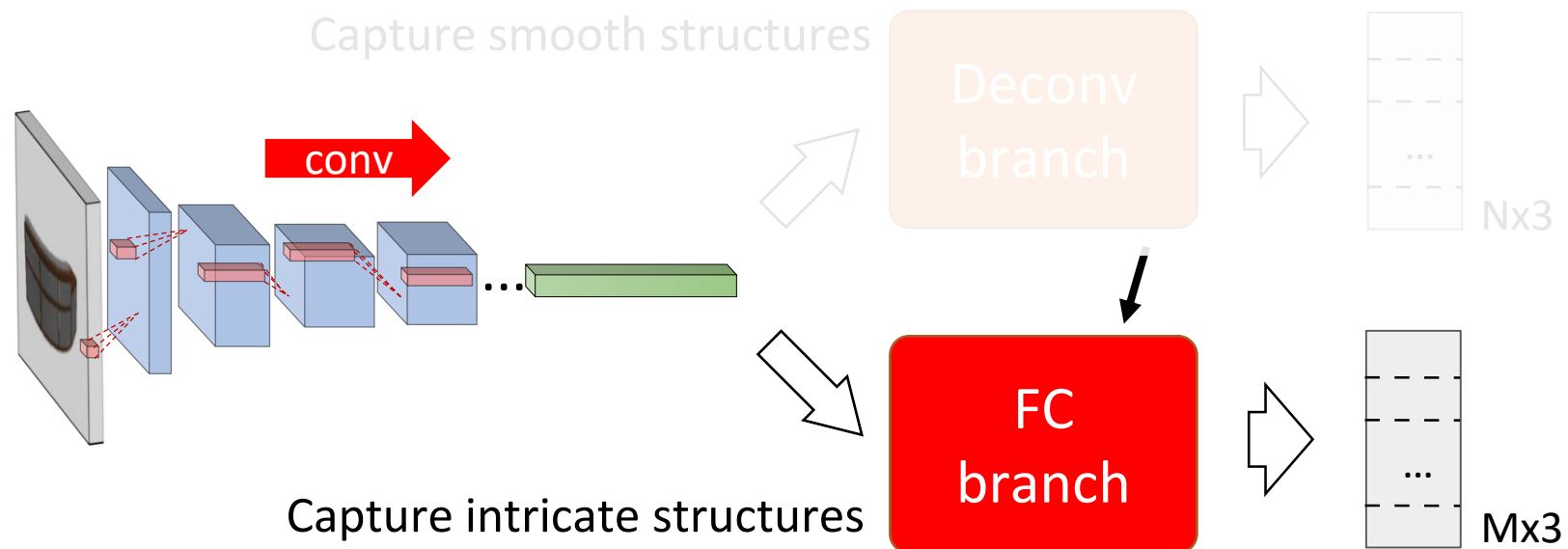
**Set union by array concatenation**

# Deconvolution Branch



- Deconvolution induces a smooth coordinate map
- Geometrically, it learns a smooth parameterization

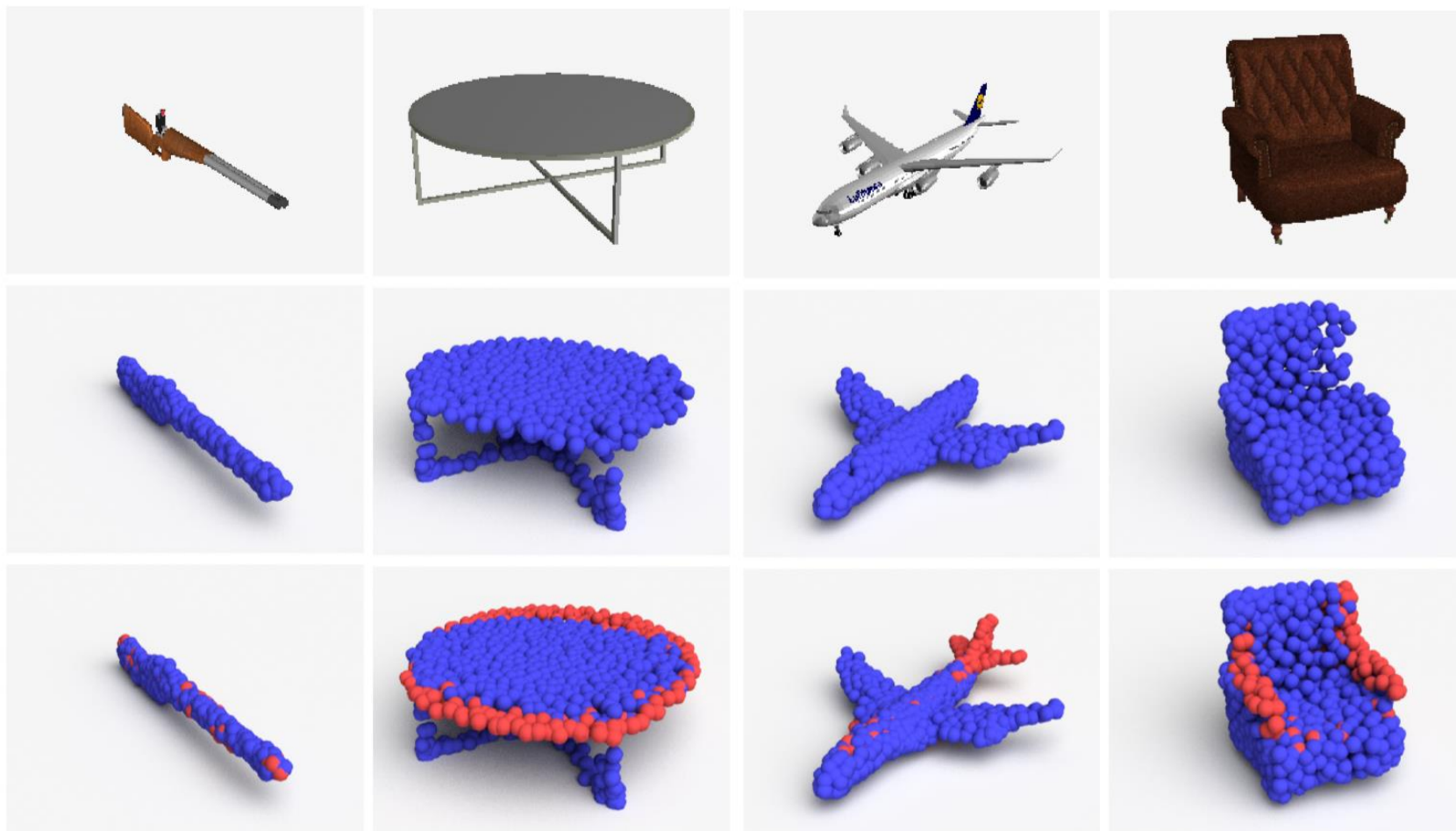
# Fully-Connected Branch



# The Two Branches

**blue:** deconv branch – large, consistent, smooth structures

**red:** fully-connected branch – **more intricate** structures



# Example Results

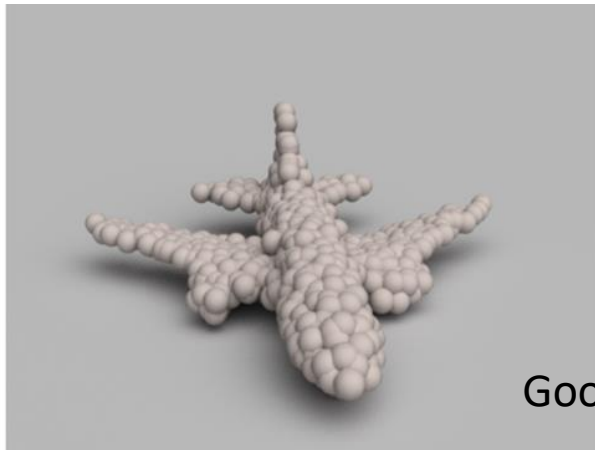
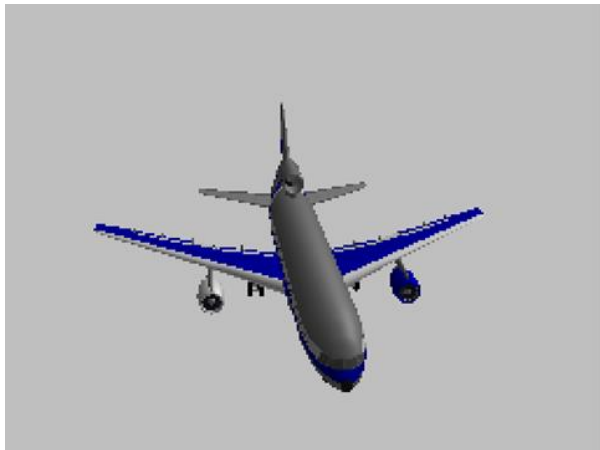


