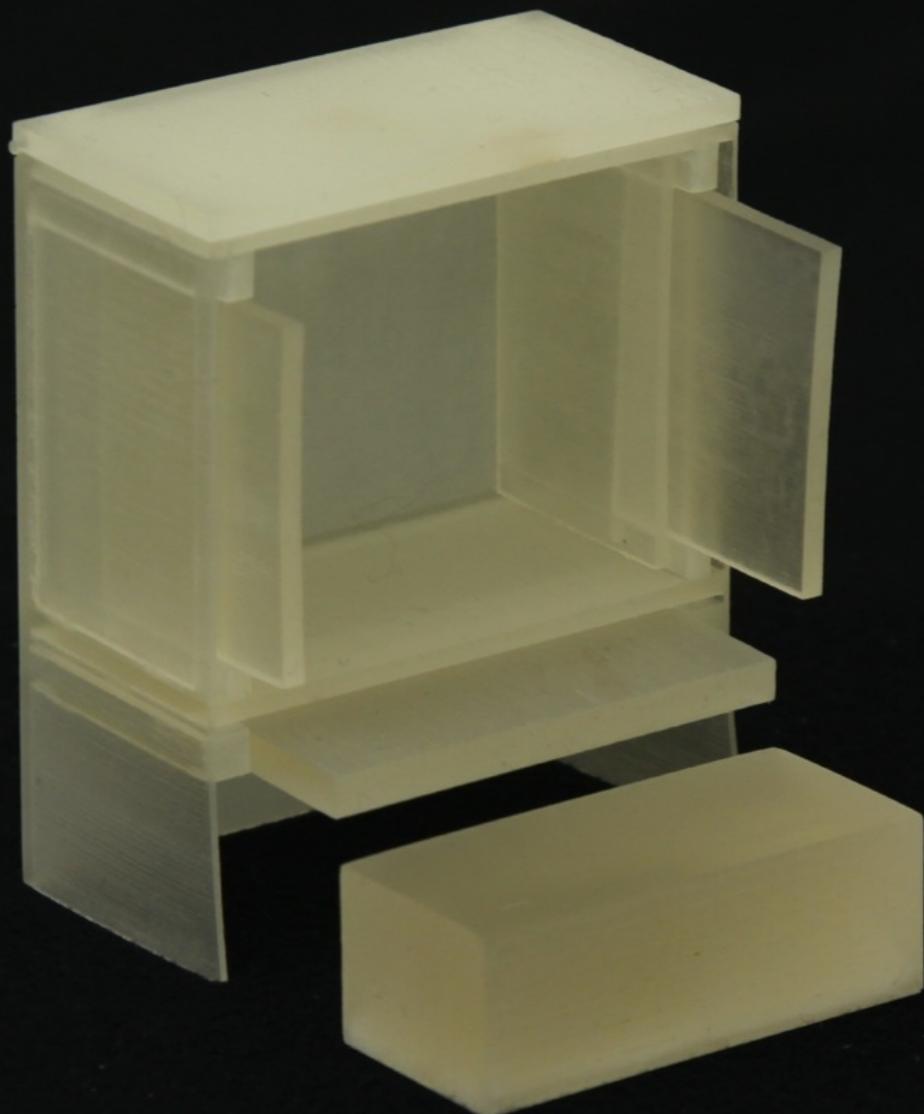


# Creating Works-like Prototypes of Mechanical Objects

Bongjin Koo<sup>1</sup> Wilmot Li<sup>2</sup> JiaXian Yao<sup>3</sup> Maneesh Agrawala<sup>3</sup>  
Niloy J. Mitra<sup>1</sup>

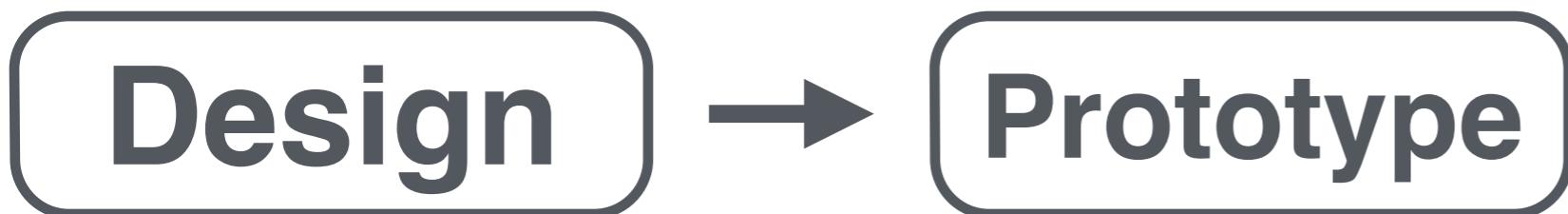
<sup>1</sup>University College London <sup>2</sup>Adobe Research <sup>3</sup>UC Berkeley



# Design process example

Design

# Design process example



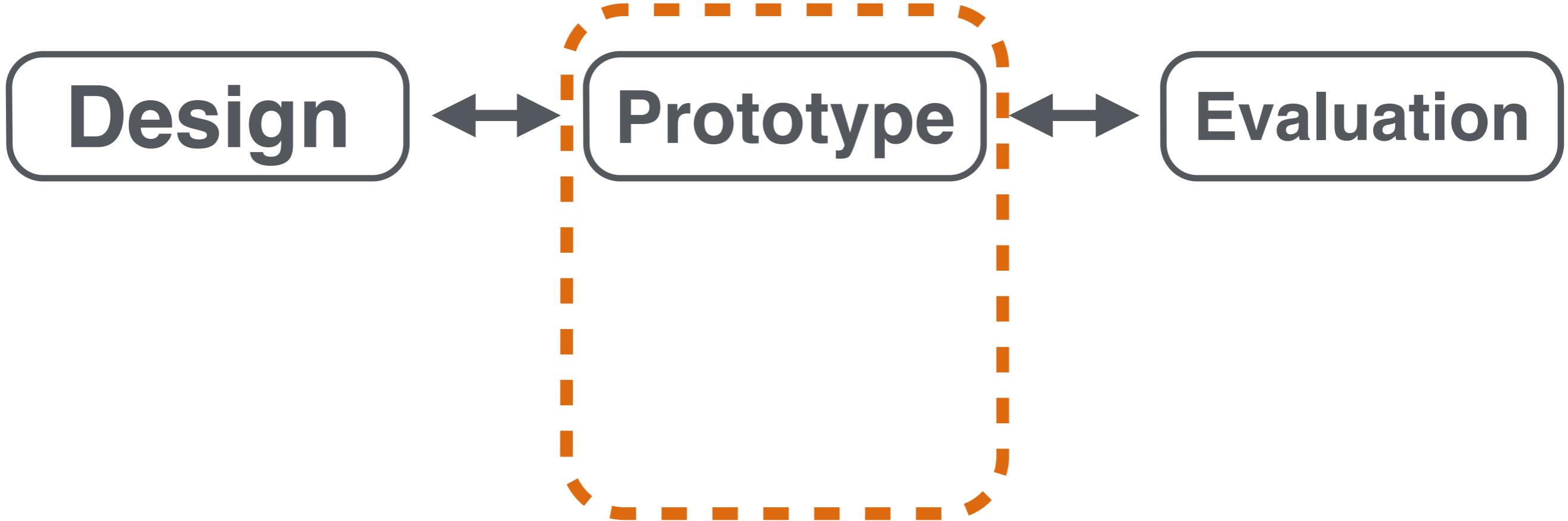
# Design process example



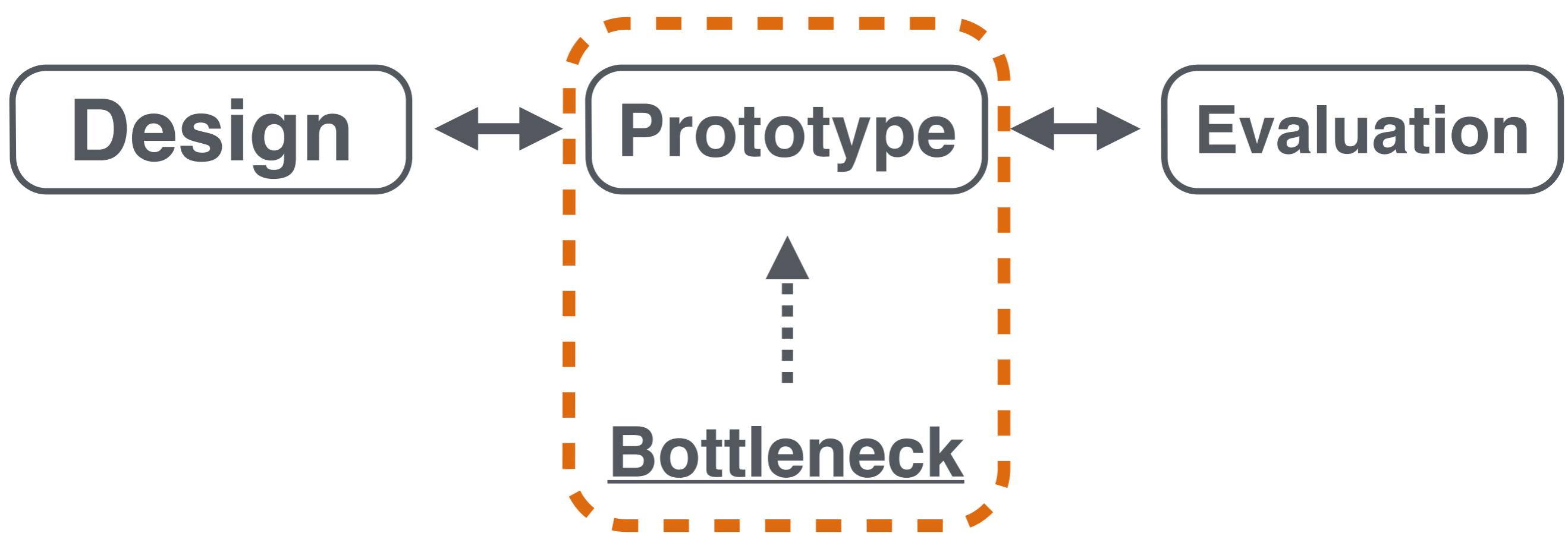
# Design process example



# Design process example



# Design process example



# Works-like prototypes



# Many iterations



# Contributions

Identified useful **high-level functional relationships**

# Contributions

Identified useful **high-level functional relationships**

**Interactive tool for creating works-like prototypes**

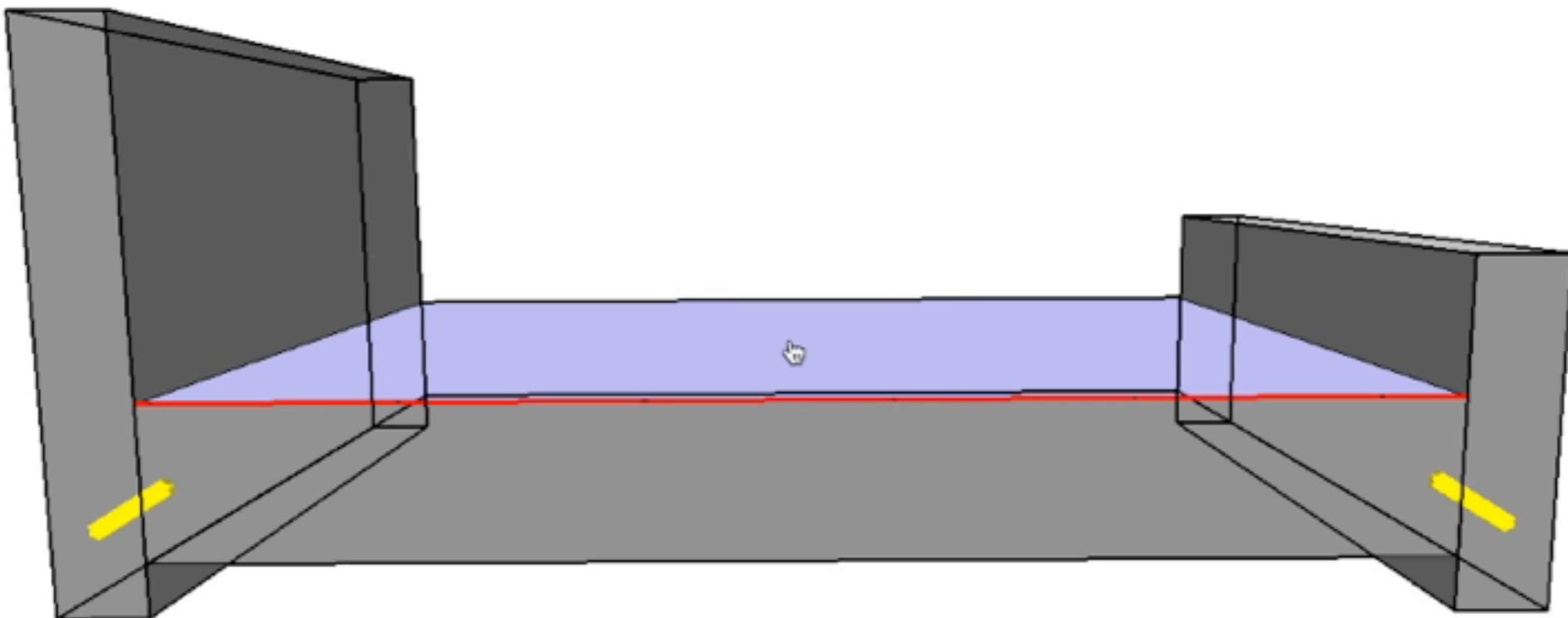
# Proposed system



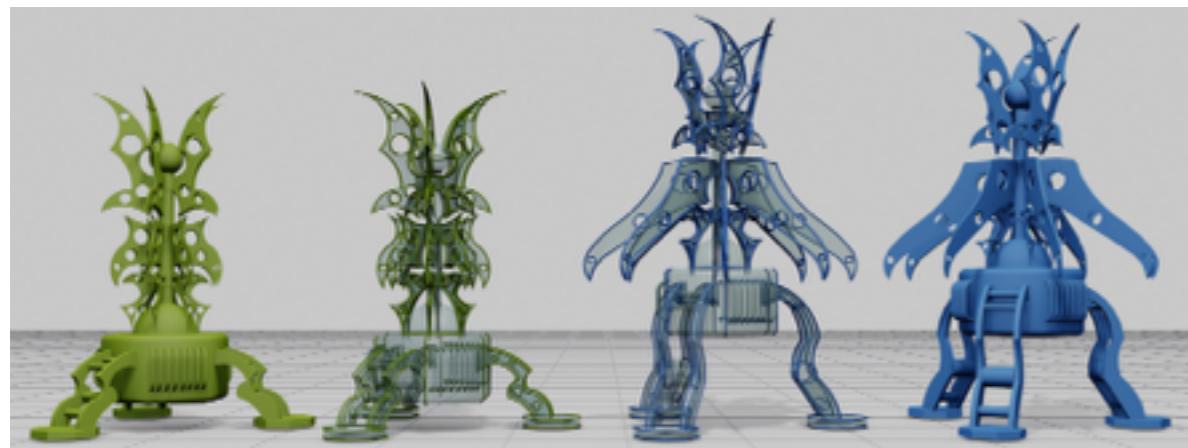
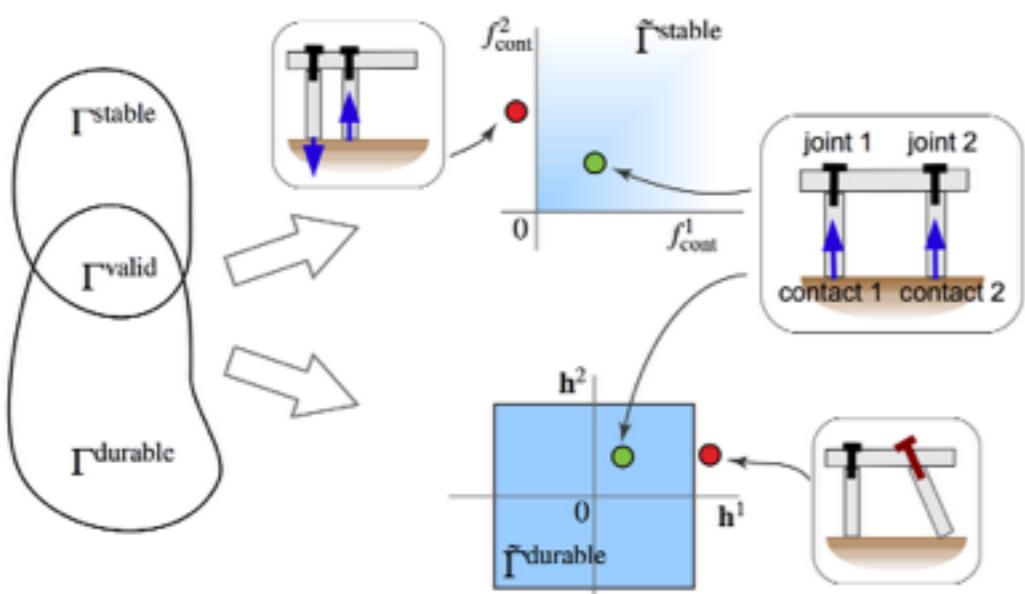
# Proposed system



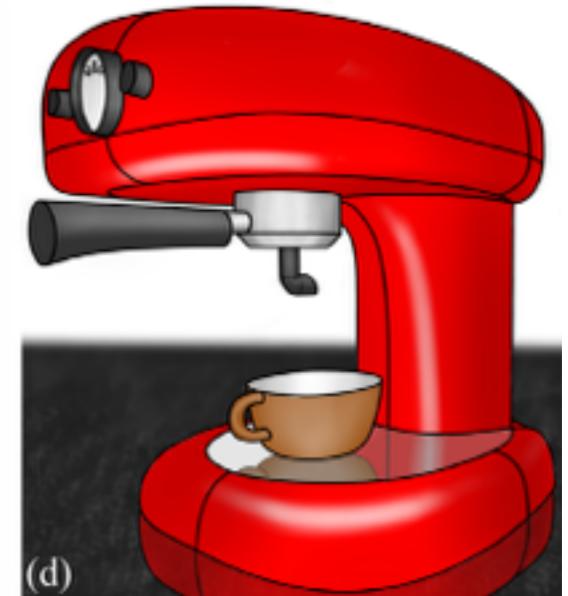
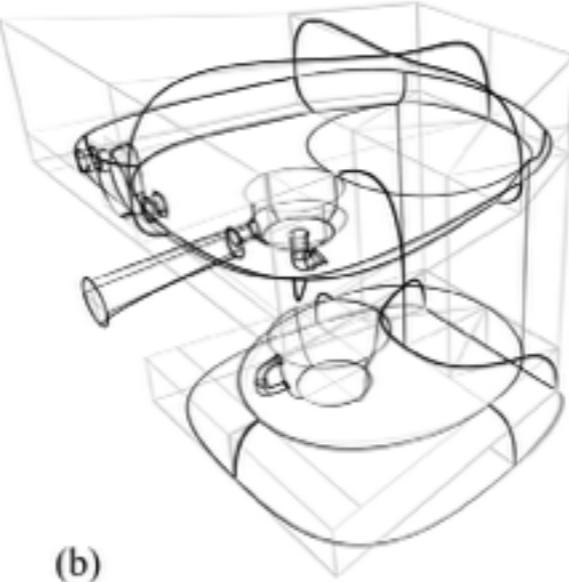
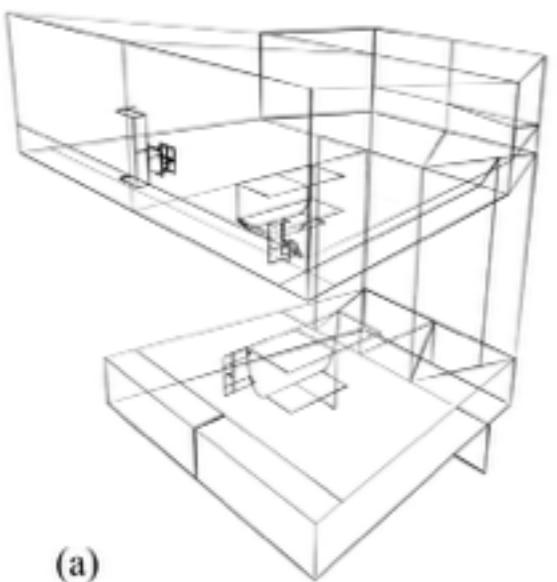
# Proposed system