Same view

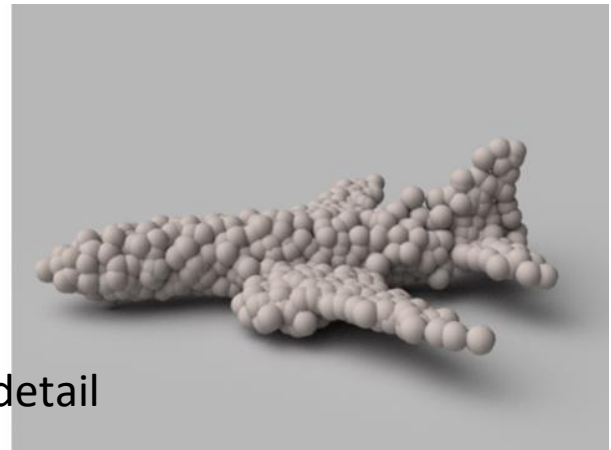


Good symmetry

New view

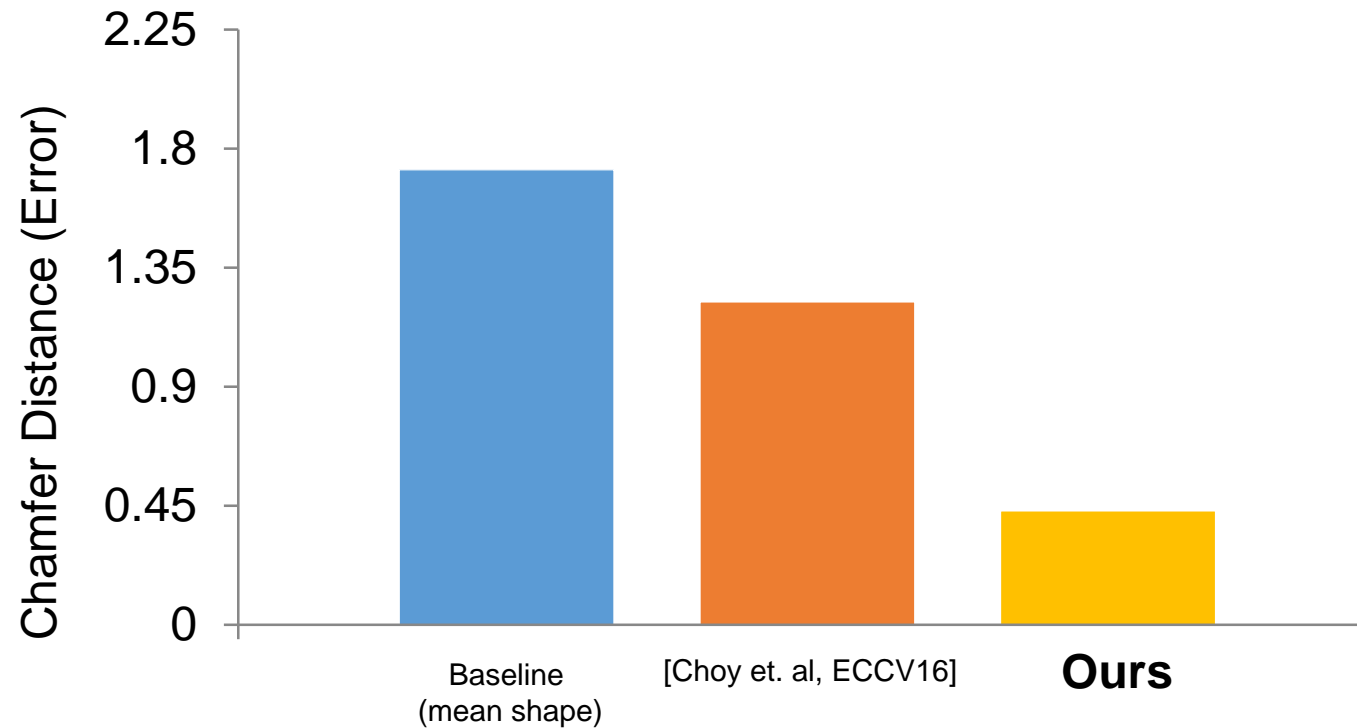


Good detail



# Comparison to State-of-the-Art

Trained/tested on 2K object categories





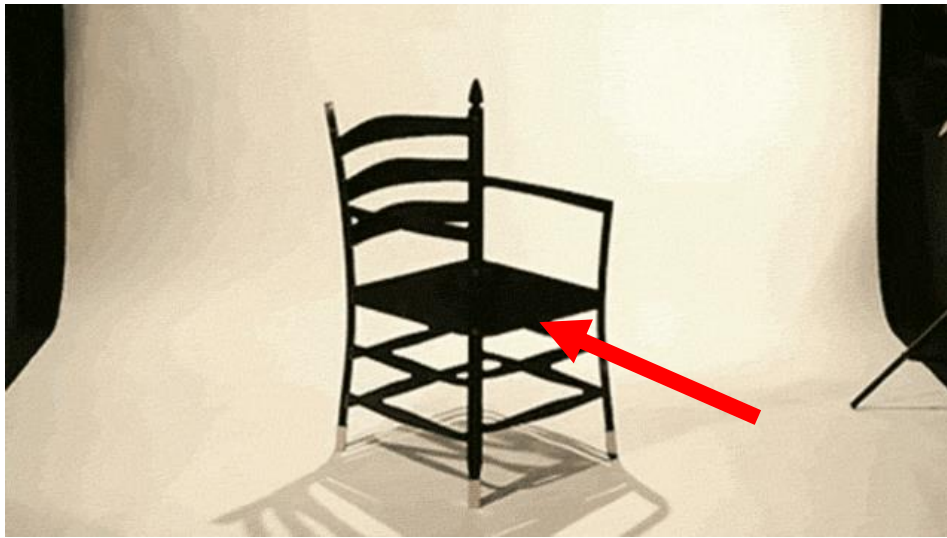
# Influence of Distance Metrics

A fundamental issue: inherent ambiguity in prediction



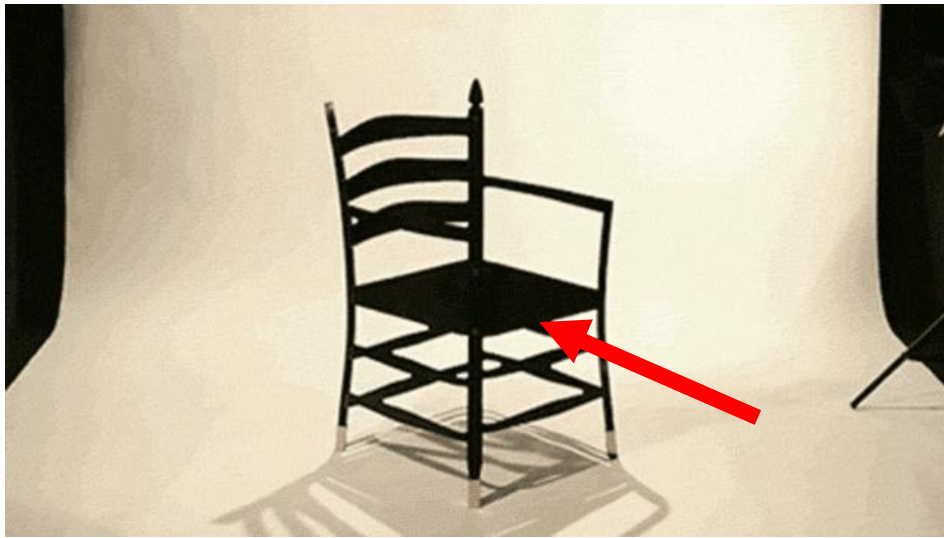
# Influence of Distance Metrics

A fundamental issue: inherent ambiguity in prediction



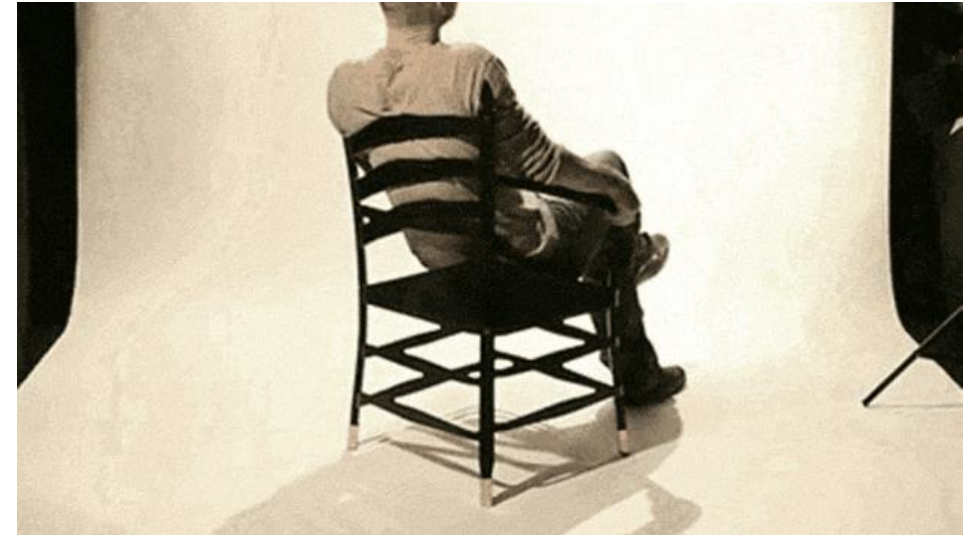
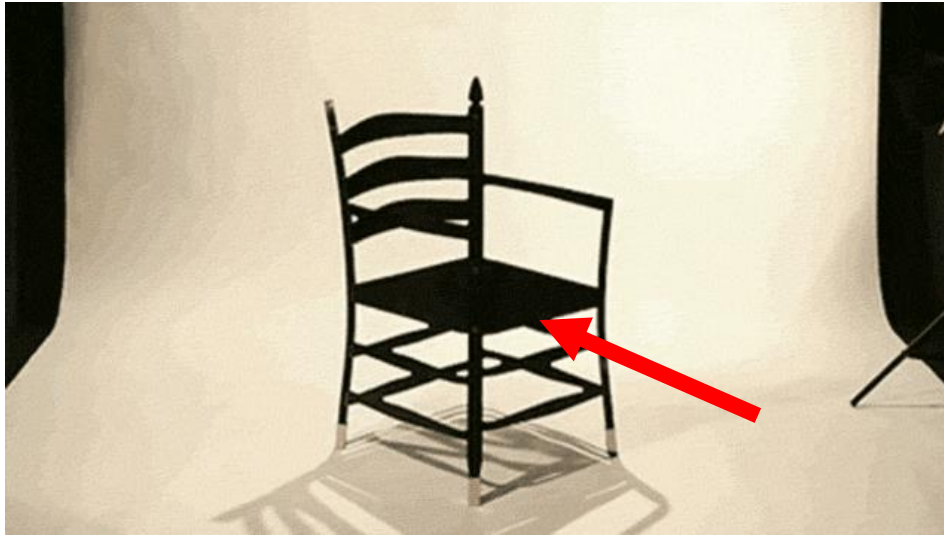
# Influence of Distance Metrics

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# Influence of Distance Metrics

A fundamental issue: inherent ambiguity in prediction



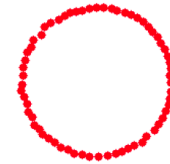