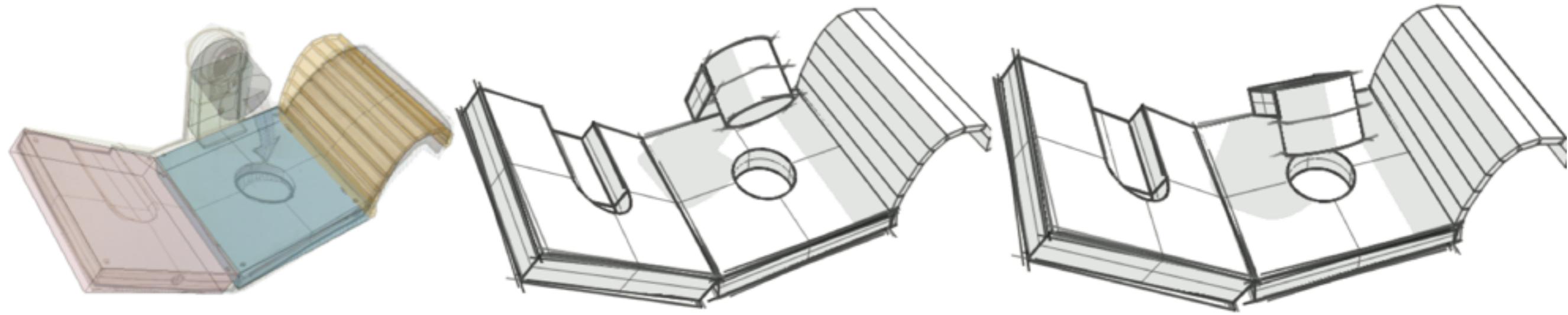
# Related work



# 1. Analysing designs



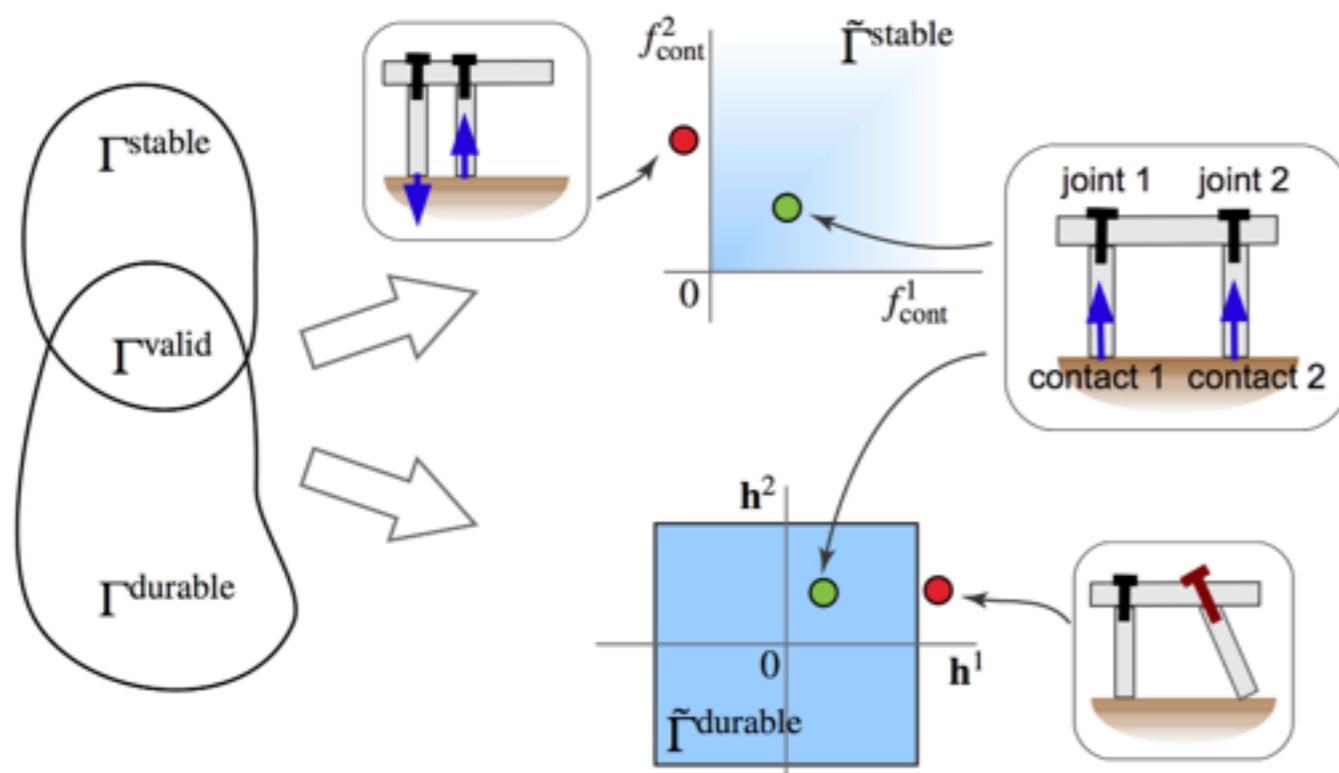
Schmidt et al. 2009



Shao et al. 2013

Bae et al. 2008, Shao et al. 2012, Xu et al. 2014

# 2. Tools for digital fabrication



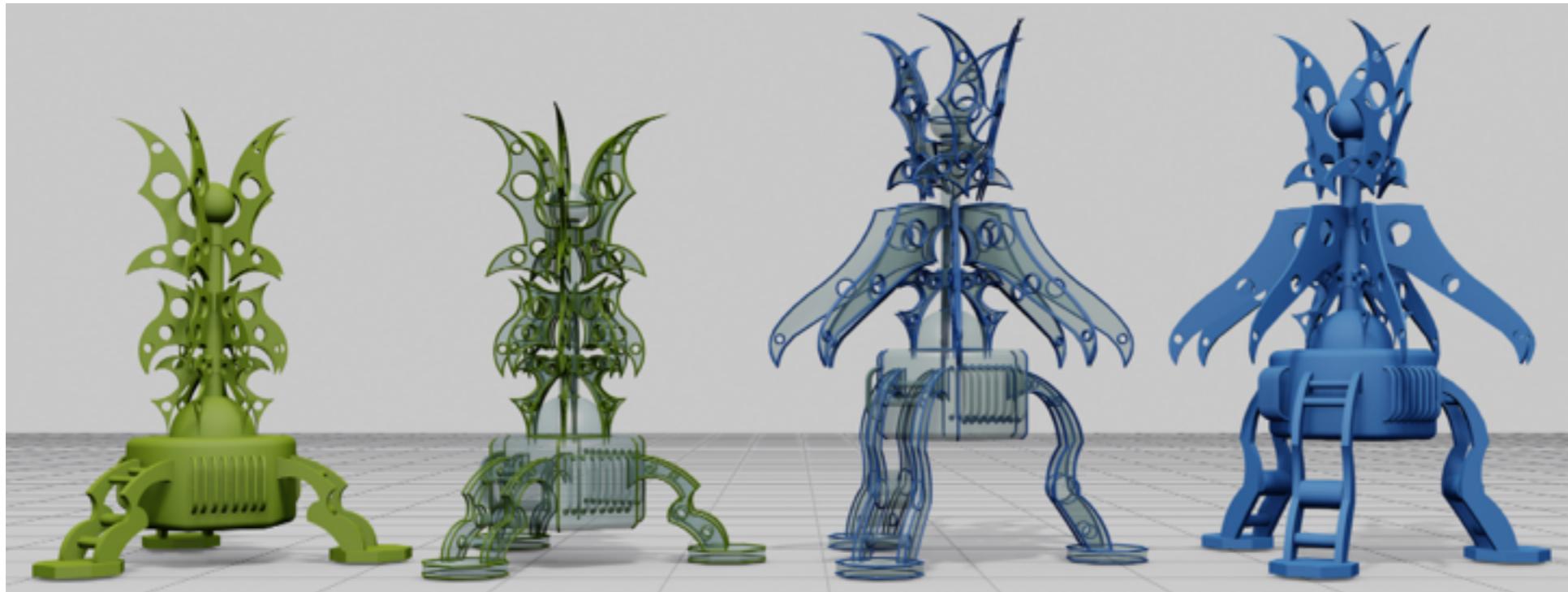
Umetani et al. 2012



Coros et al. 2013

Bächer et al. 2012, Calì et al. 2012, Stava et al. 2012, Zhu et al. 2012,  
Ceylan et al. 2013, Prévost et al. 2013

# 3. Constraint-based modelling



Gal et al. 2009

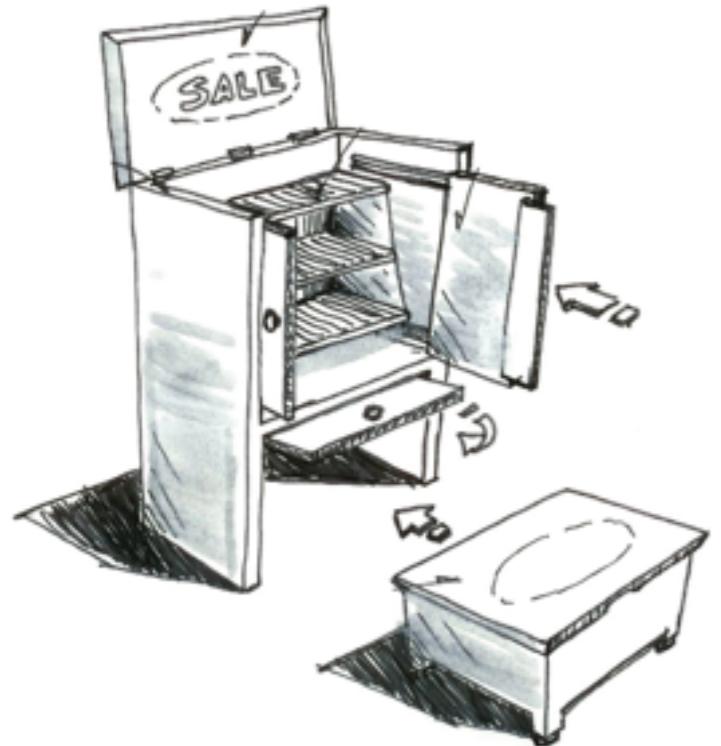


Xu et al. 2009

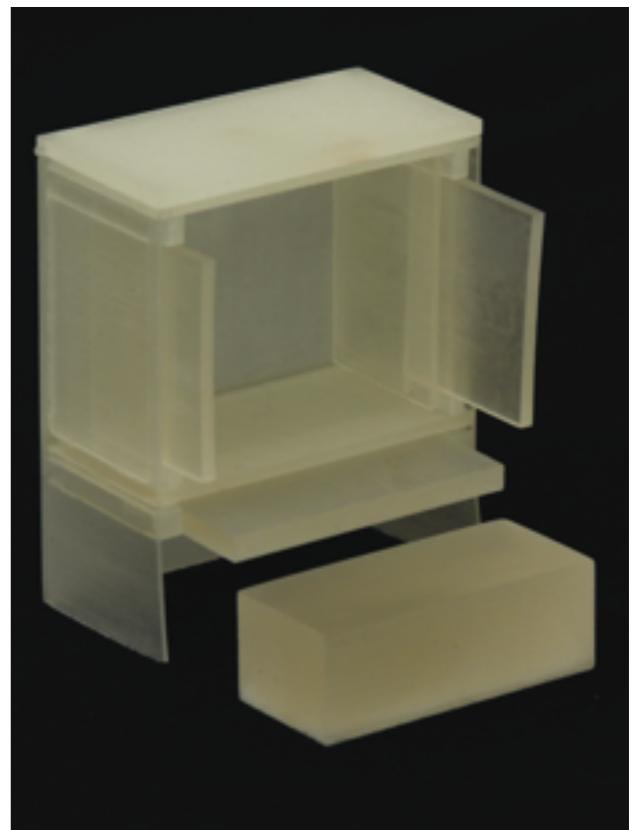
Daniel and Lucas 1997, Yvars 2008, Bokeloh et al. 2012, Zheng et al. 2012

# Overview

## Input

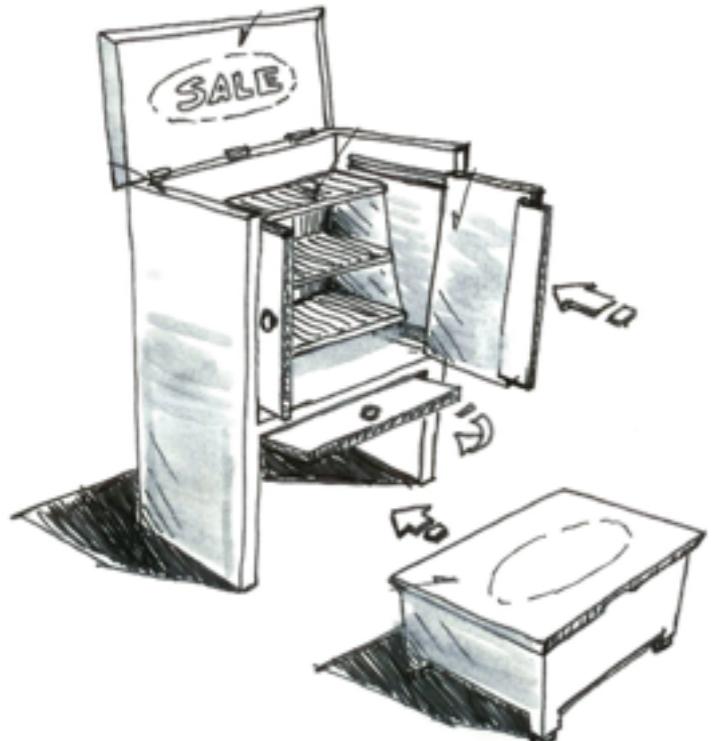


## Output

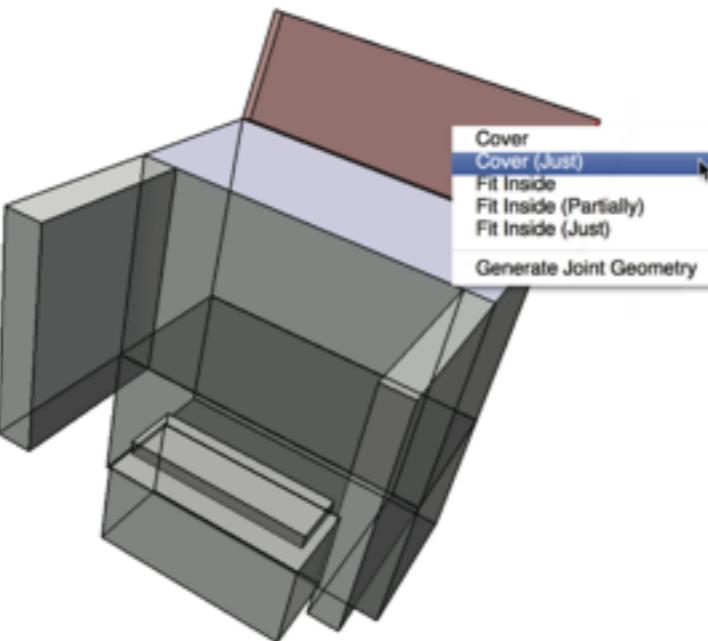


# Overview

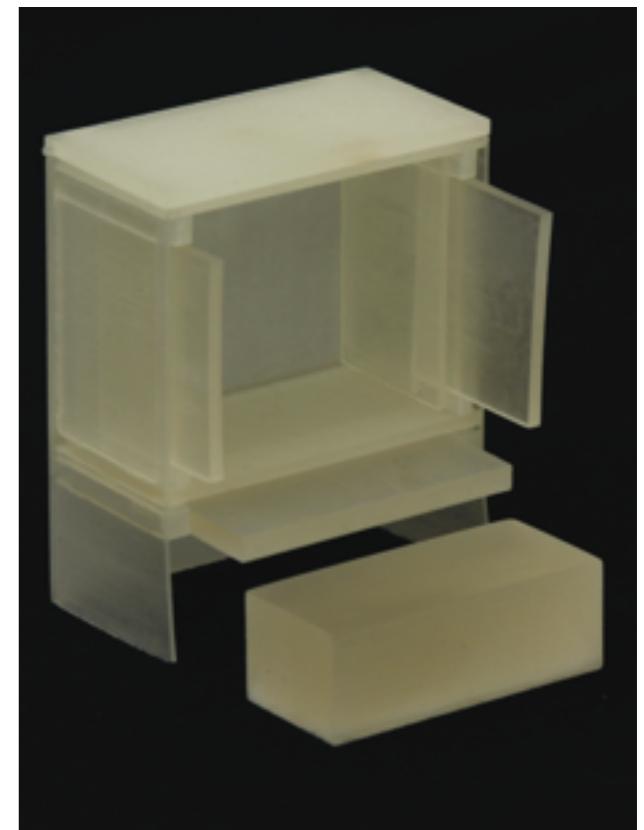
## Input



## 1. Constraints

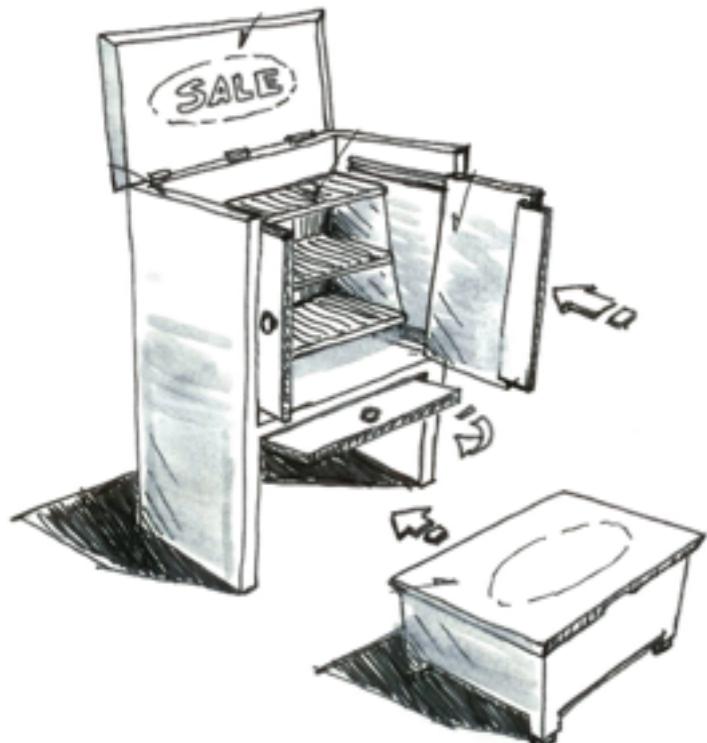


## Output

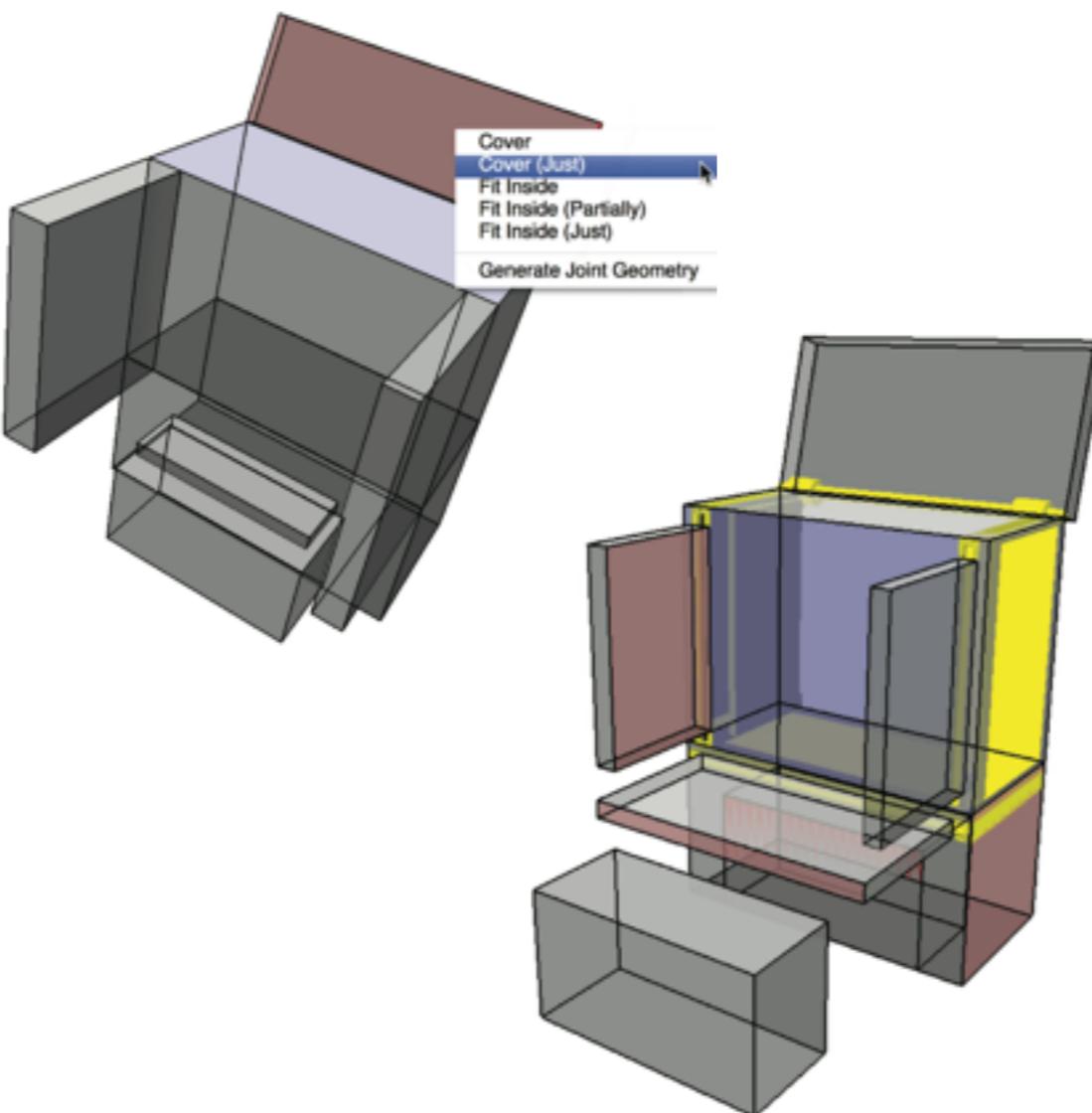


# Overview

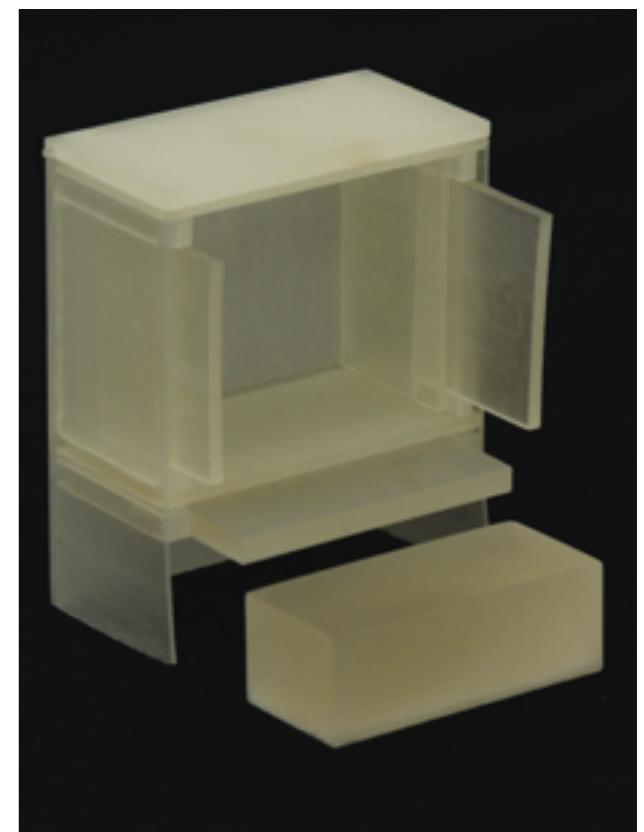
## Input



## 1. Constraints



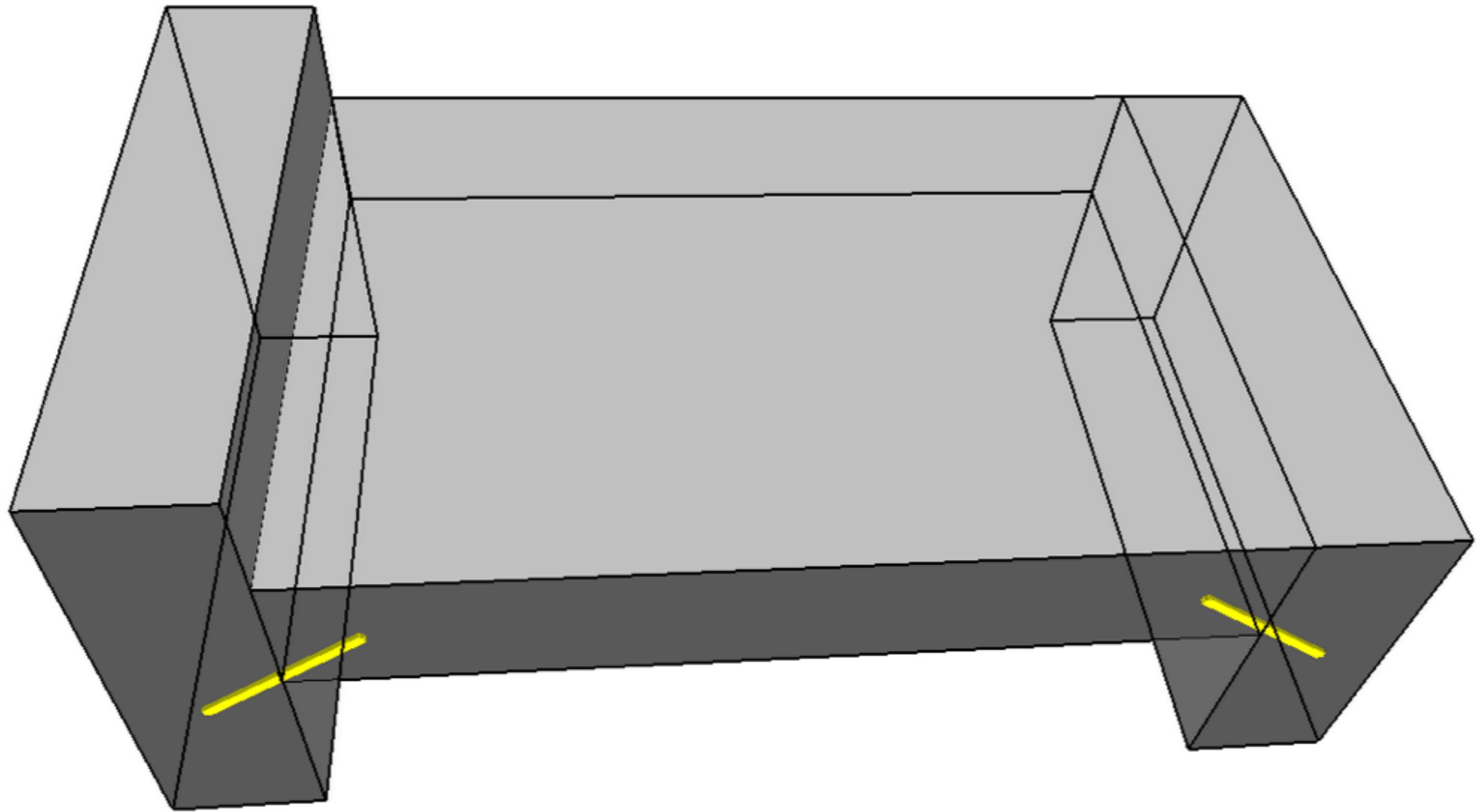
## Output



## 2. Optimisation

# Parts

## Axis-aligned cuboids



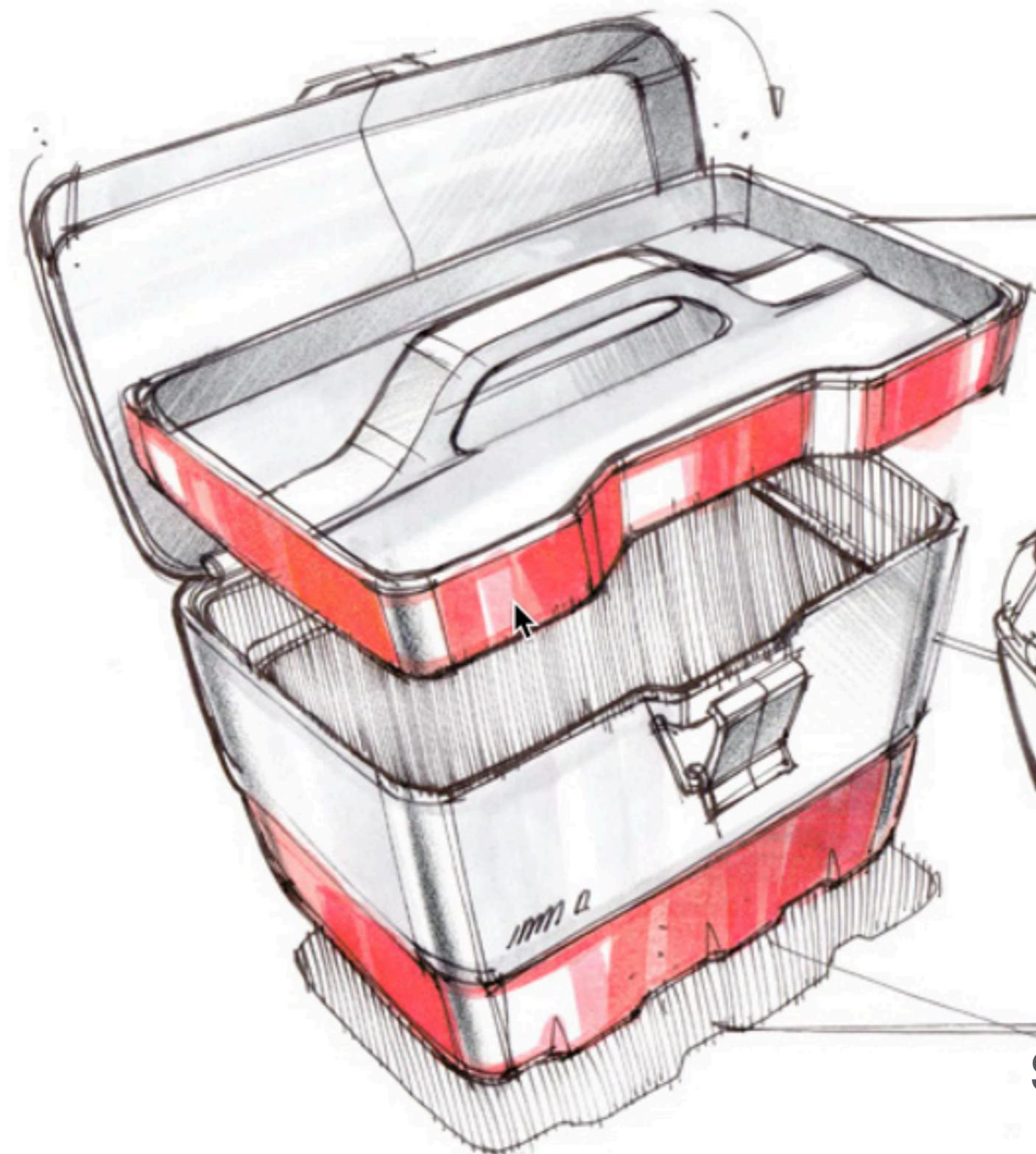
# Generating parts



# Generating parts



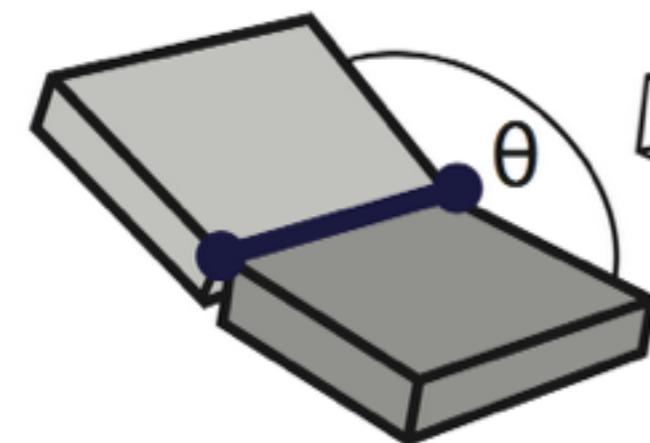
# Generating parts



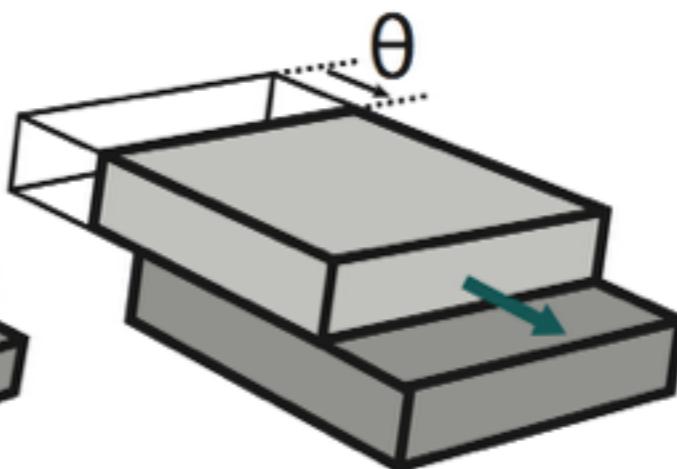
Shao et al. 2013

# Joints

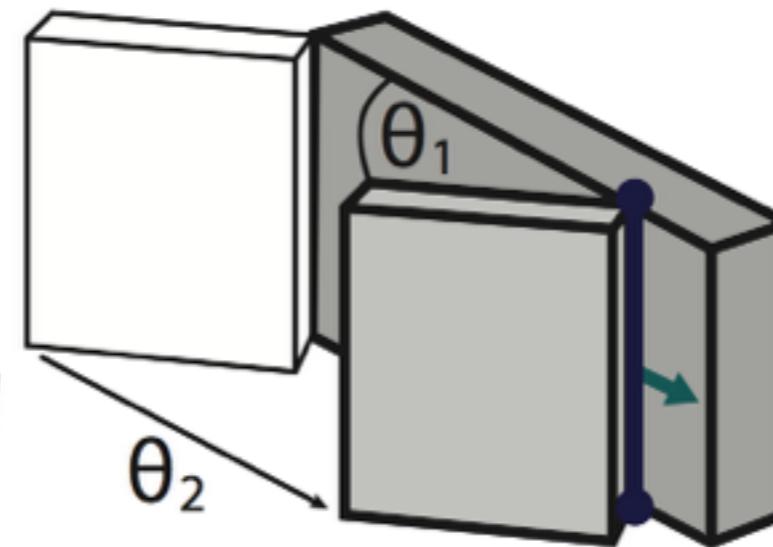
●—● rotation axis    → sliding vector    ●—● double pivot