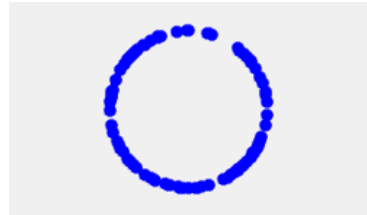
- By loss minimization, the network tends to predict a “**mean shape**” that **averages out** uncertainty

# Distance Metrics Affect Mean Shapes

The mean shape carries characteristics of the distance metric

$$\bar{x} = \operatorname{argmin}_x \mathbb{E}_{s \sim \mathcal{S}} [d(x, s)]$$

continuous  
hidden variable  
(radius)



Input

EMD mean

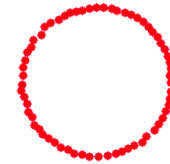
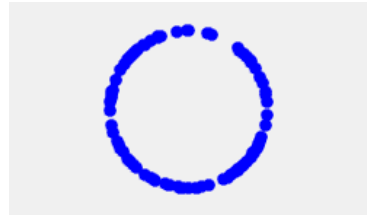
Chamfer mean

# Distance Metrics Affect Mean Shapes

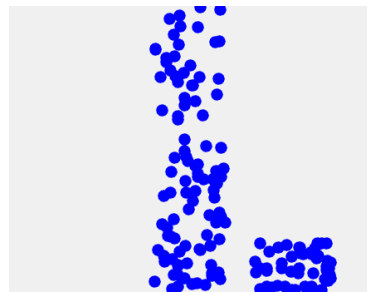
The mean shape carries characteristics of the distance metric

$$\bar{x} = \operatorname{argmin}_x \mathbb{E}_{s \sim \mathcal{S}} [d(x, s)]$$

continuous  
hidden variable  
(radius)



discrete  
hidden variable  
(add-on location)



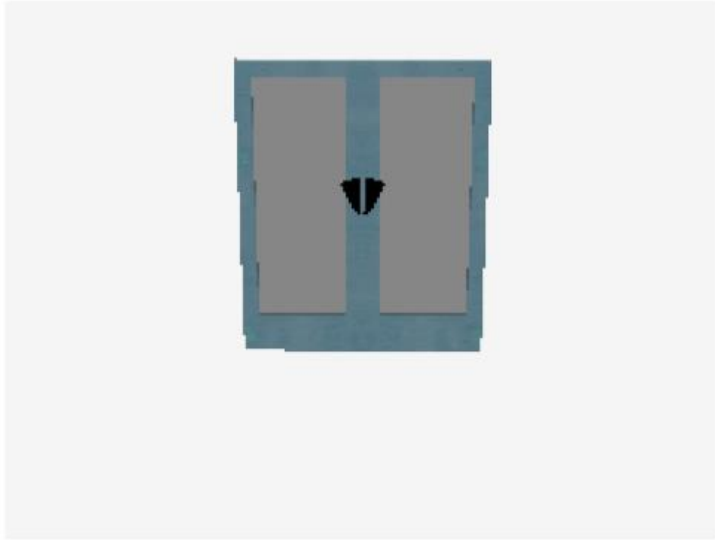
Input

EMD mean

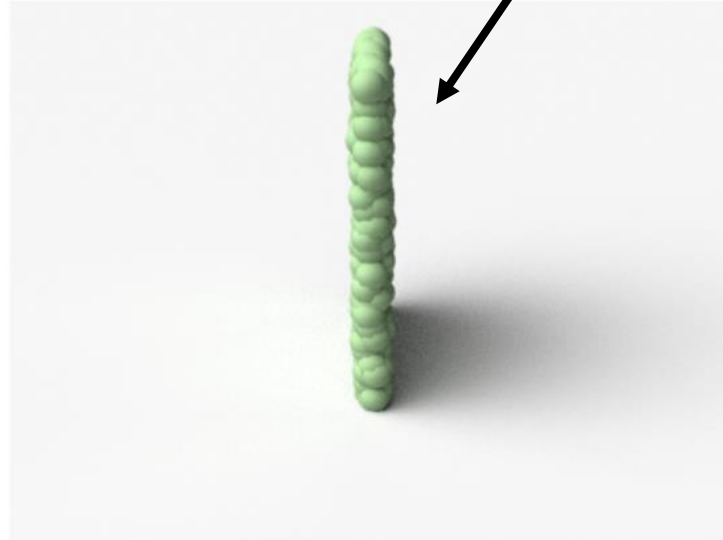
Chamfer mean

# Comparison of Predictions by EMD versus CD

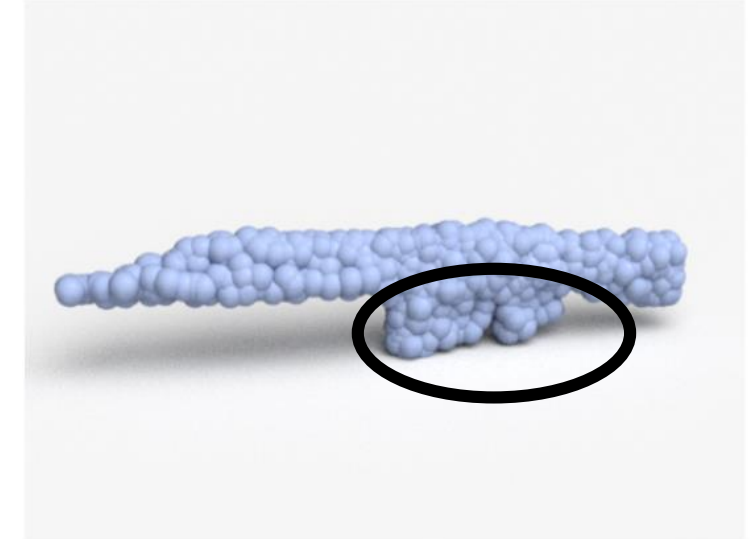
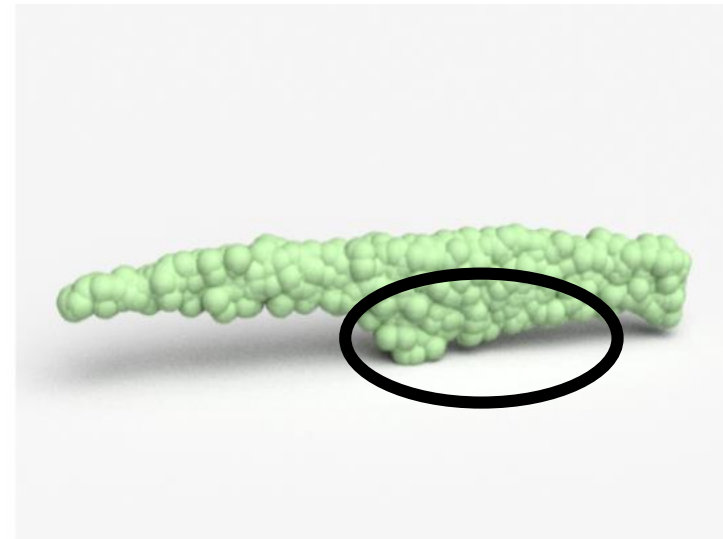
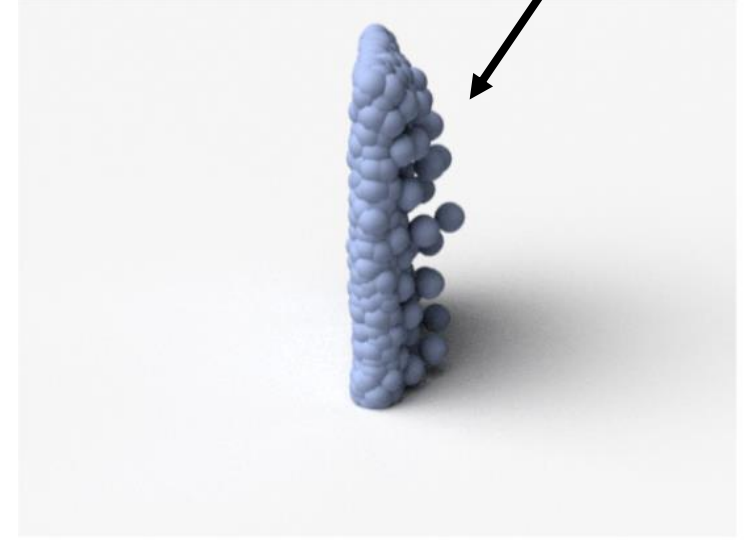
Input