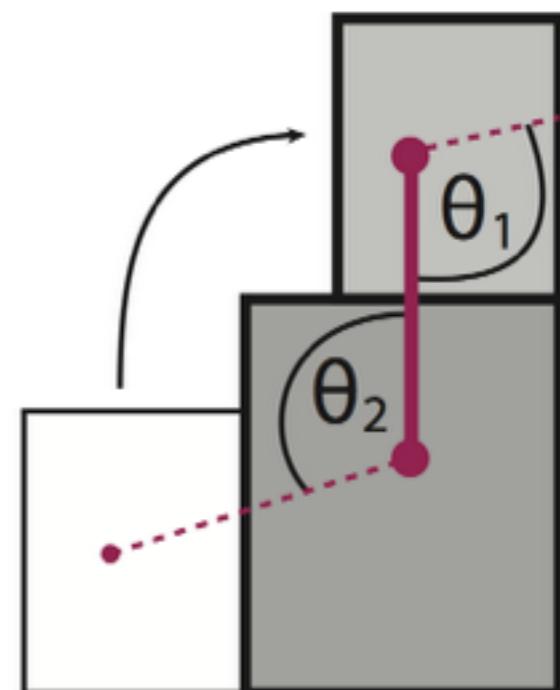
(a) hinge



(b) sliding joint



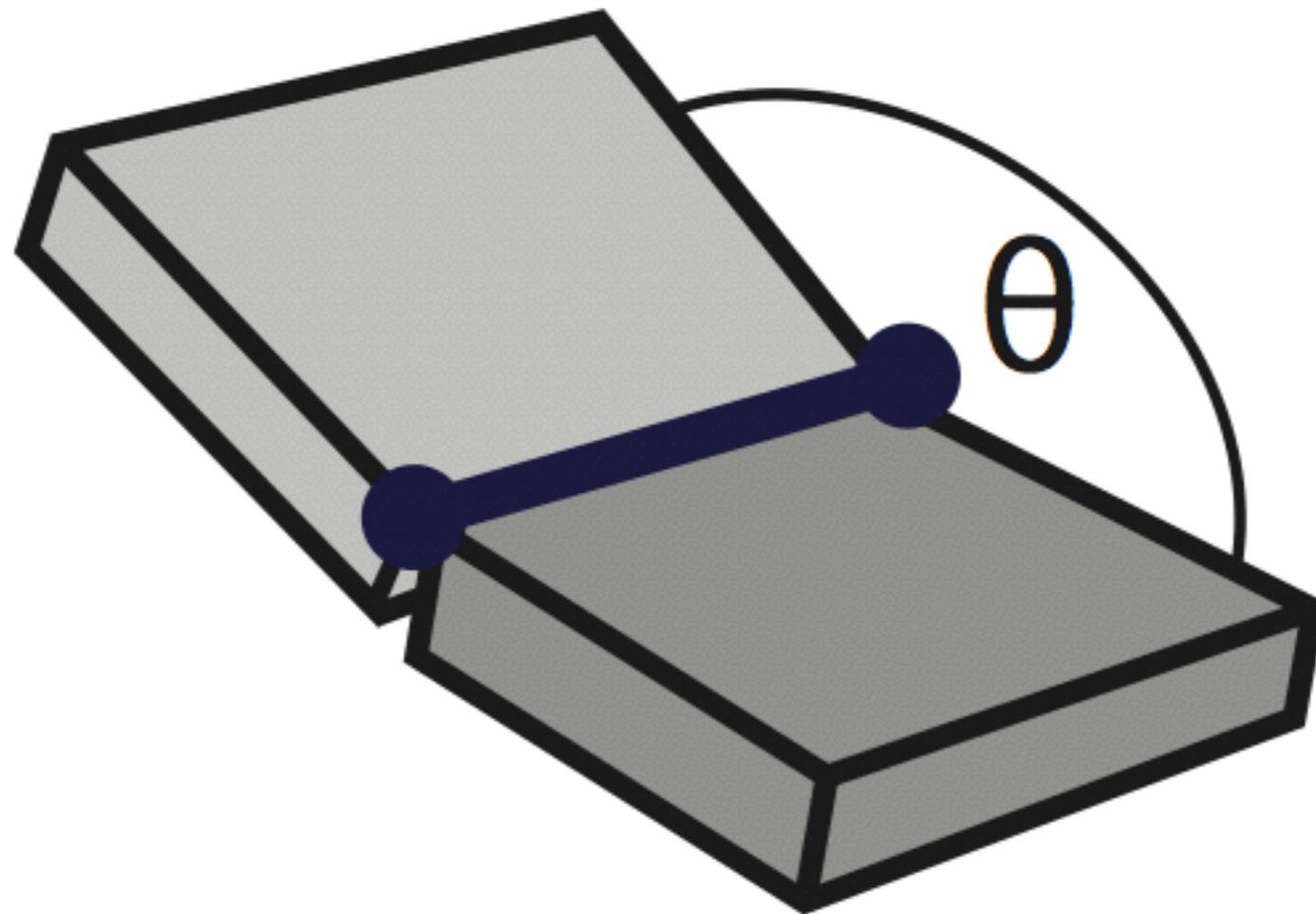
(c) sliding hinge



(d) double pivot

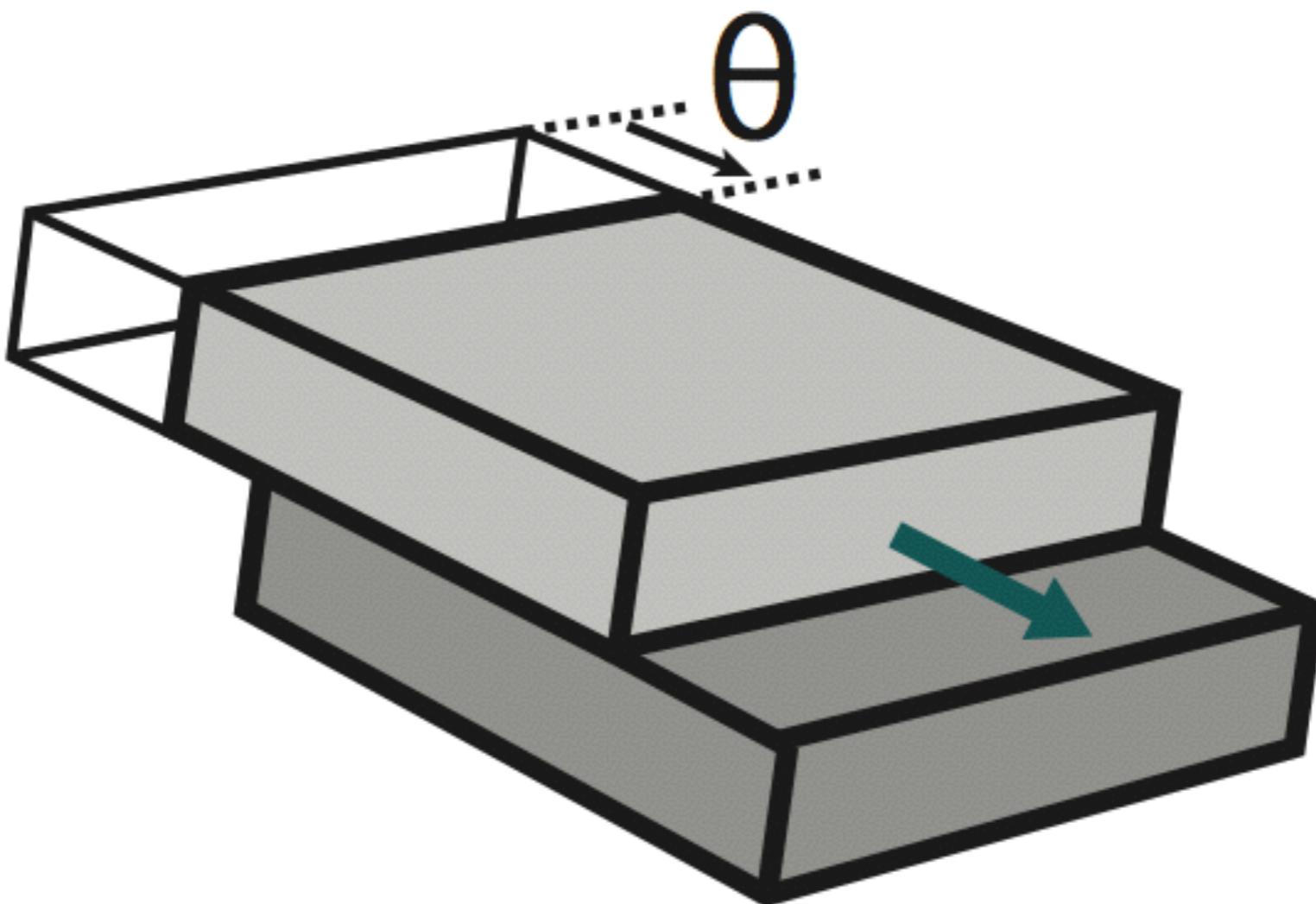
# 1. Hinge

rotation axis



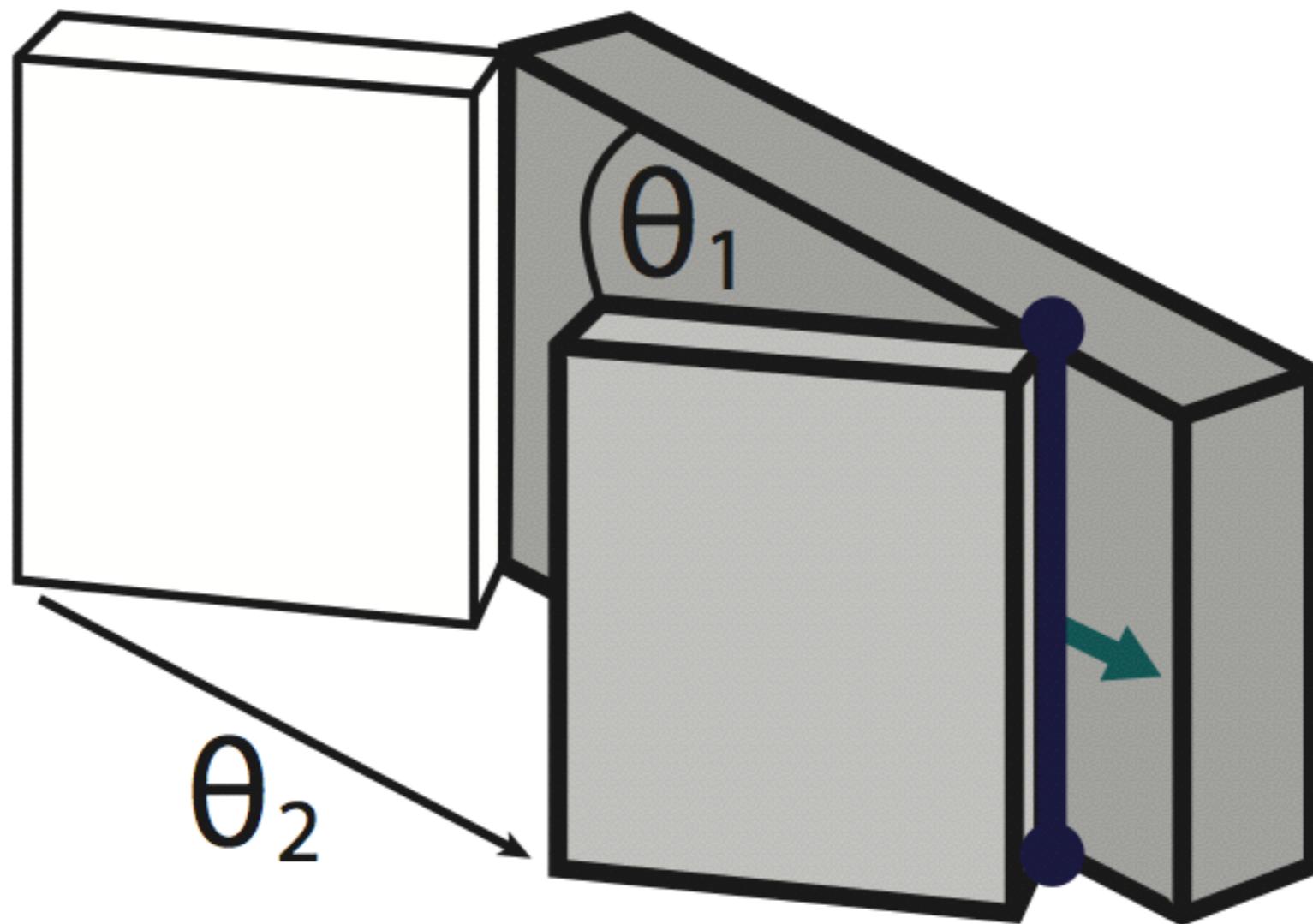
## 2. Sliding joint

→ sliding vector



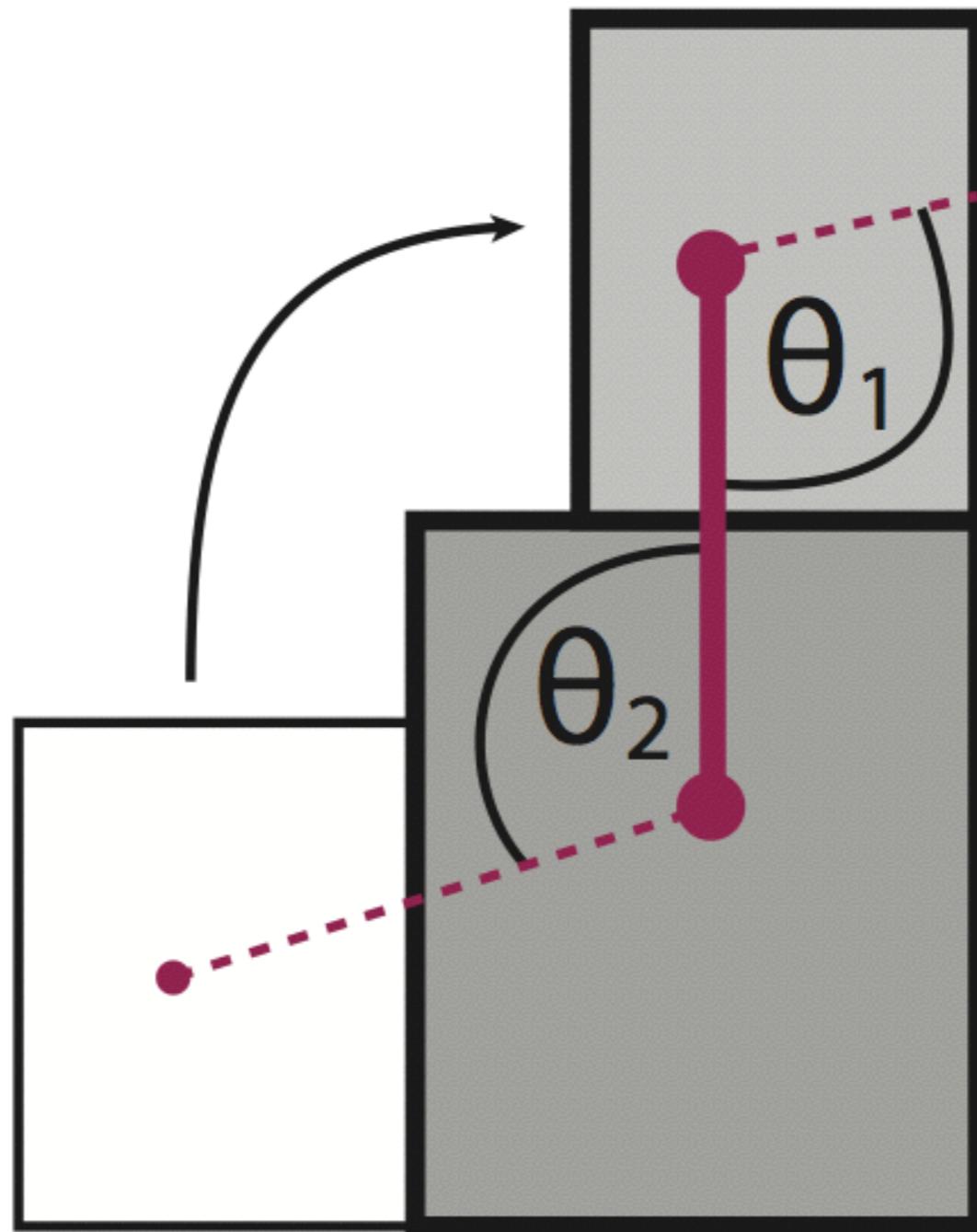
### 3. Sliding hinge

— rotation axis → sliding vector



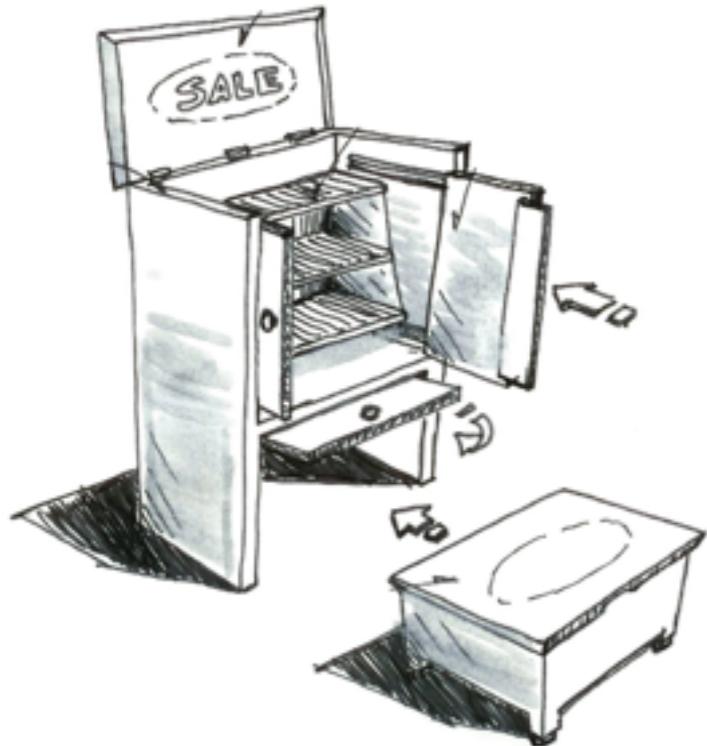
# 4. Double pivot

●—● double pivot

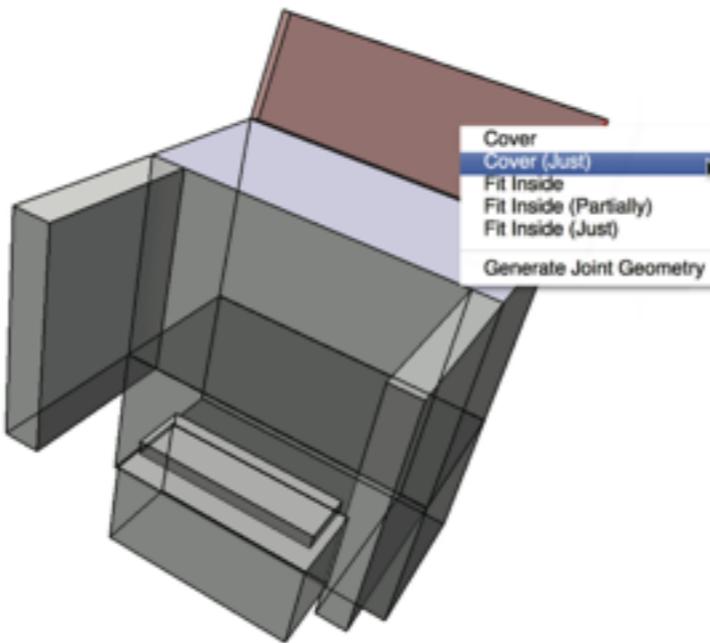


# Overview

## Input



## 1. Constraints



# Functional relationships

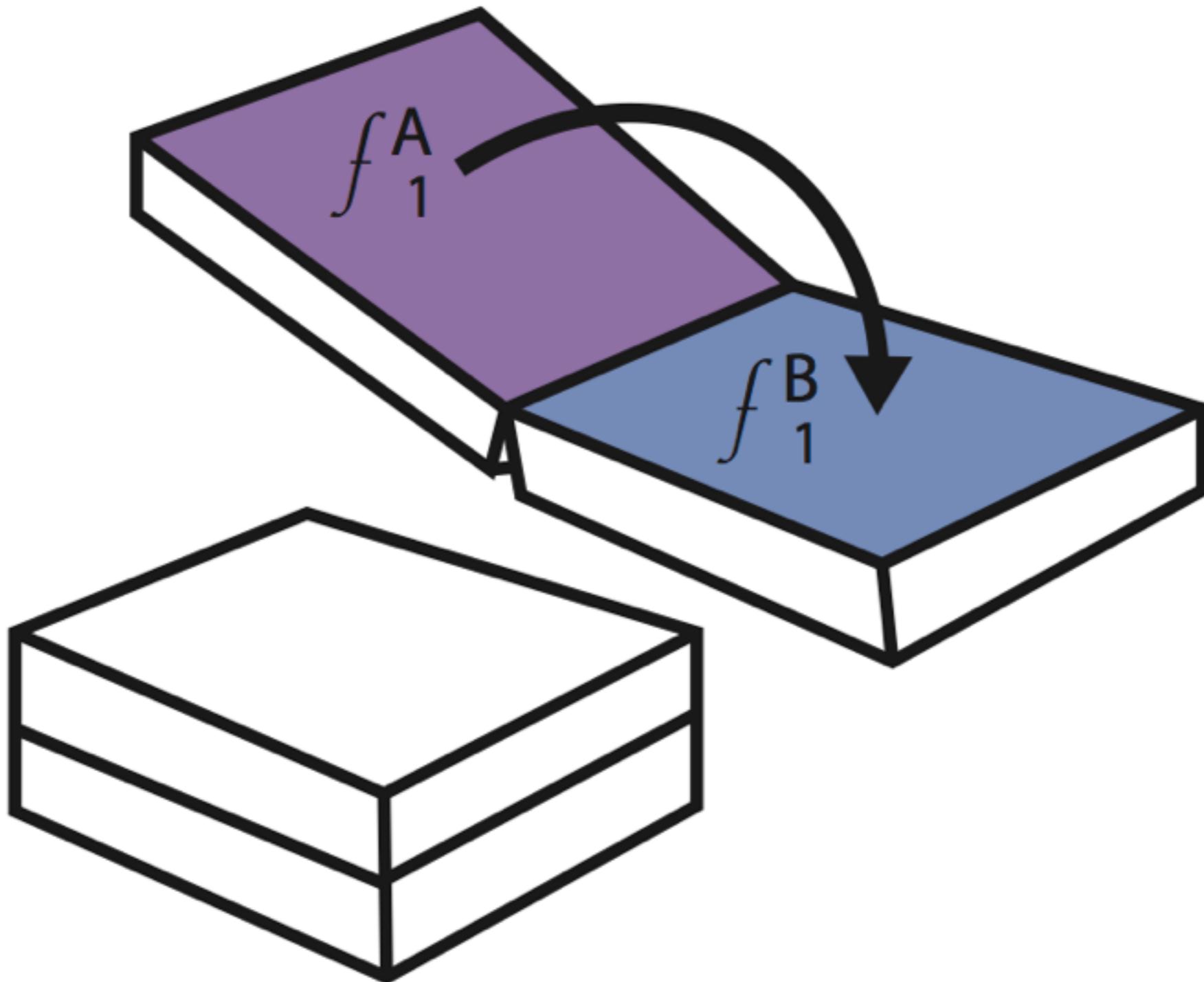
## Functional Relationships

# Functional relationships

## Functional Relationships

# 1. Cover

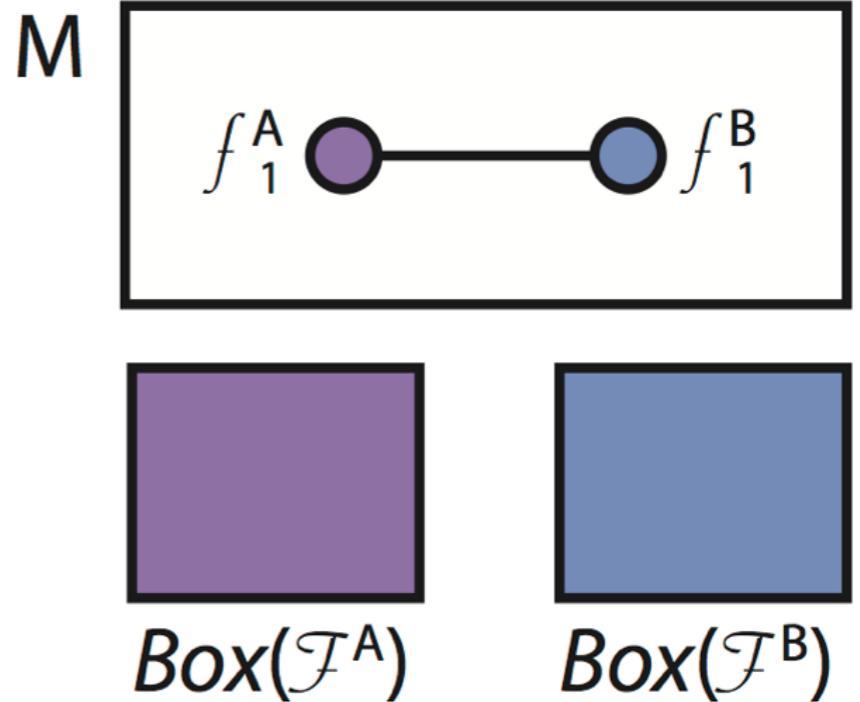
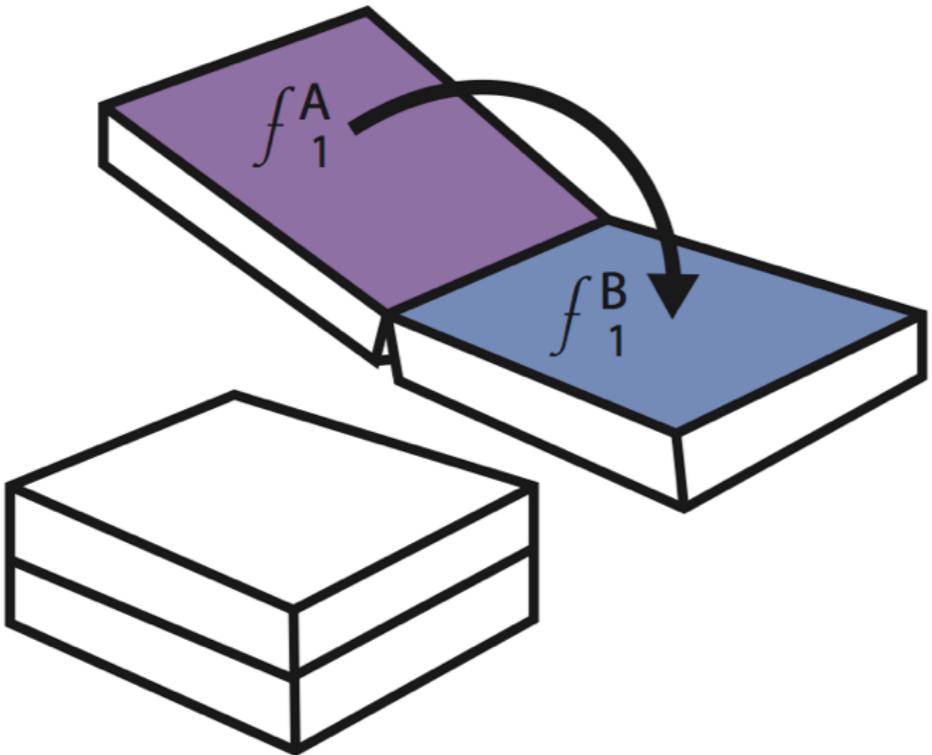
■ covering face ■ covered face