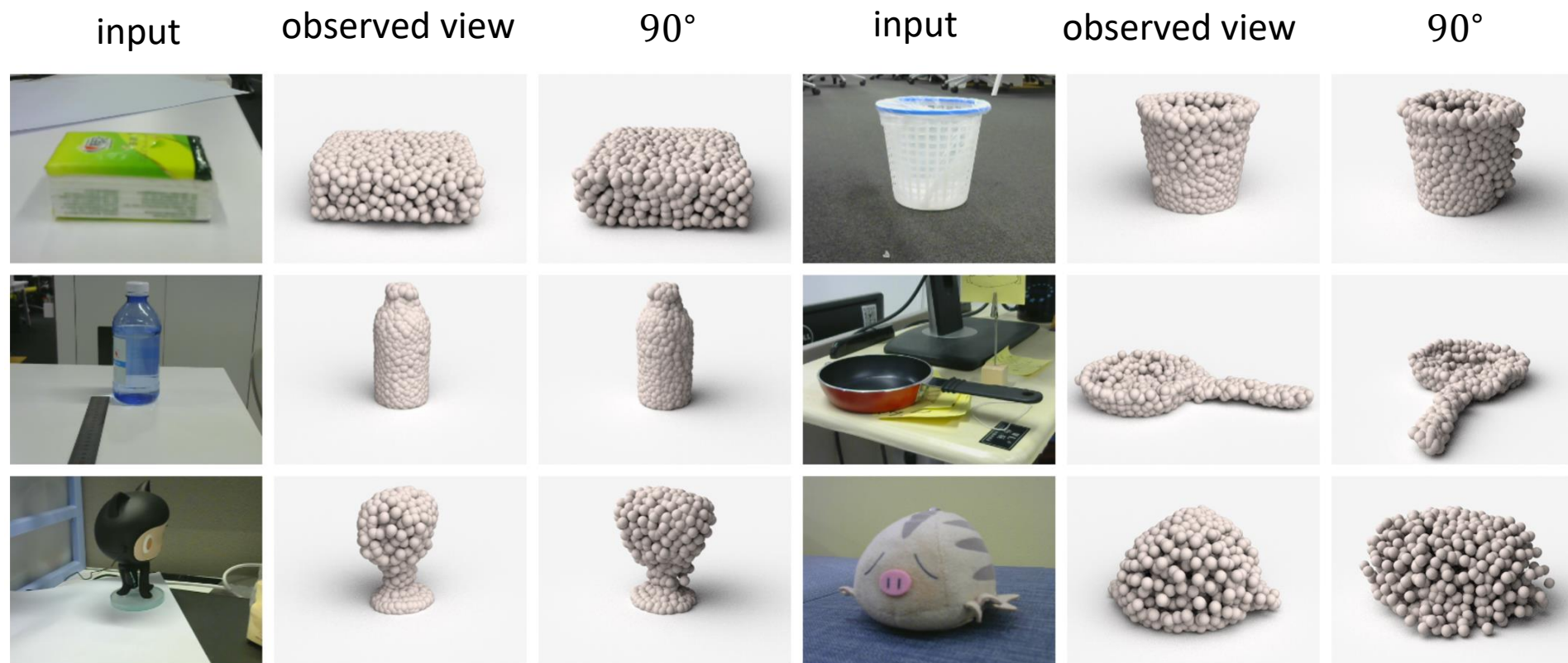
EMD



Chamfer



# From Real Images



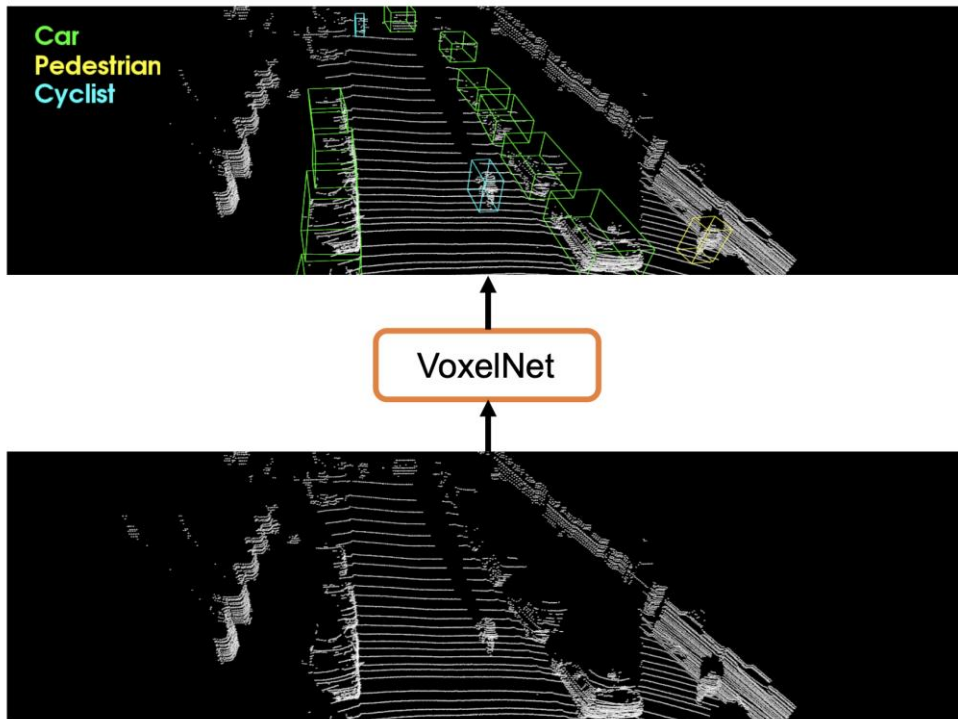
Out of training categories



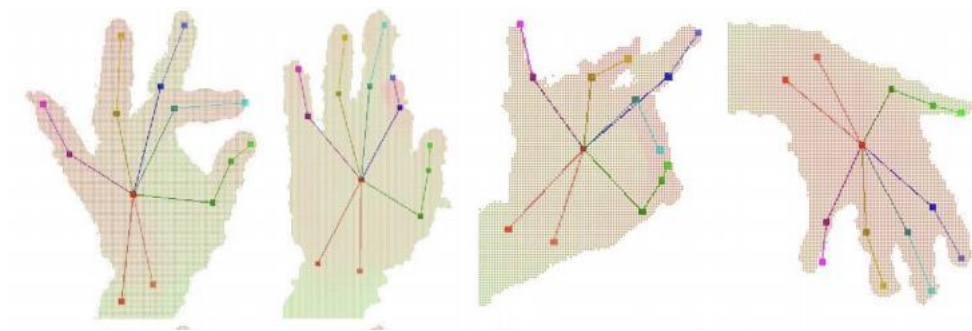
# More Applications of Point Cloud Deep Learning

# Applications of Point Cloud Deep Learning

- 3D object & scene understanding



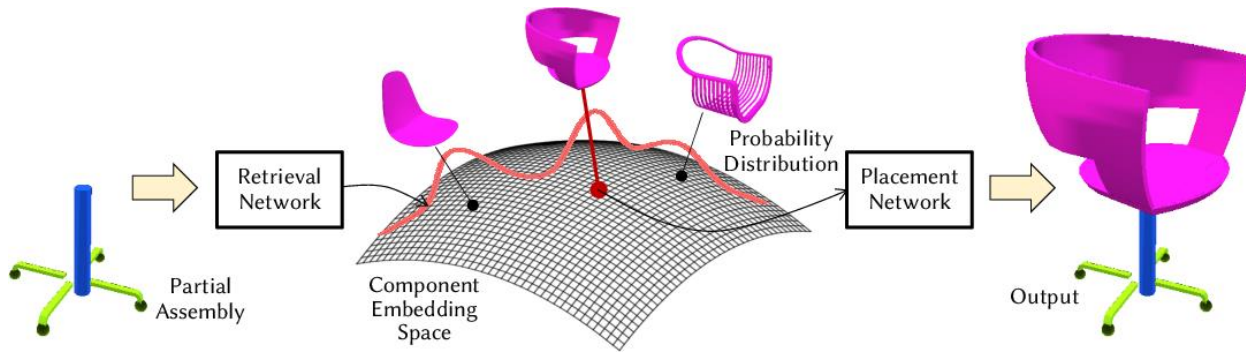
3D Object Detection [VoxelNet by Yin et al.]



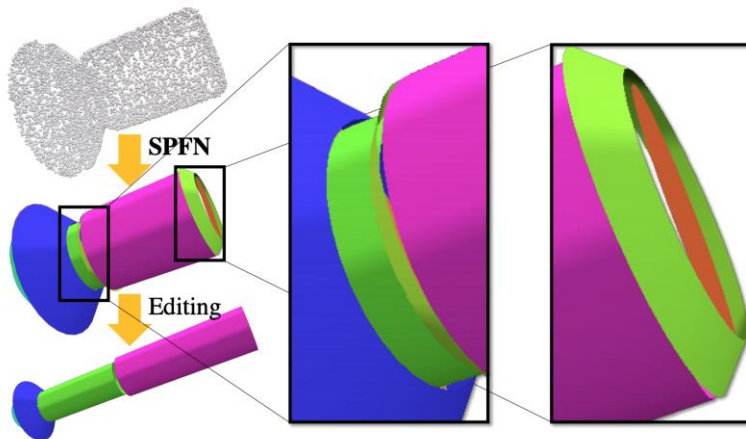
Hand Pose Estimation [Hand PointNet by Ge et al.]

# Applications of Point Cloud Deep Learning

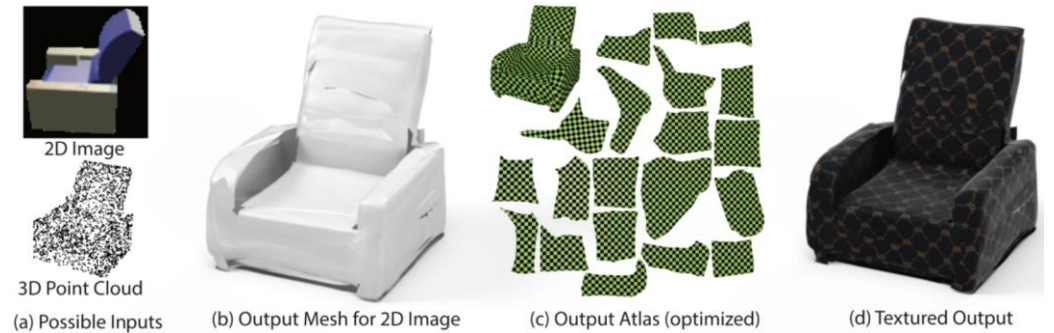
- 3D object & scene understanding
- **AI-assisted shape design**



ComplementMe [Sung et al. 2017]



Primitive fitting [Li et al. CVPR'19]