# 1. Cover

covering face

covered face



$Cover(F^A, F^B, M, J, \Theta)$

$F^A$  covers  $F^B$

$M$  : a corresponding faces graph

$J(\Theta)$  : the set of joints and parameters

$$Box(F^A)_l \leq Box(F^B)_l$$

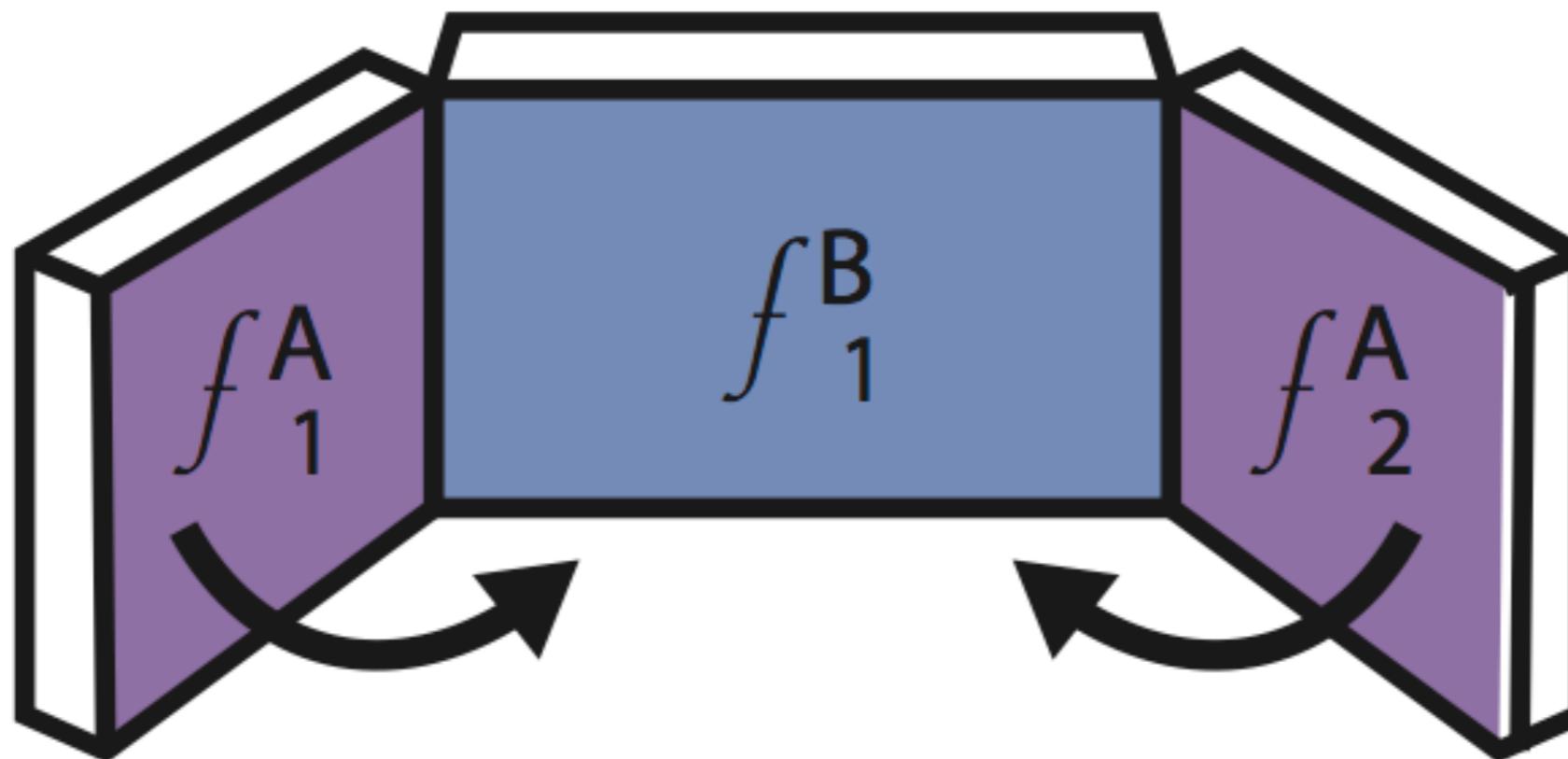
$$Box(F^A)_r \geq Box(F^B)_r$$

$$Box(F^A)_b \leq Box(F^B)_b$$

$$Box(F^A)_t \geq Box(F^B)_t$$

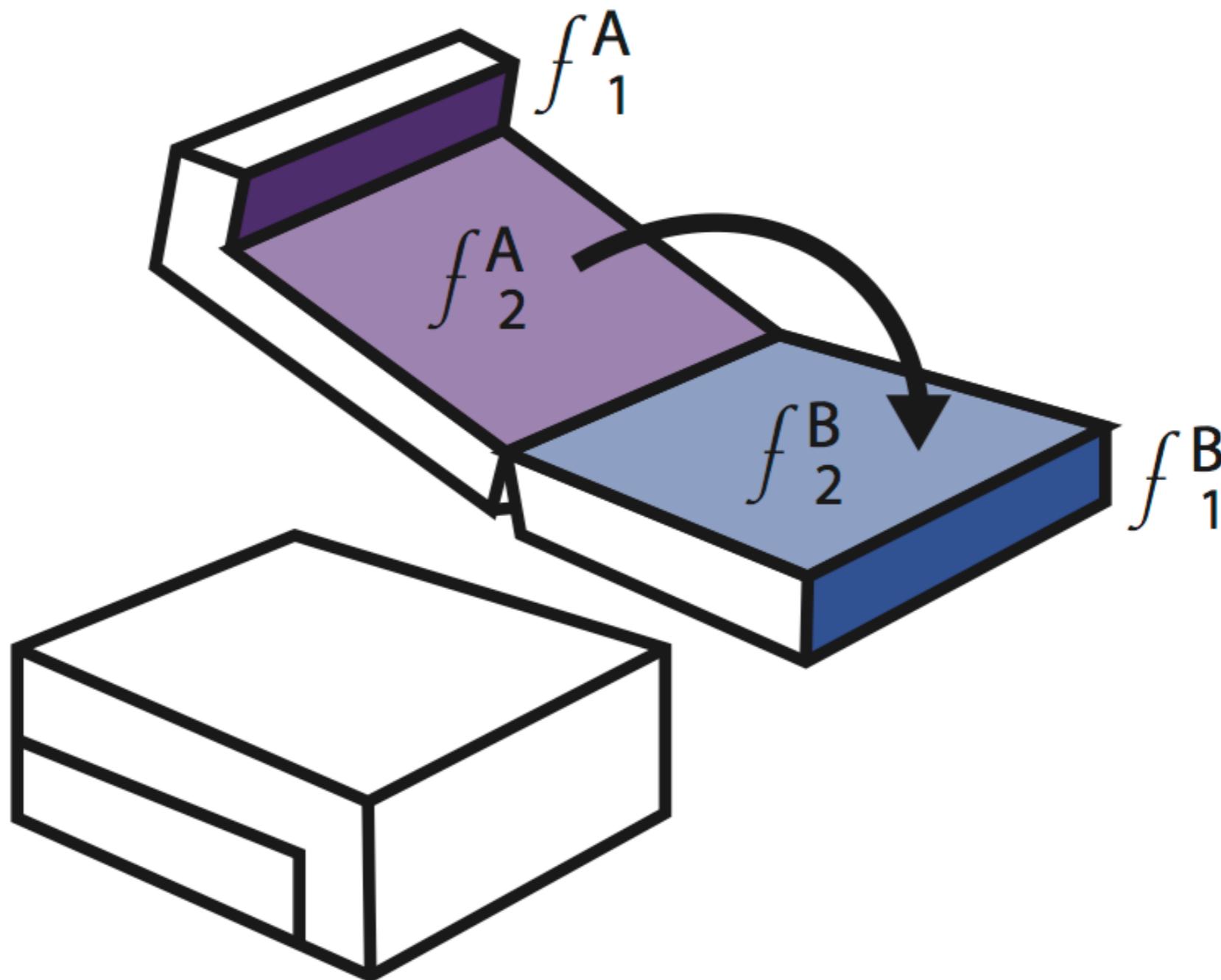
# 1. Cover

■ covering face ■ covered face

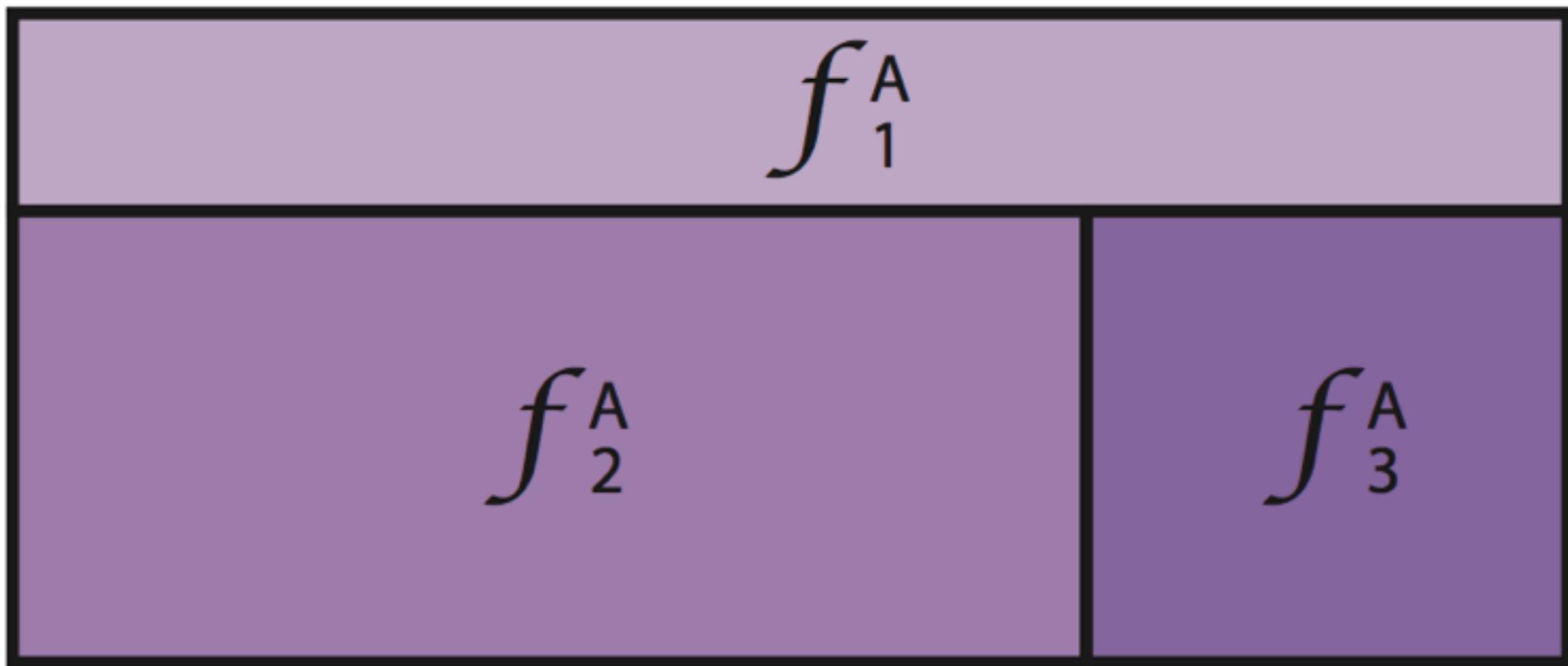


# 1. Cover

■ covering face   ■ covered face



# 1. Cover

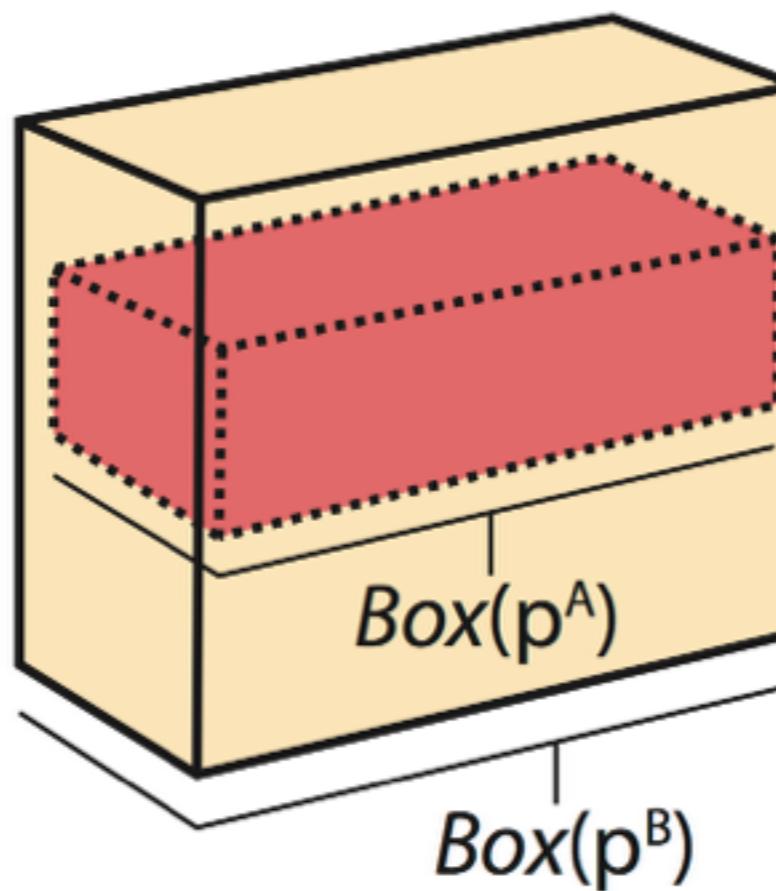
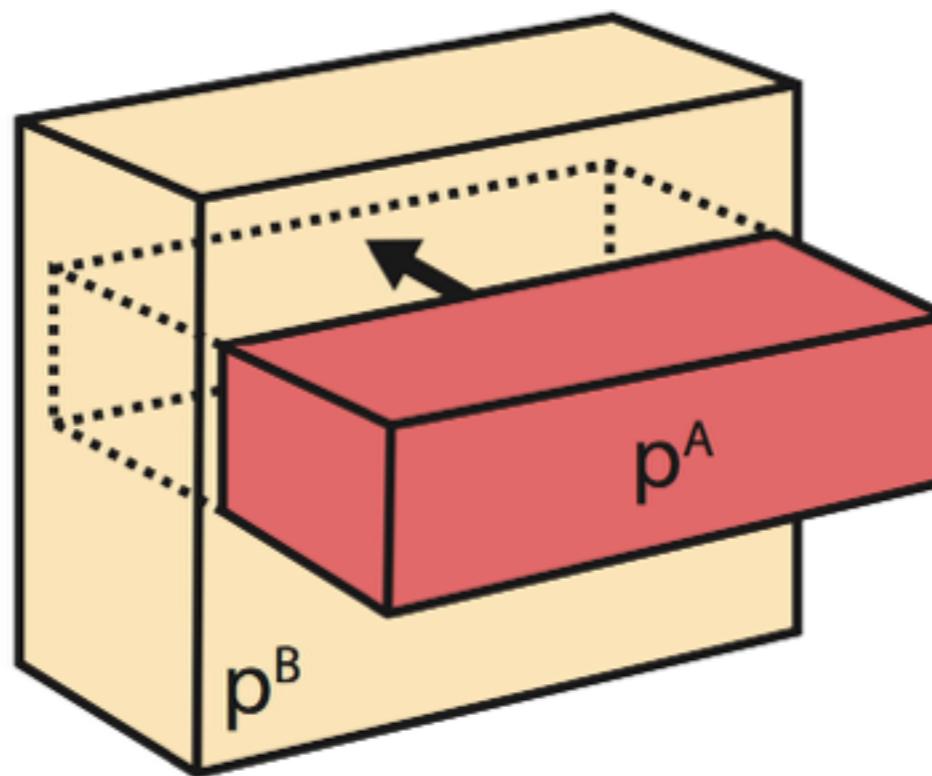


$$Box(f_1^A)_b = Box(f_2^A)_t$$

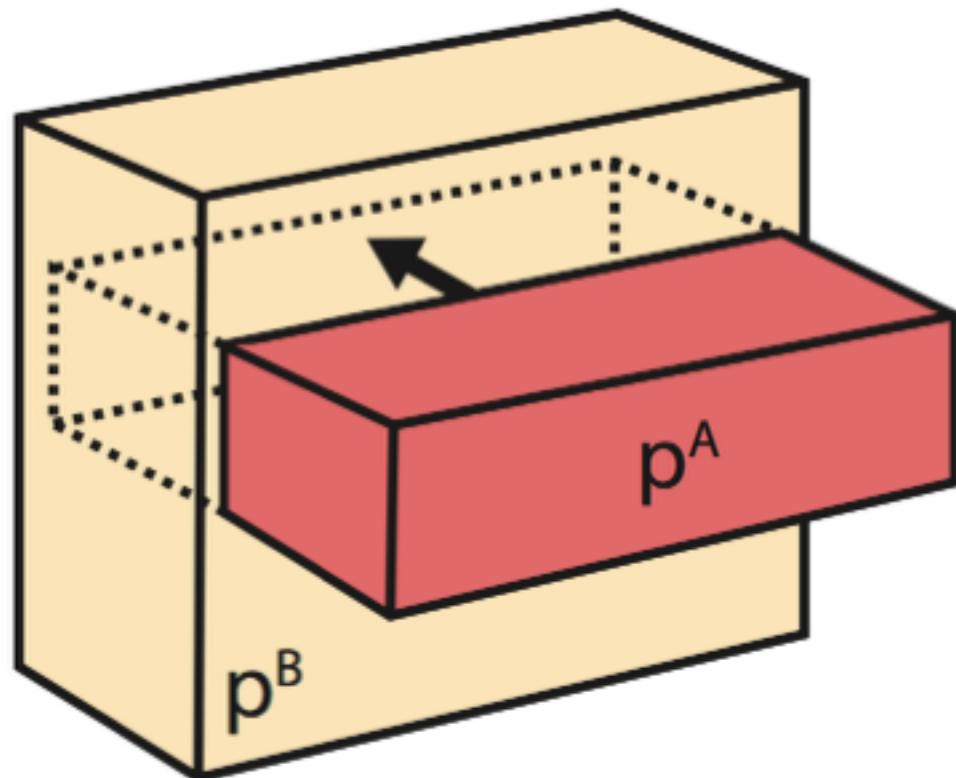
$$Box(f_1^A)_b = Box(f_3^A)_t$$

$$Box(f_2^A)_r = Box(f_3^A)_l$$

## 2. Fit inside



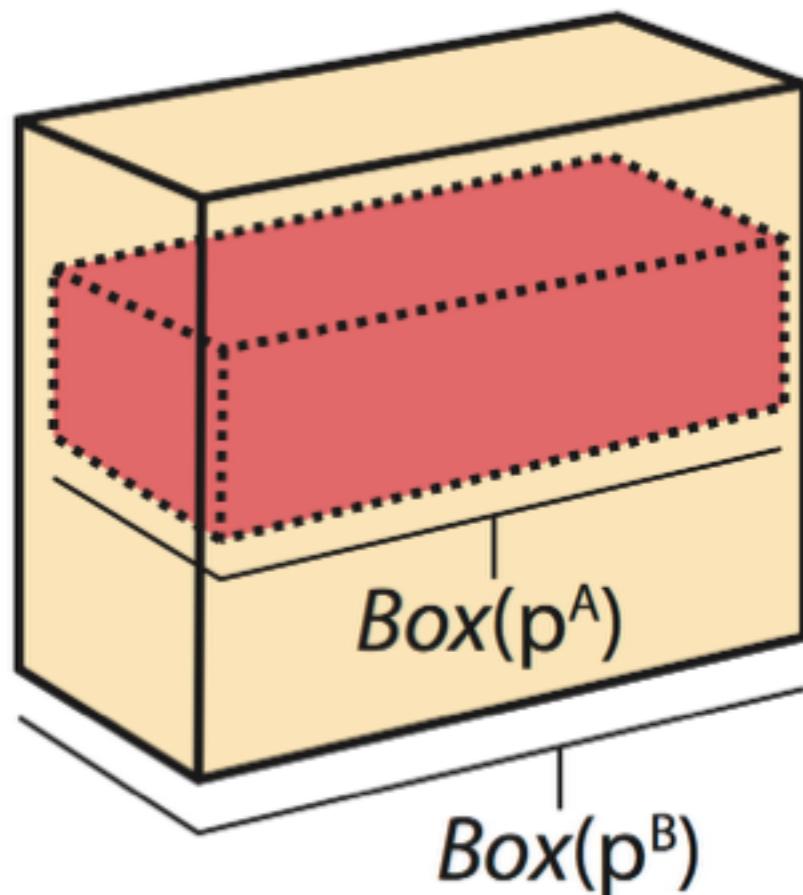
## 2. Fit inside



$Fit(P^A, p^B, J, \Theta)$

$P^A$  fit inside  $p^B$

$J(\Theta)$ : the set of joints and parameters



$$Box(P^A)_l \geq Box(p^B)_l$$

$$Box(P^A)_r \leq Box(p^B)_r$$

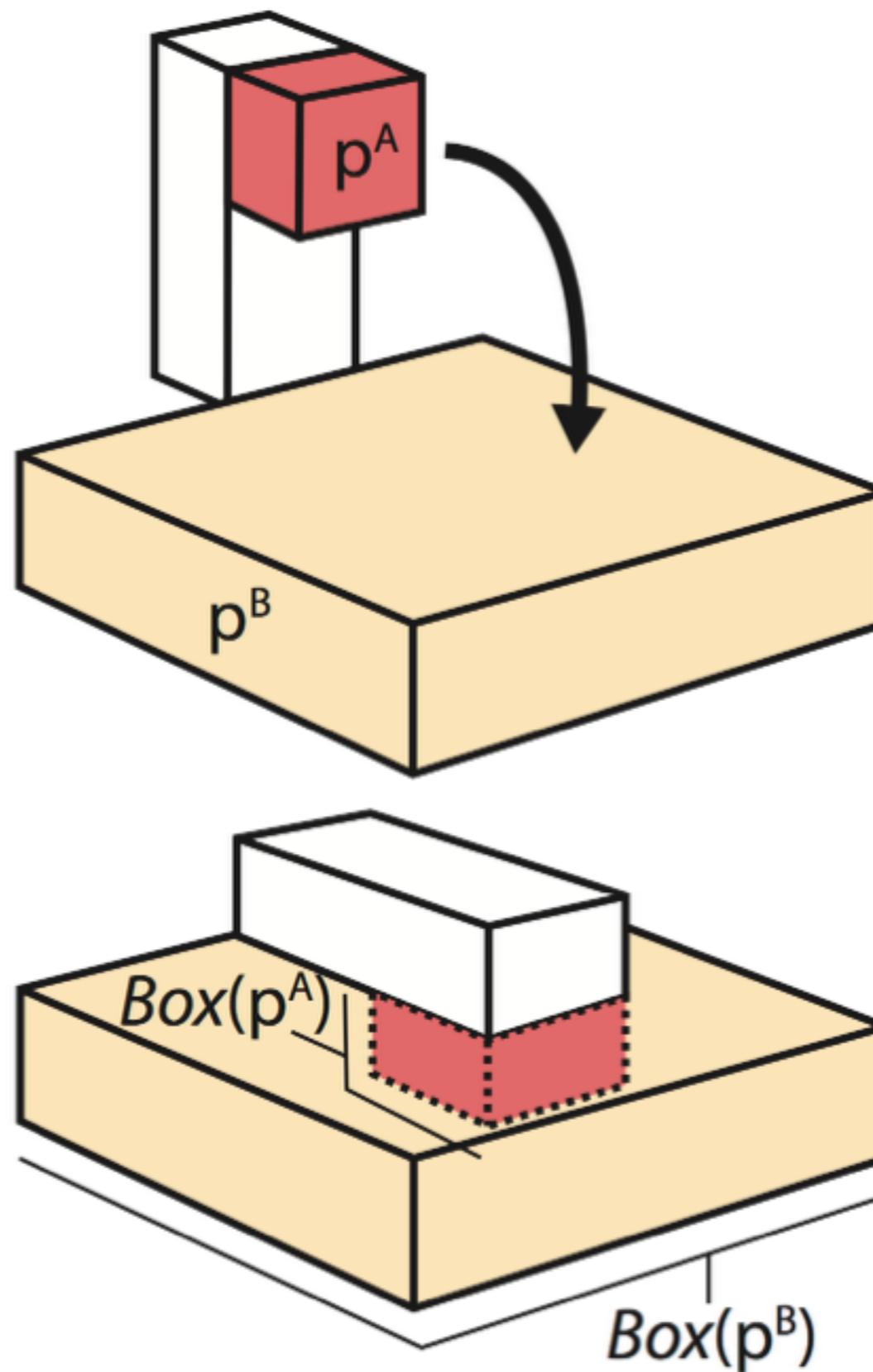
$$Box(P^A)_b \geq Box(p^B)_b$$

$$Box(P^A)_t \leq Box(p^B)_t$$

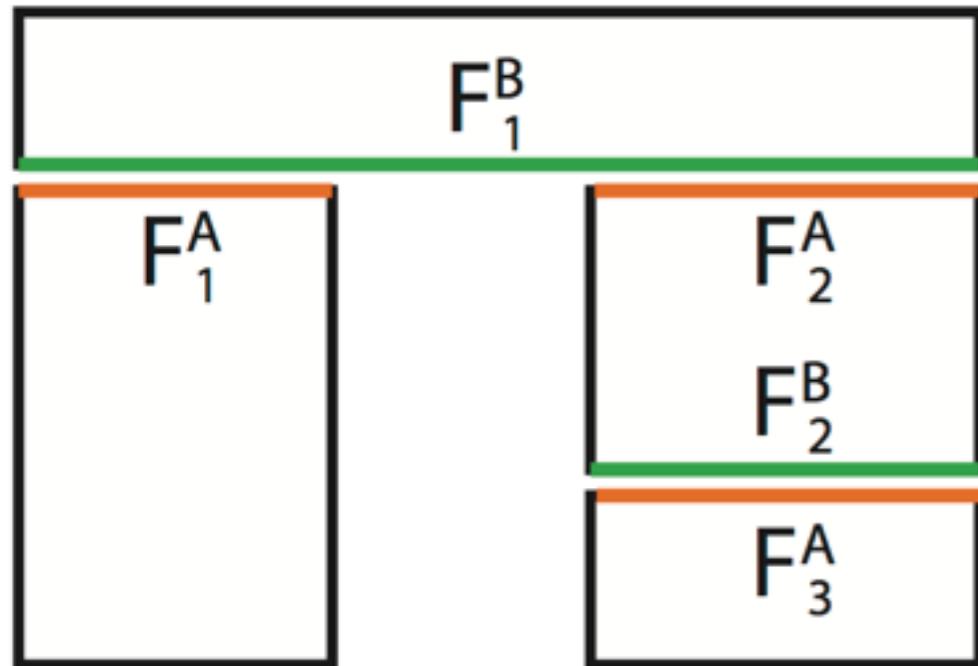
$$Box(P^A)_n \geq Box(p^B)_n$$

$$Box(P^A)_f \leq Box(p^B)_f$$

## 2. Fit inside



# 3. Support



$Support(F^A, F^B, M, J, \Theta)$

$F^A, F^B$  : the set of supporting / supported faces

$M$  : a corresponding faces graph

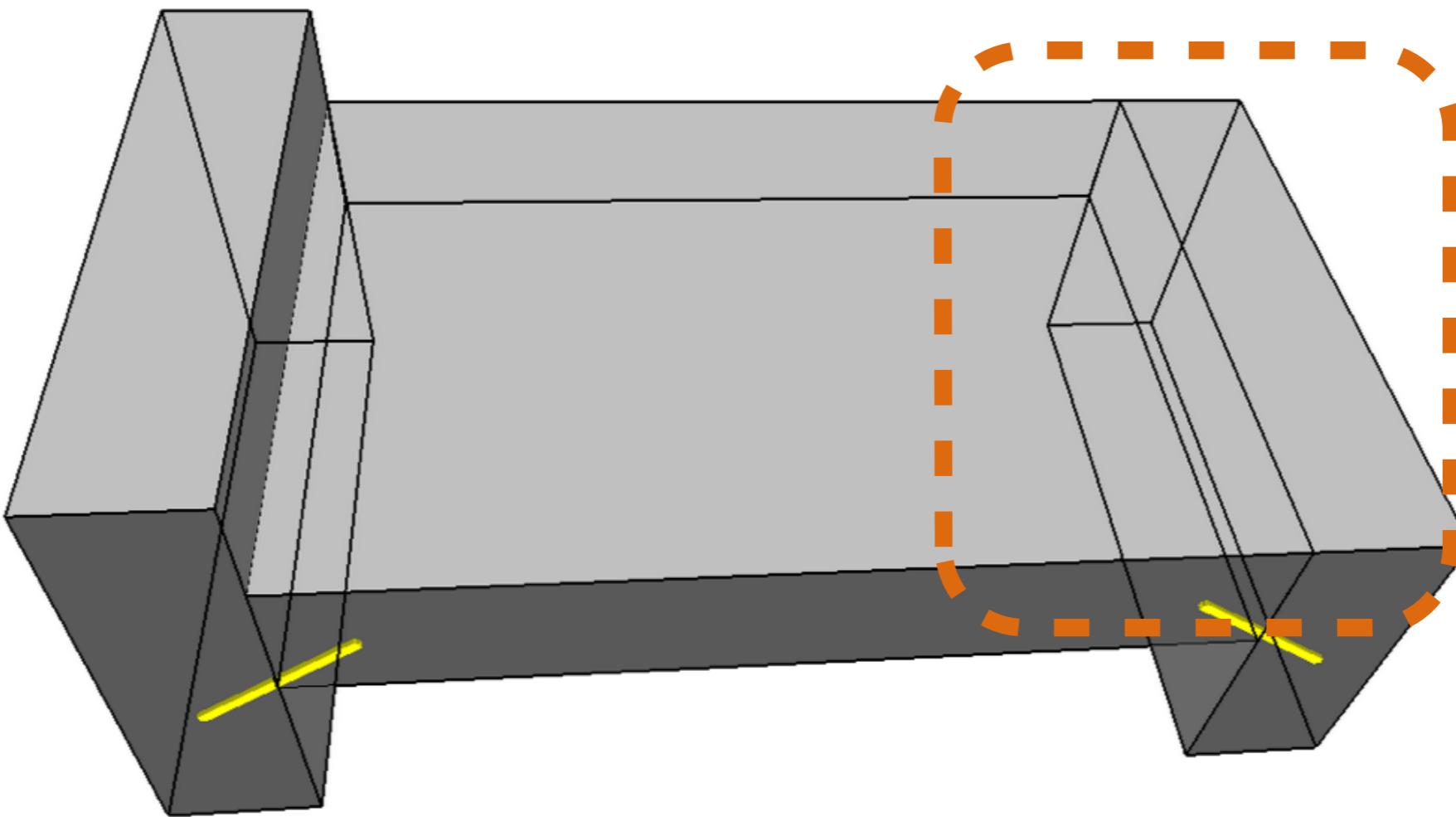
$J(\Theta)$  : the set of joints and parameters

$$f_l^A < f_r^B \quad f_t^A < f_b^B$$

$$f_r^A > f_l^B \quad f_b^A > f_t^B$$

$$c_t^A = c_b^B$$

# 4. Flush

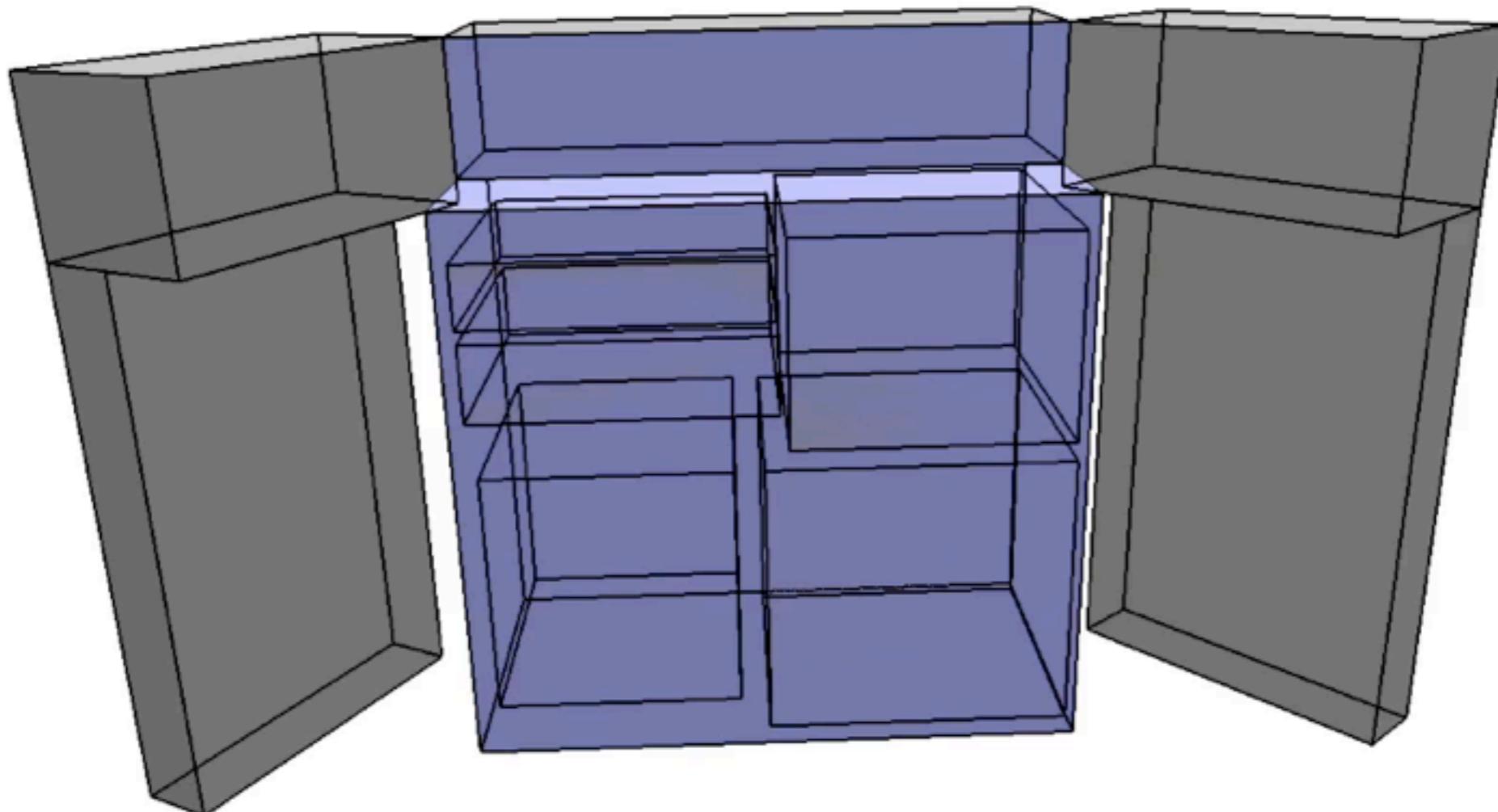


$\text{Flush}(f^A, f^B, J, \Theta)$

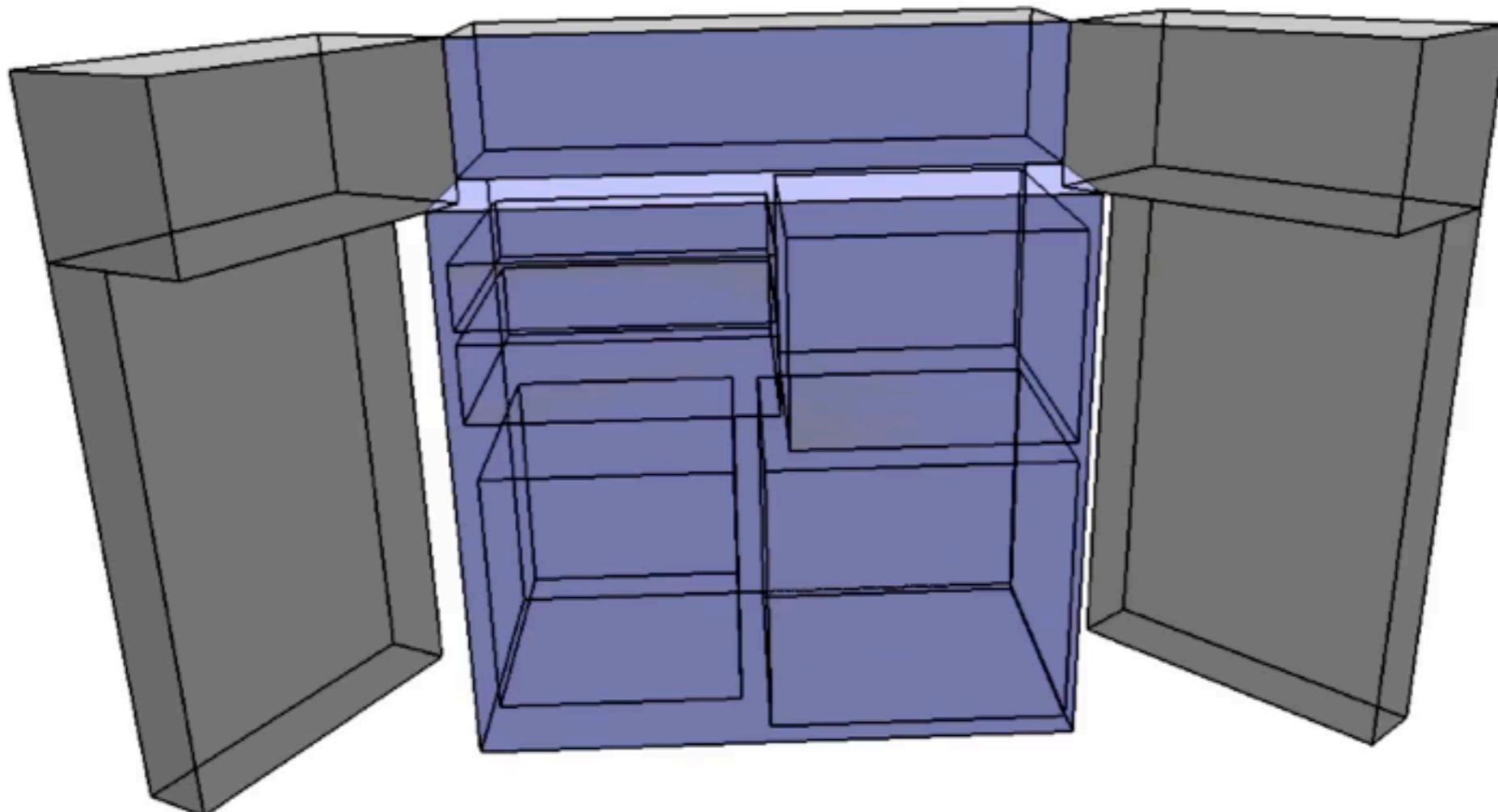
$f^A, f^B$ : the two faces that are flush