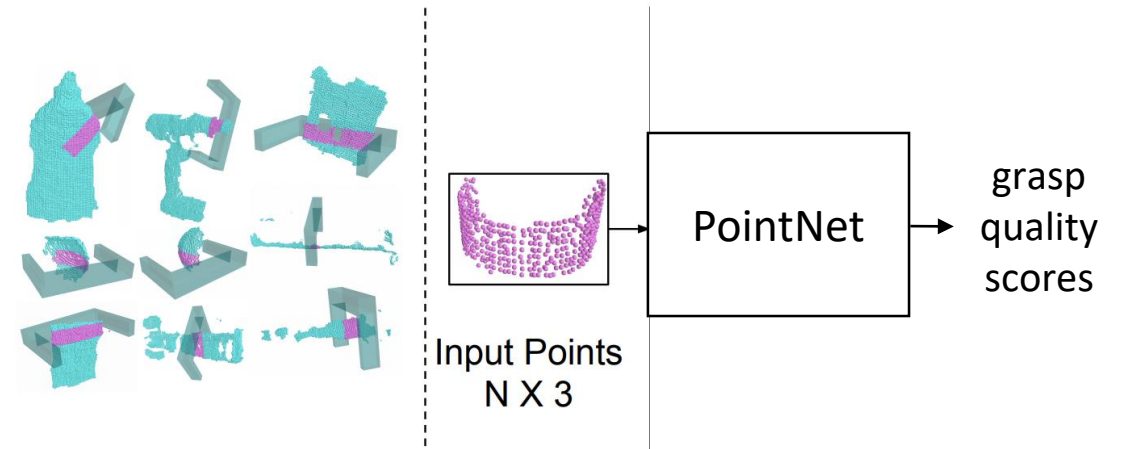
AtlasNet [Groueix et al. 2018]

# Applications of Point Cloud Deep Learning

- 3D object & scene understanding
- AI-assisted shape design
- **Robotics: grasping, manipulation and simulation**



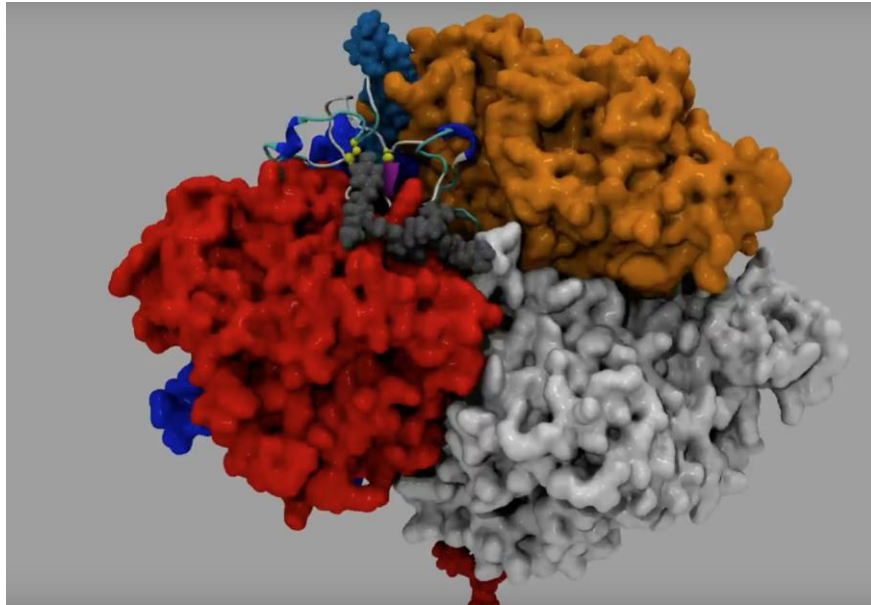
source: Ludovic Righetti



PointNetGPD by Liang et al. ICRA19

# Applications of Point Cloud Deep Learning

- 3D object & scene understanding
- AI-assisted shape design
- Robotics: grasping, manipulation and simulation
- **Molecular biology: from structure to function**



source: BPC@University Greifswald

# Future Directions for Point Cloud Deep Learning

# Future Directions

- **Scalability**

How to scale up from processing 100k points to 1M or even 10M points?

(1024 x 1024 image  $\approx$  1M pixels)