$J(\Theta)$ : the set of joints and parameters

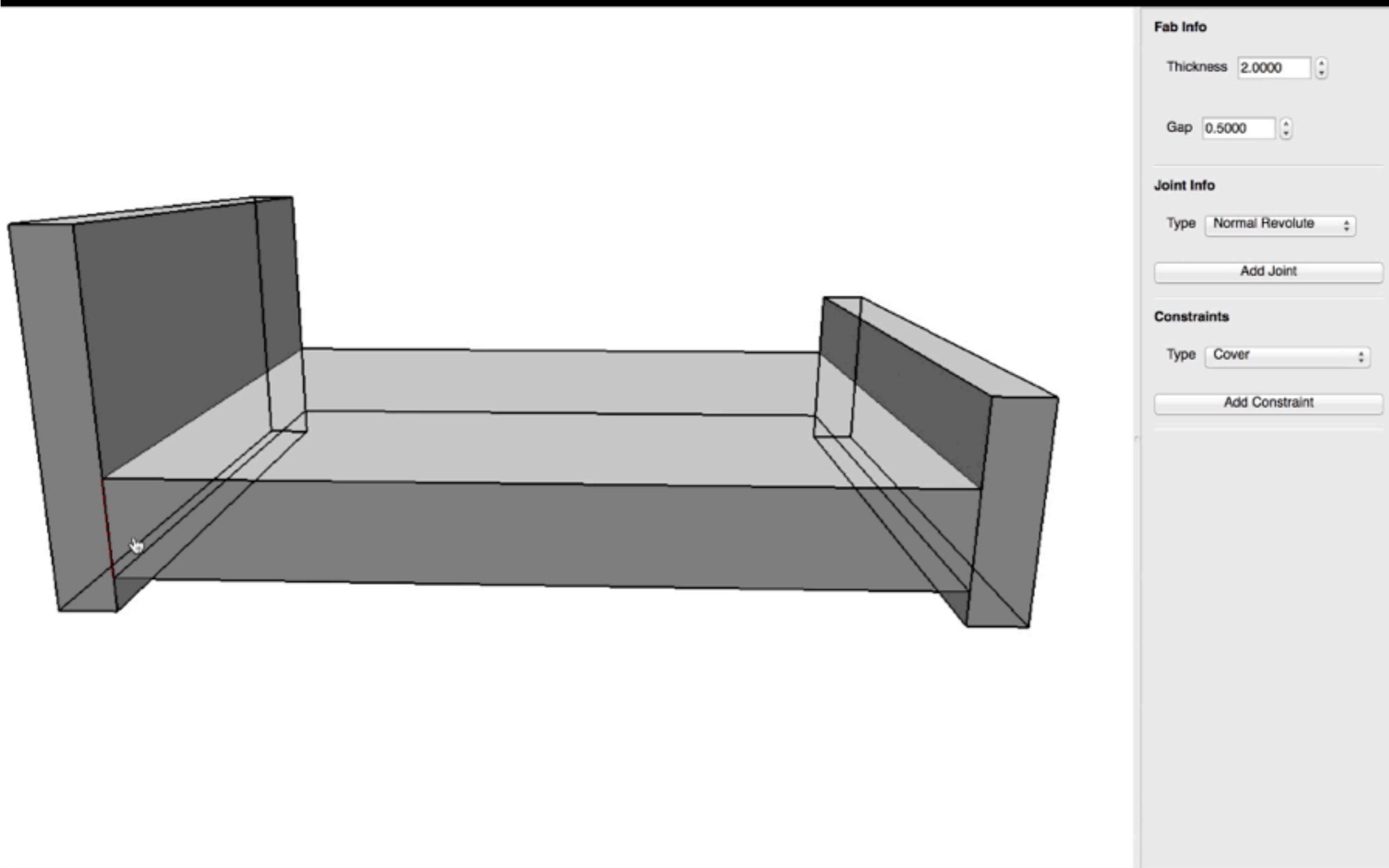
# Specifying functional relationships



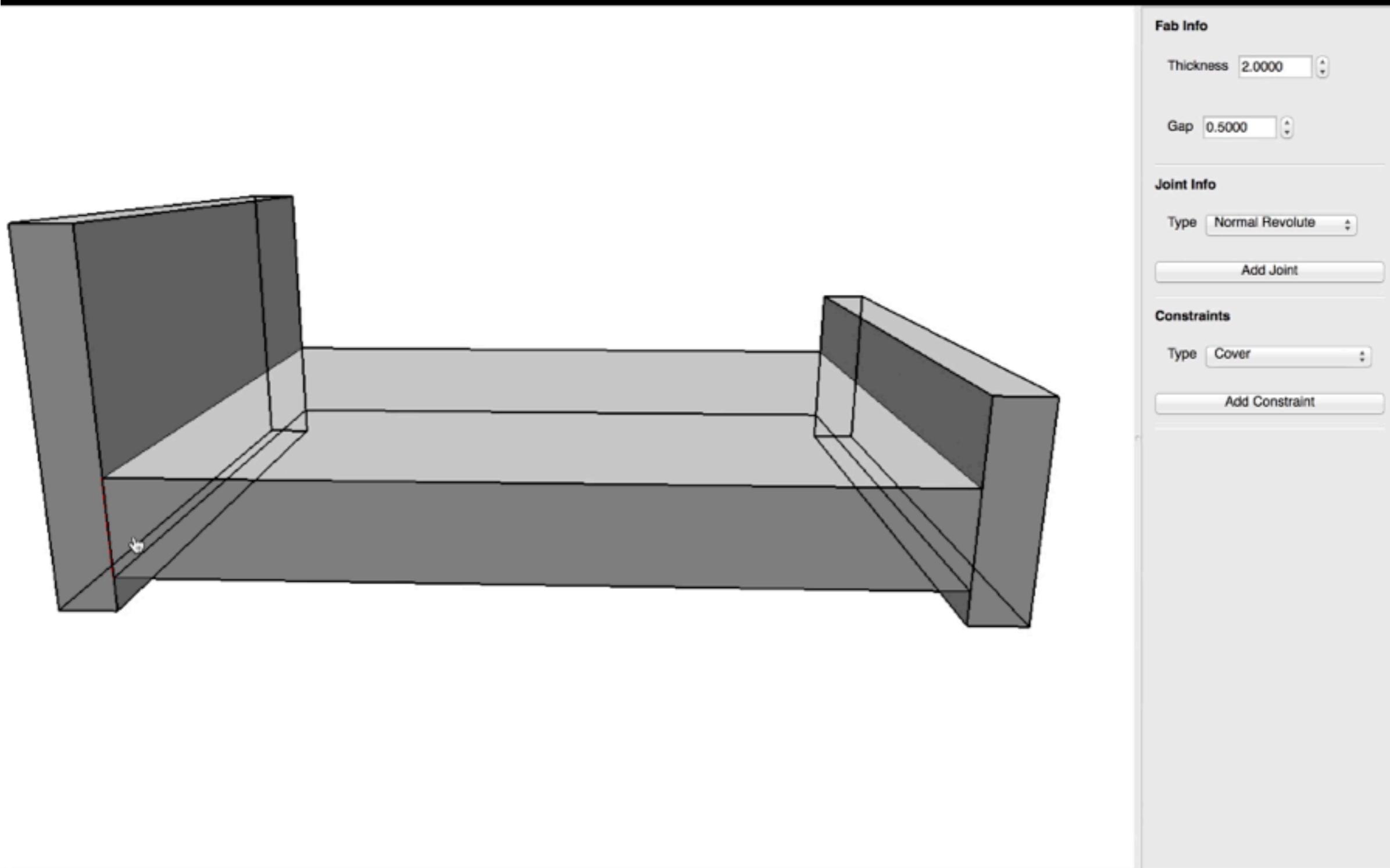
# Specifying functional relationships



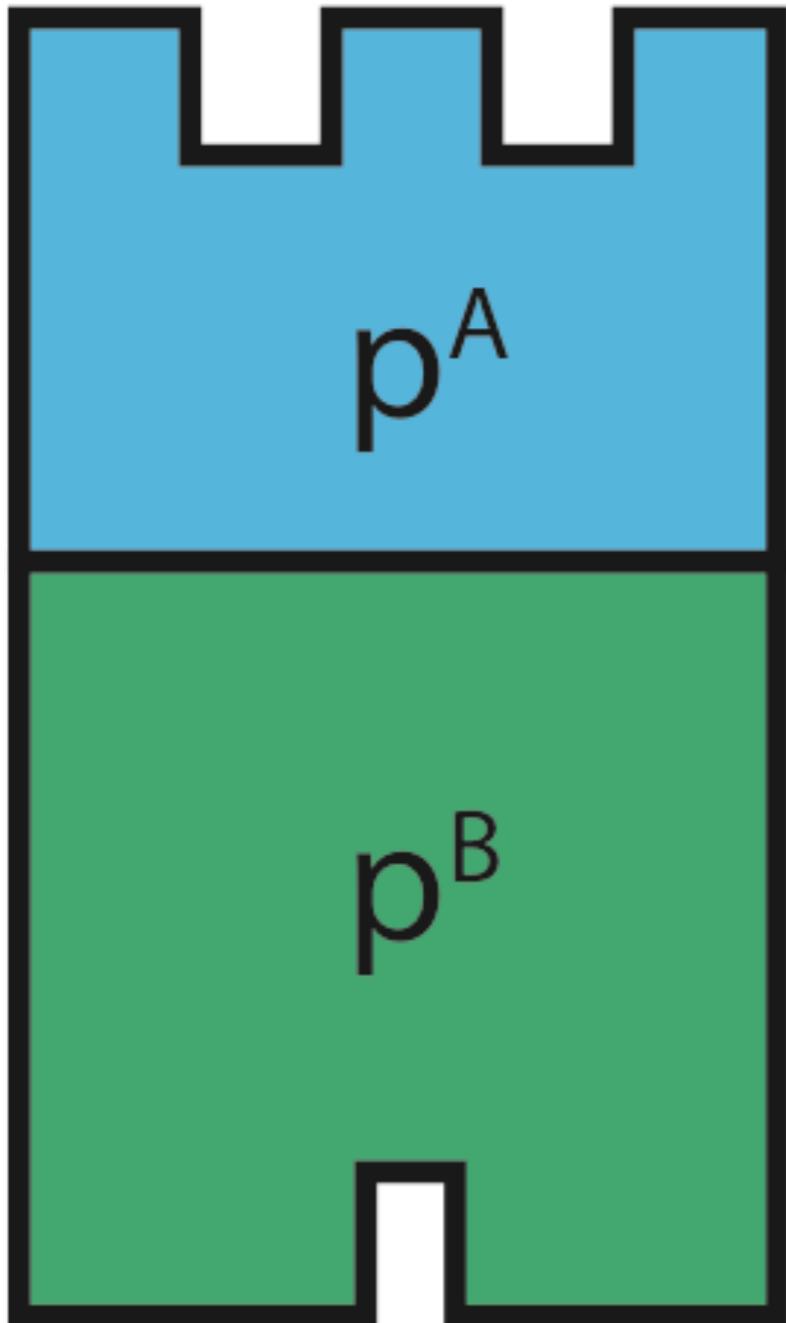
# Double pivot joints go wrong



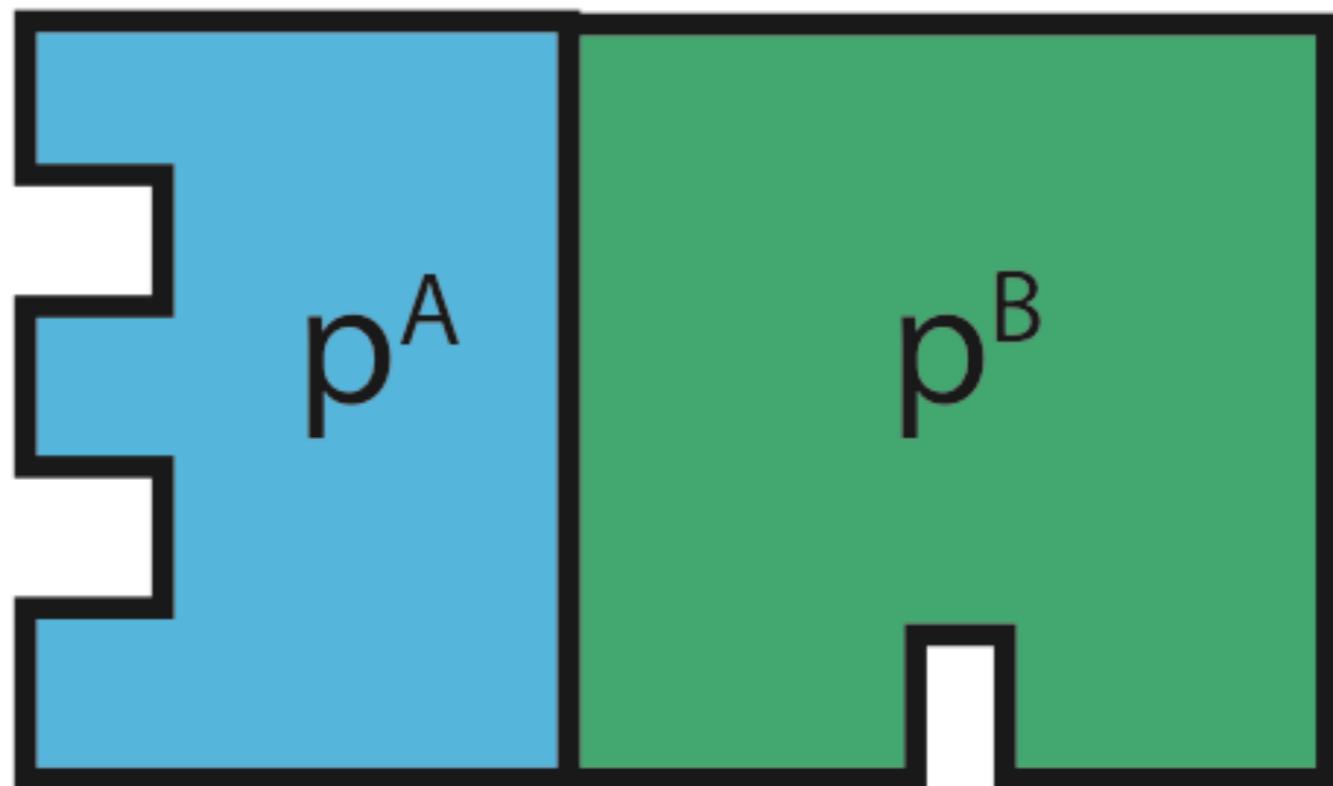
# Double pivot joints go wrong



# Double pivot joint constraints

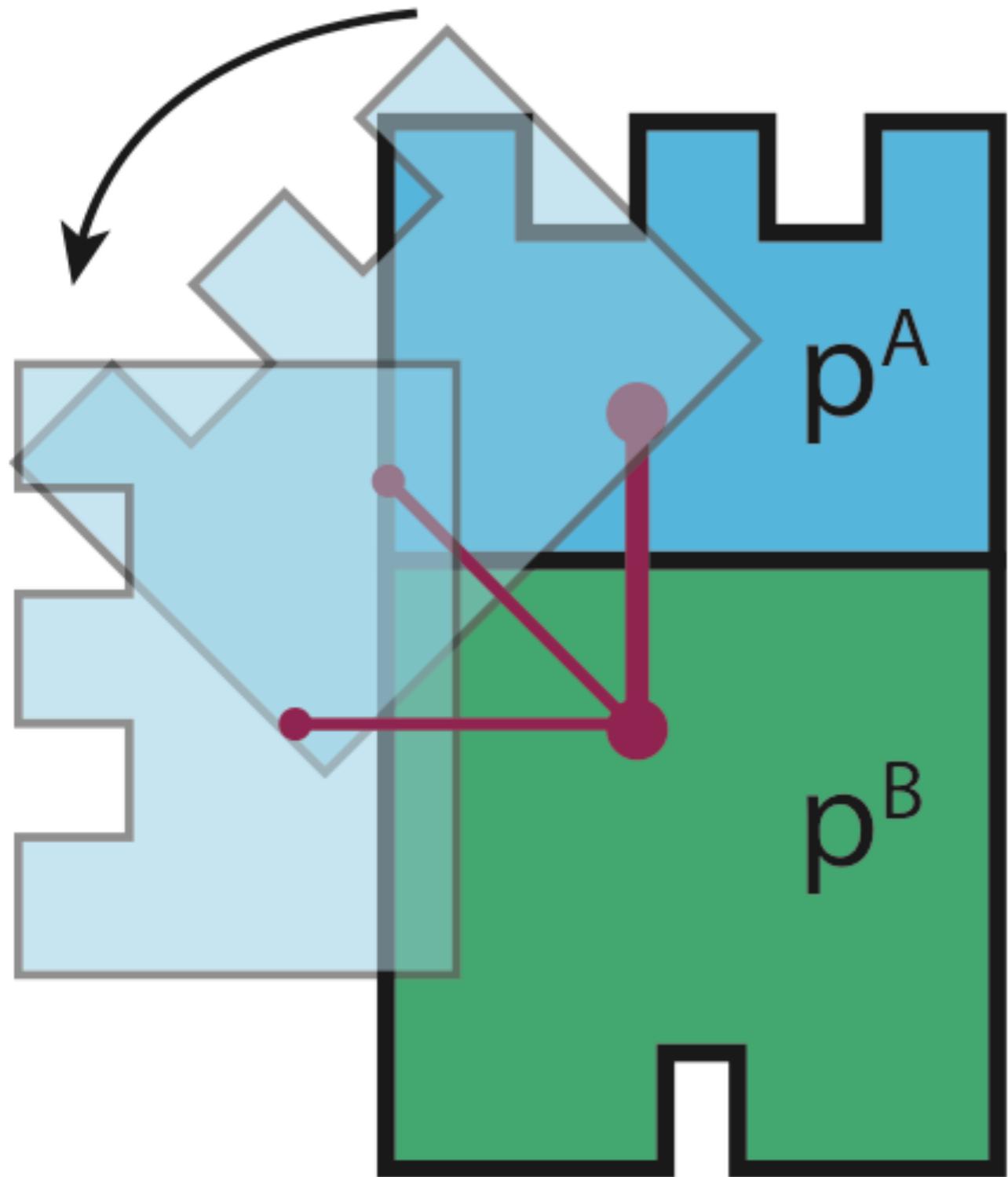


(a)  $C_1$

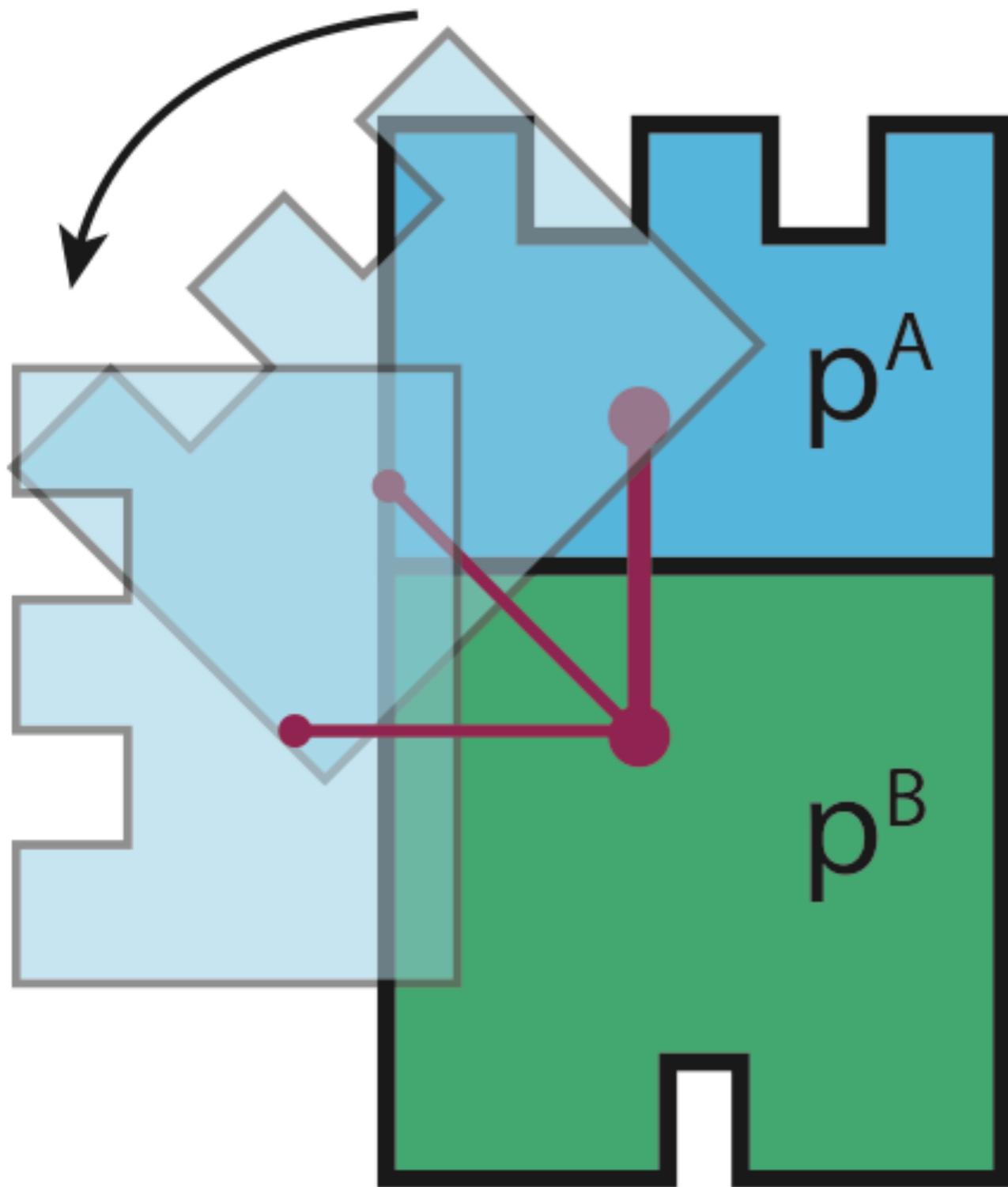


(b)  $C_2$

# Double pivot joint constraints



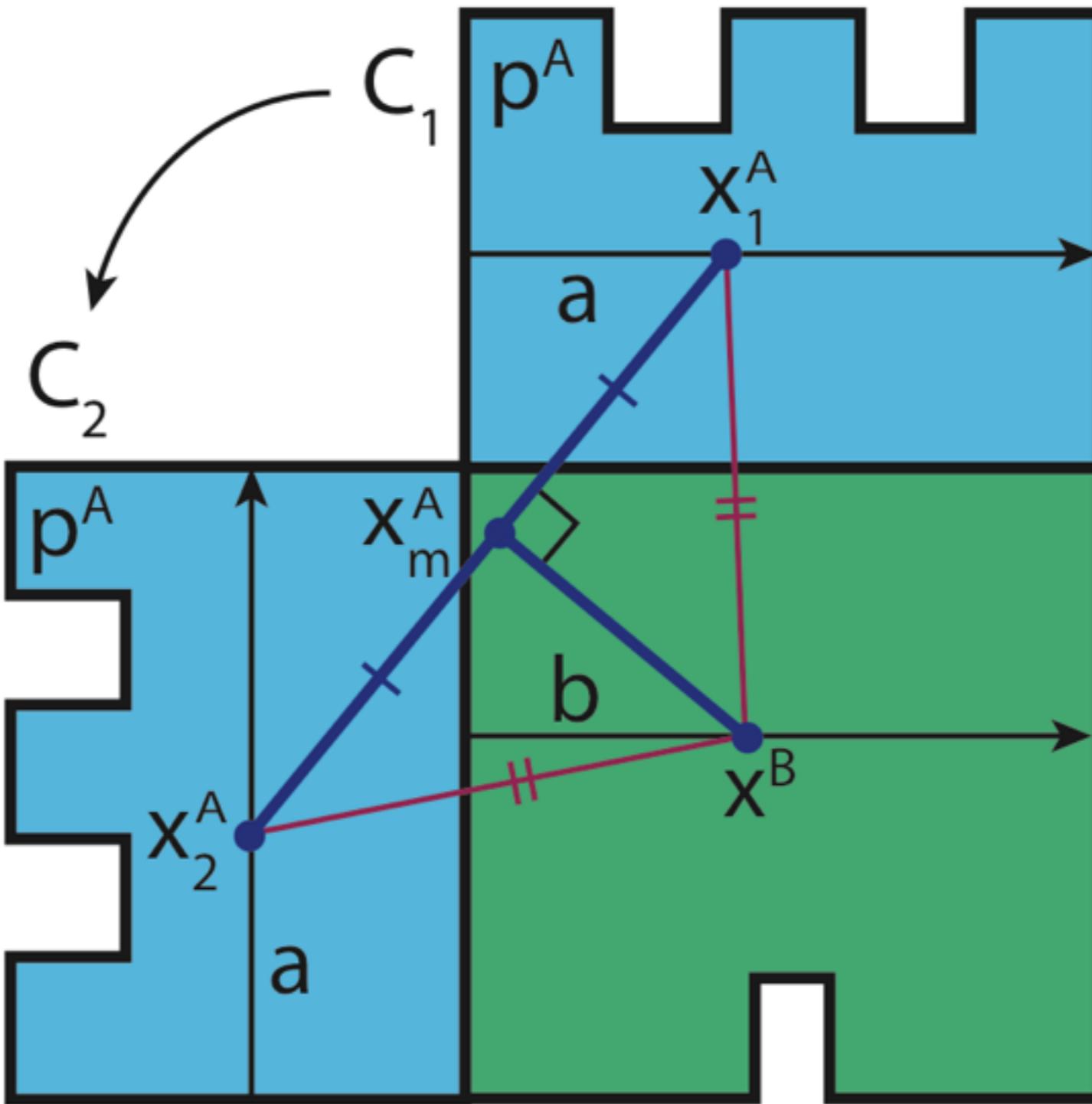