Trade-offs in neighborhood sampling

More memory efficient operators



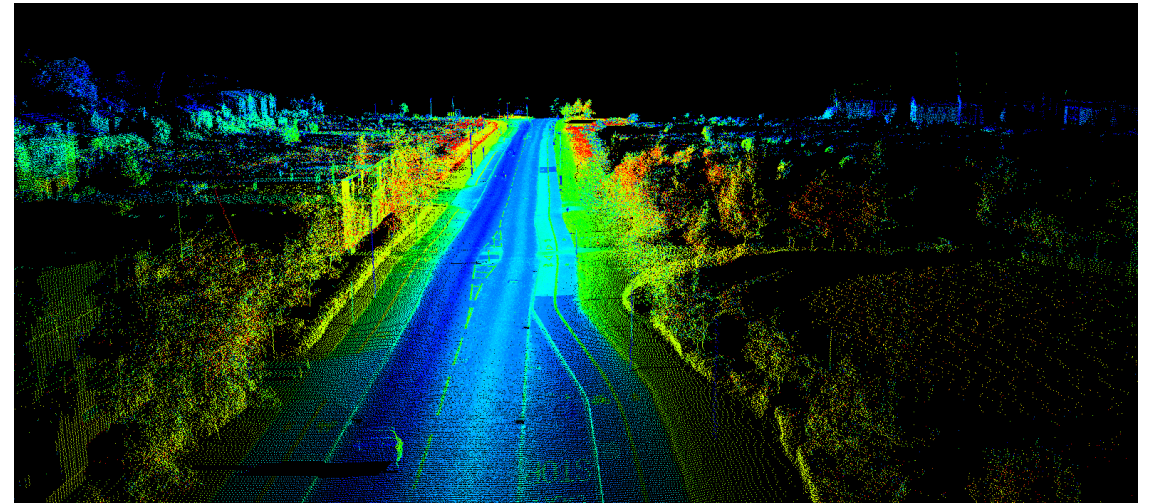
# Future Directions

- Scalability
- **Multi-modality**



*RGB images*

*High resolution  
Rich textures*



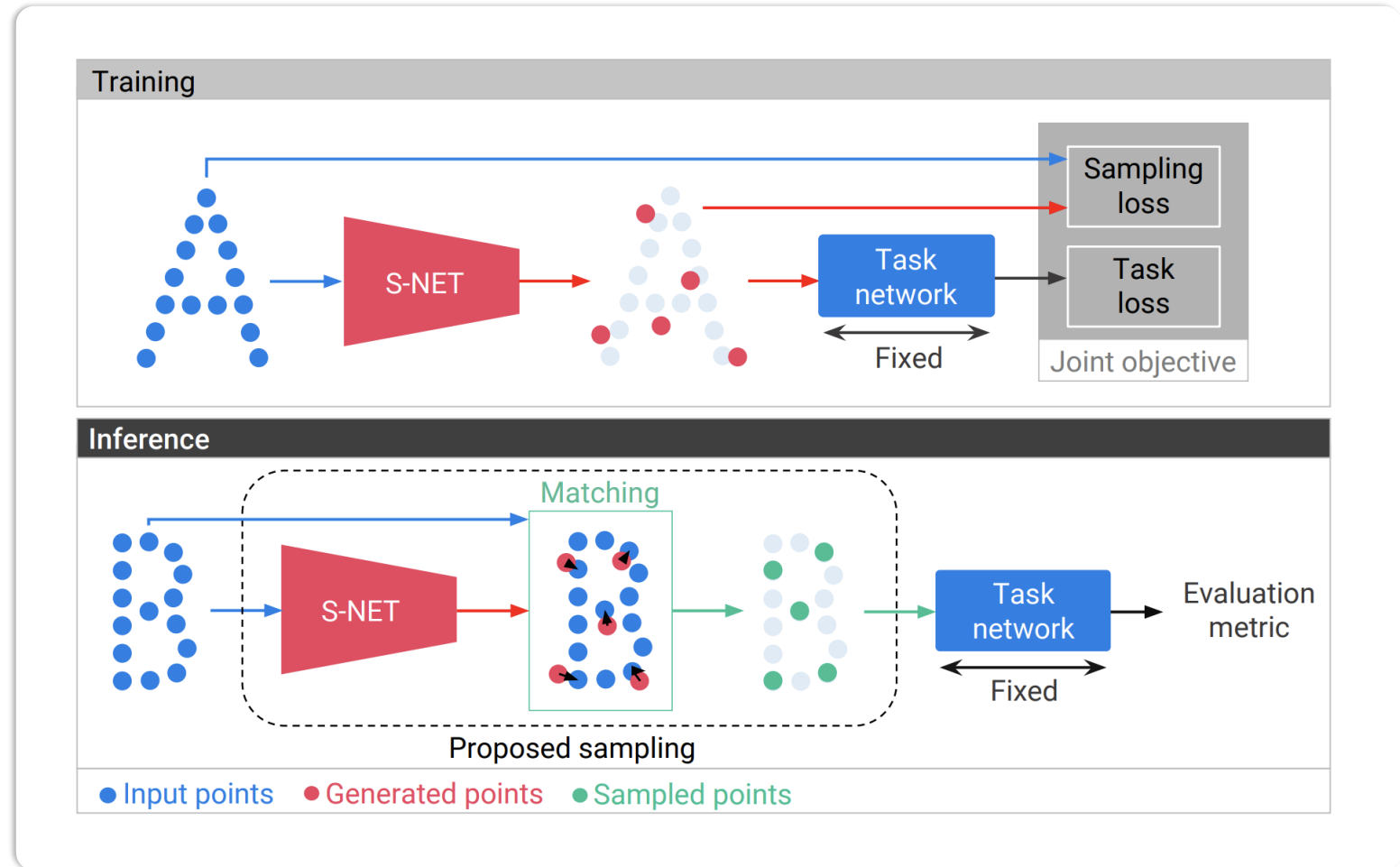
*Lidar point clouds*

*Accurate depth  
Accurate 3D geometry*



# Future Directions

- Scalability
- Multi-modality
- **Sampling**



Learning to sample [Dovrat et al.]

# General Set / Graph Processors

- Scalability
- Multi-modality
- Sampling
- **Set processing**



# Future Directions

- Scalability
- Multi-modality
- Sampling
- Set processing
- **Geometry generation**

How to generate?  
How to measure quality?

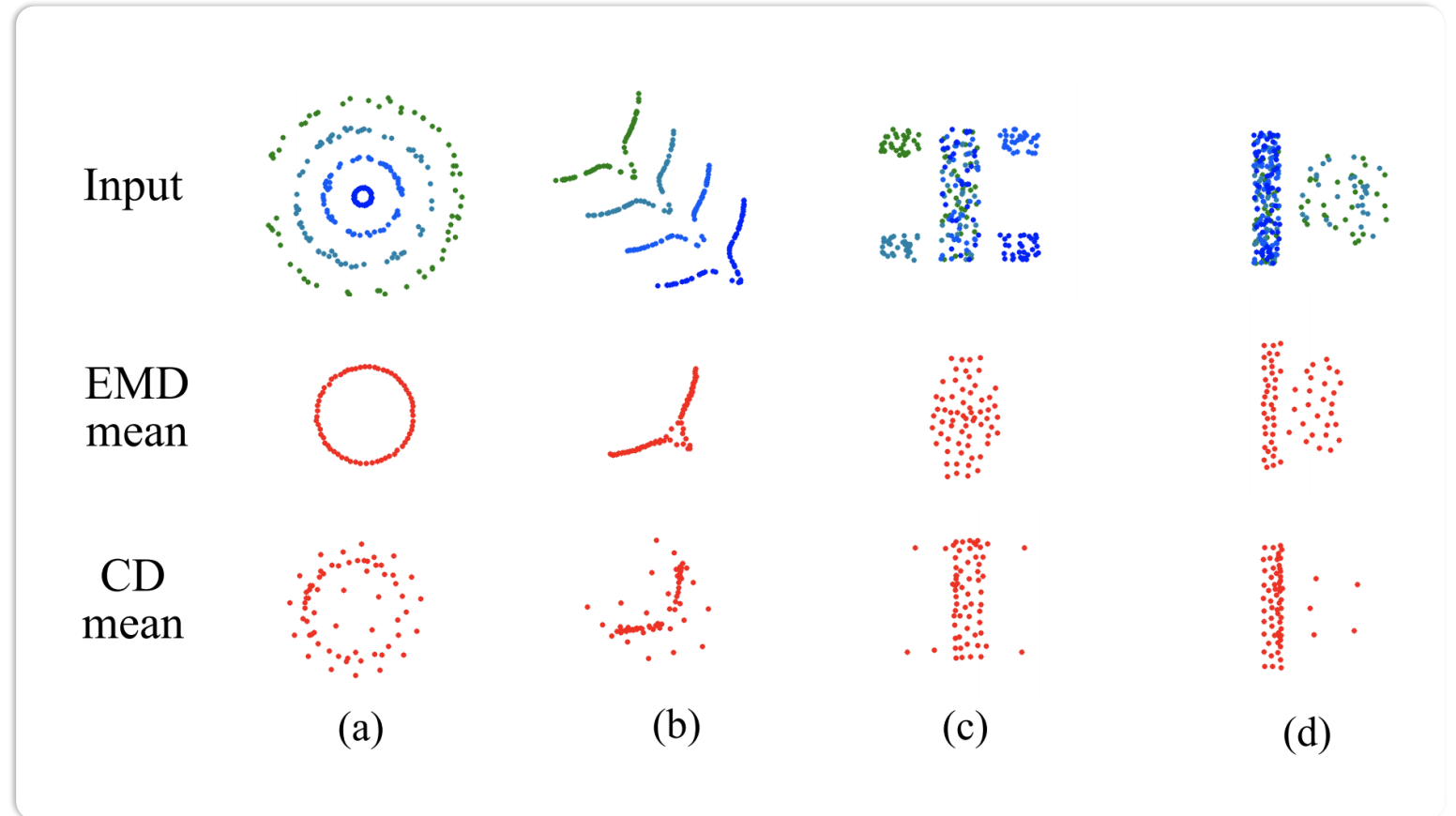
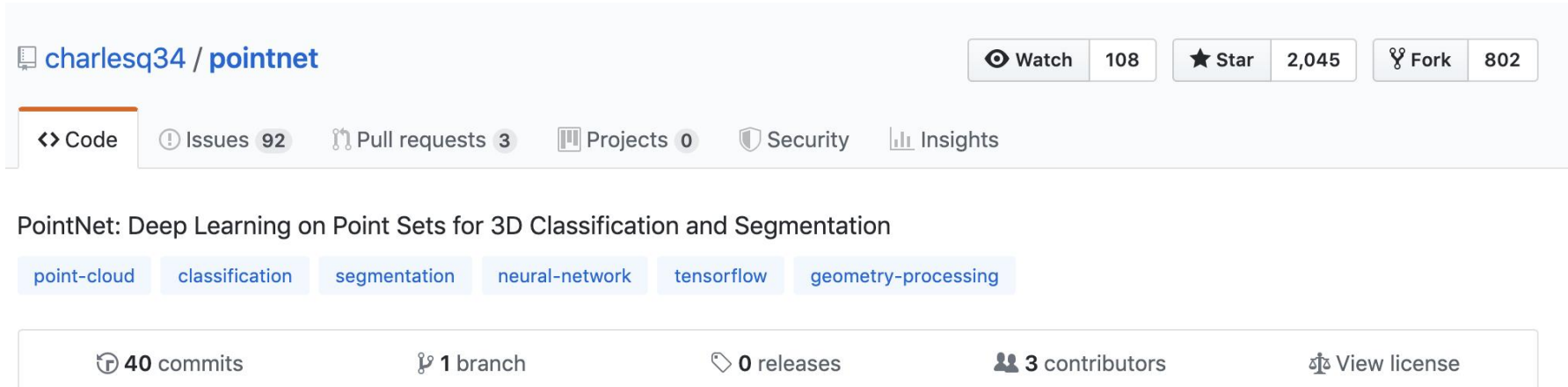


Figure from [Fan et al. CVPR 2017]

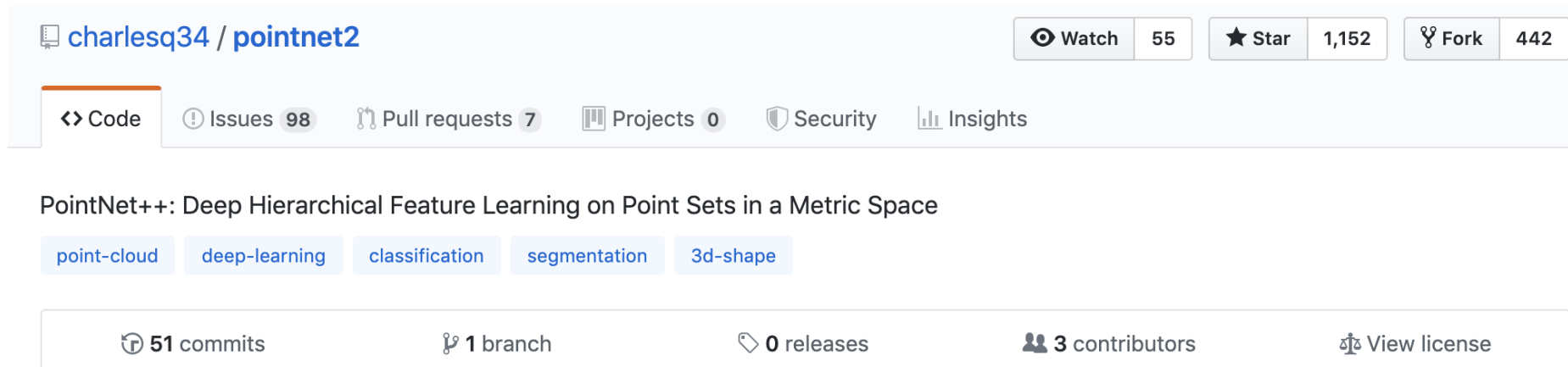
# Code for PointNet, PointNet++ on GitHub

- <https://github.com/charlesq34/pointnet>



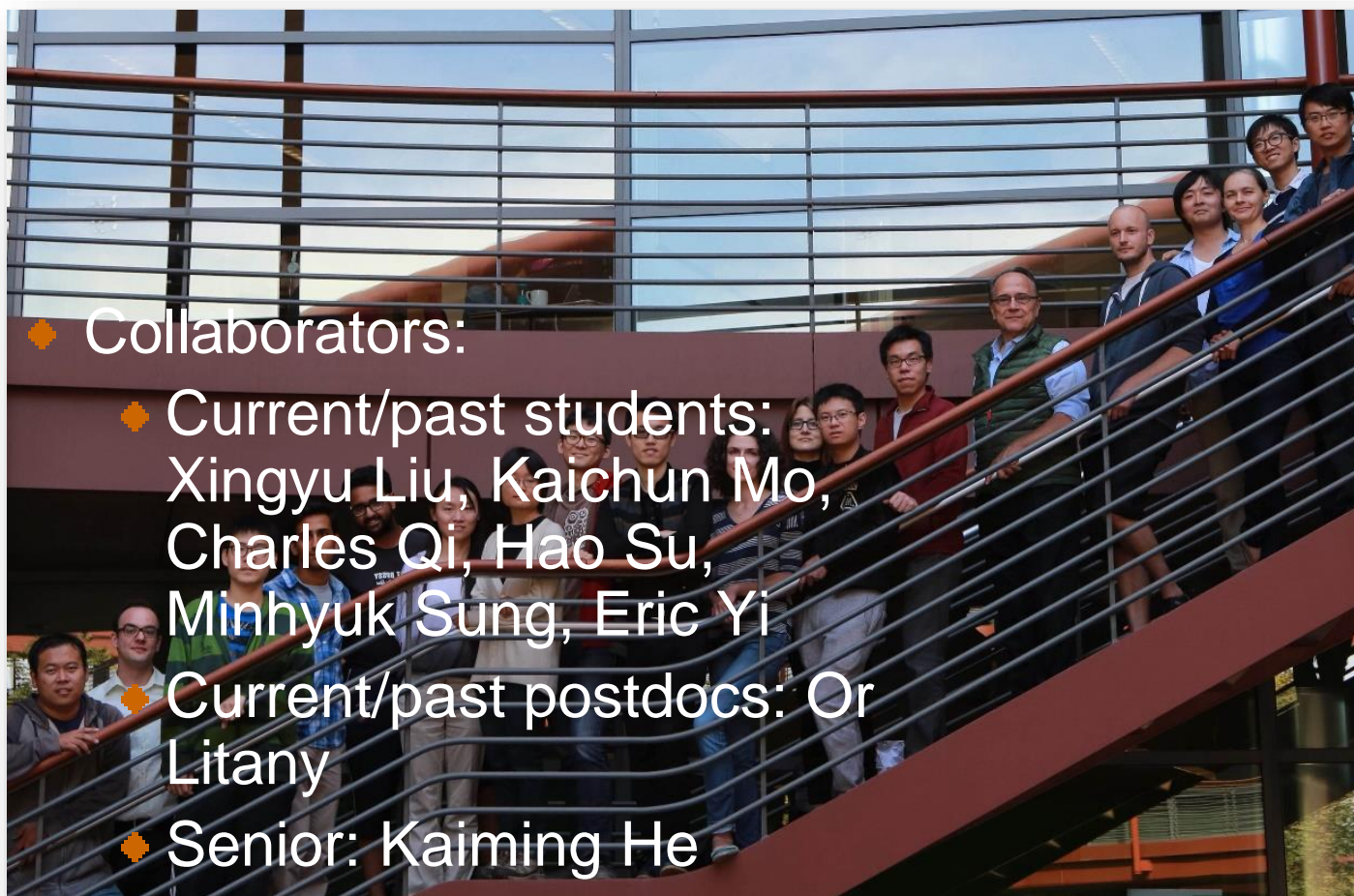
The screenshot shows the GitHub repository page for 'charlesq34 / pointnet'. At the top, there are statistics: Watch (108), Star (2,045), and Fork (802). Below these are navigation tabs: Code (selected), Issues (92), Pull requests (3), Projects (0), Security, and Insights. The repository description is 'PointNet: Deep Learning on Point Sets for 3D Classification and Segmentation'. There are six topic tags: point-cloud, classification, segmentation, neural-network, tensorflow, and geometry-processing. At the bottom, there are more statistics: 40 commits, 1 branch, 0 releases, 3 contributors, and a link to View license.

- <https://github.com/charlesq34/pointnet2>



The screenshot shows the GitHub repository page for 'charlesq34 / pointnet2'. At the top, there are statistics: Watch (55), Star (1,152), and Fork (442). Below these are navigation tabs: Code (selected), Issues (98), Pull requests (7), Projects (0), Security, and Insights. The repository description is 'PointNet++: Deep Hierarchical Feature Learning on Point Sets in a Metric Space'. There are five topic tags: point-cloud, deep-learning, classification, segmentation, and 3d-shape. At the bottom, there are more statistics: 51 commits, 1 branch, 0 releases, 3 contributors, and a link to View license.

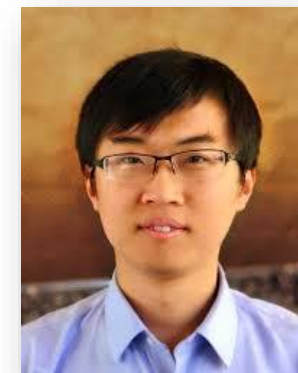
# Acknowledgements



- ◆ Collaborators:
  - ◆ Current/past students: Xingyu Liu, Kaichun Mo, Charles Qi, Hao Su, Minhyuk Sung, Eric Yi
  - ◆ Current/past postdocs: Or Litany
  - ◆ Senior: Kaiming He



Charles Qi



Hao Su



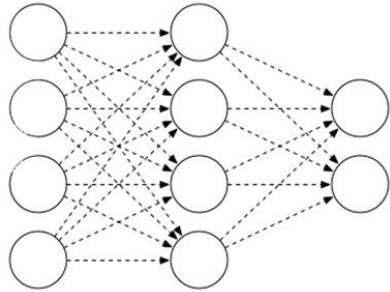
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# Course Information (slides/code/comments)



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