# Double pivot joint constraints



Position constraint

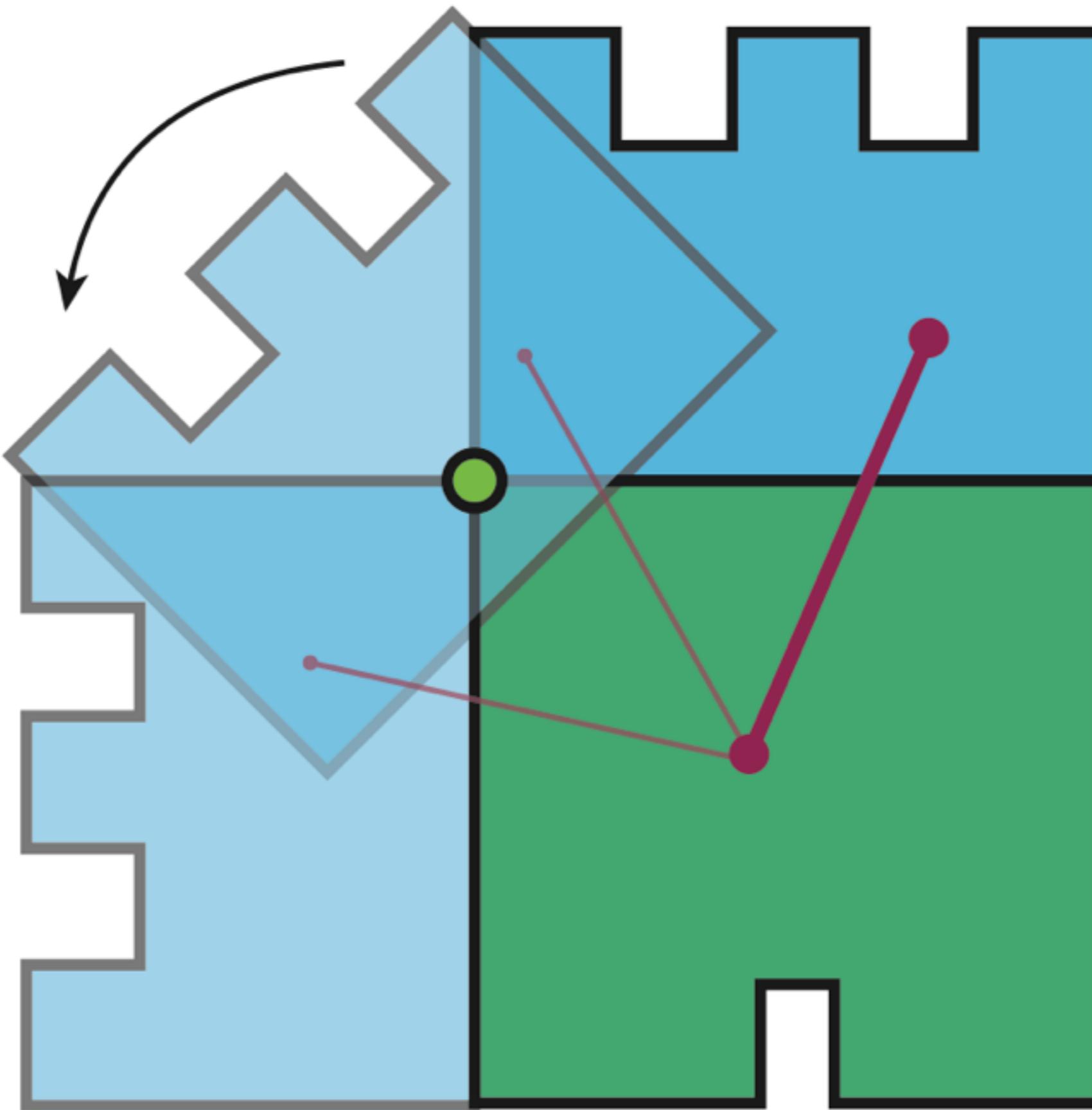
Motion constraint

# 1. Position constraint

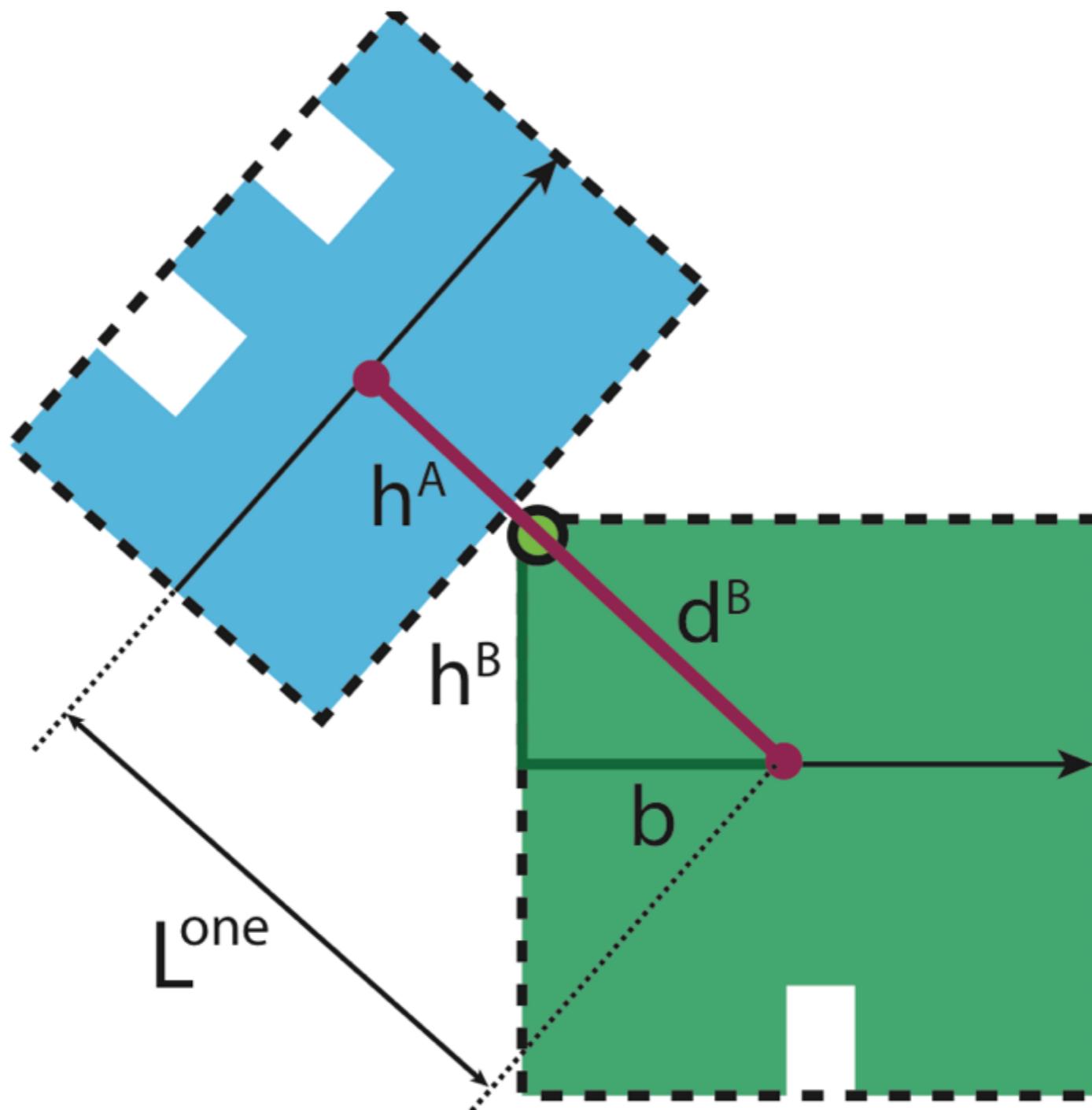


$$(x_2^A - x_1^A) \cdot (x_m^A - x^B) = 0$$

## 2. Motion constraint



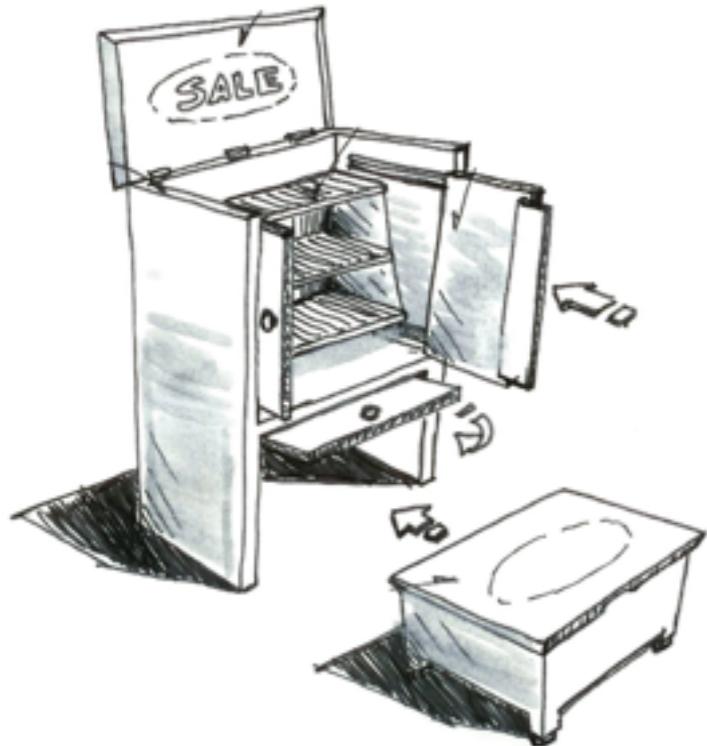
## 2. Motion constraint



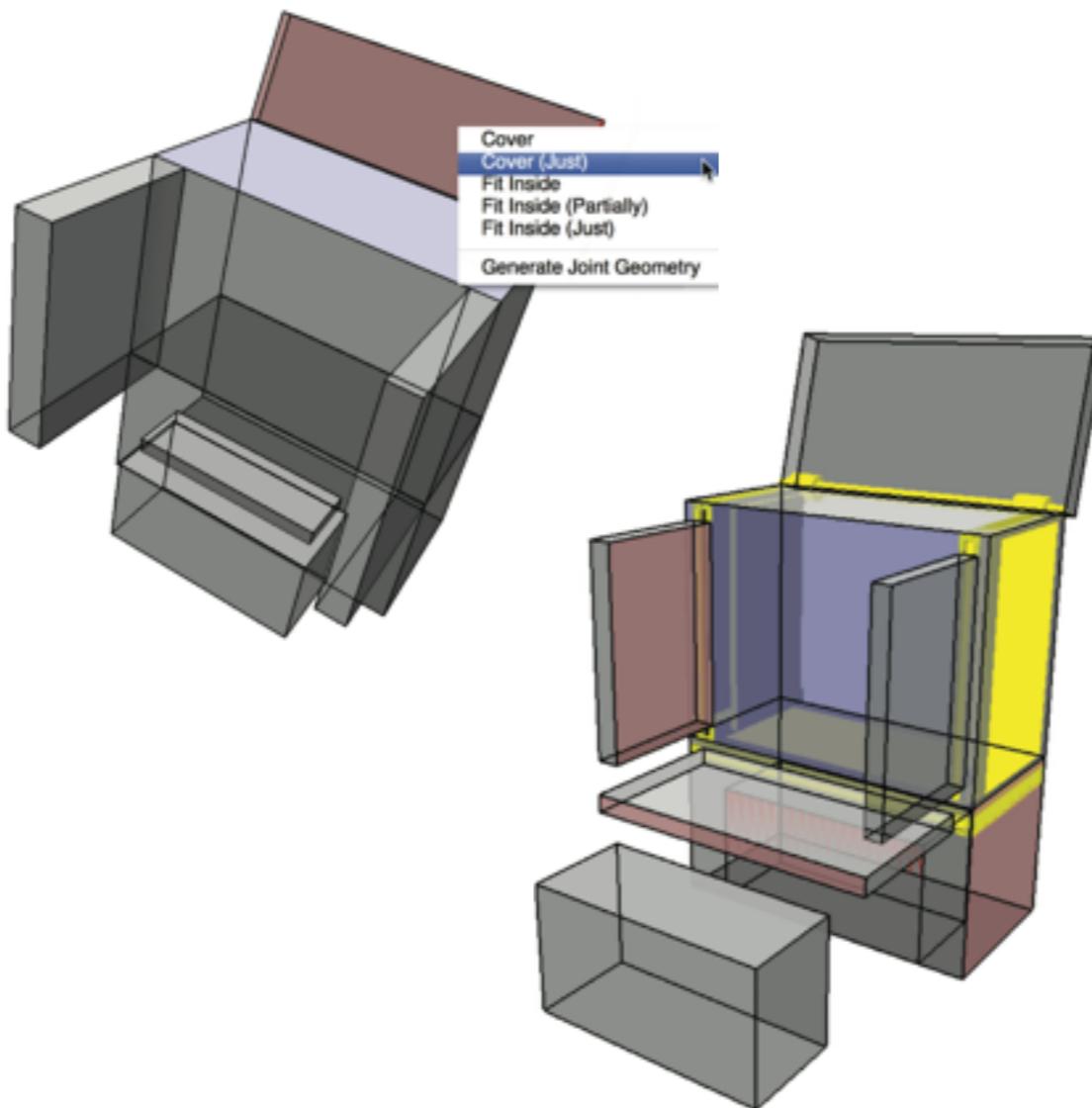
$$L^{one} > h^A + (h^B + b) / \sqrt{2}$$

# Overview

## Input

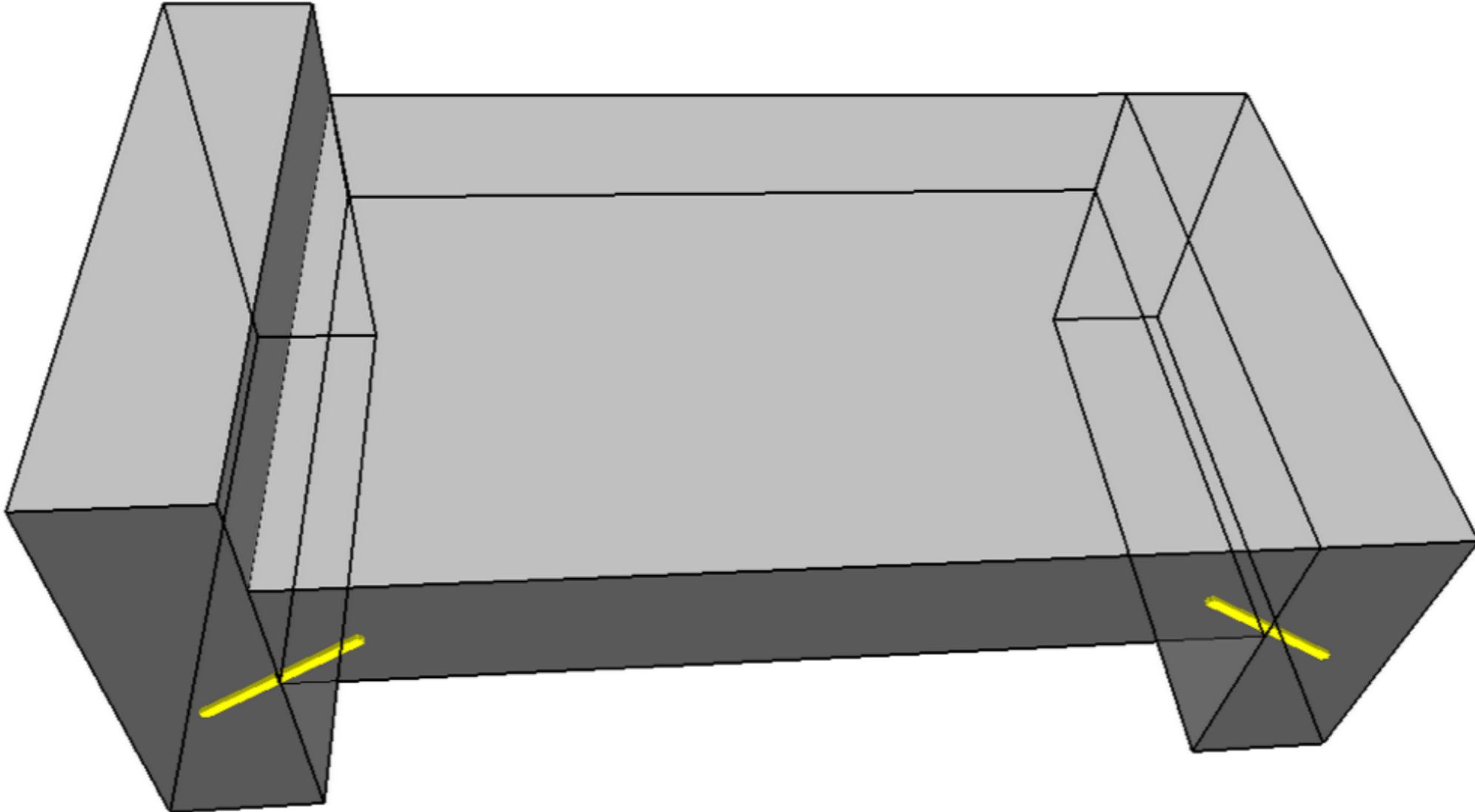


## 1. Constraints



## 2. Optimisation

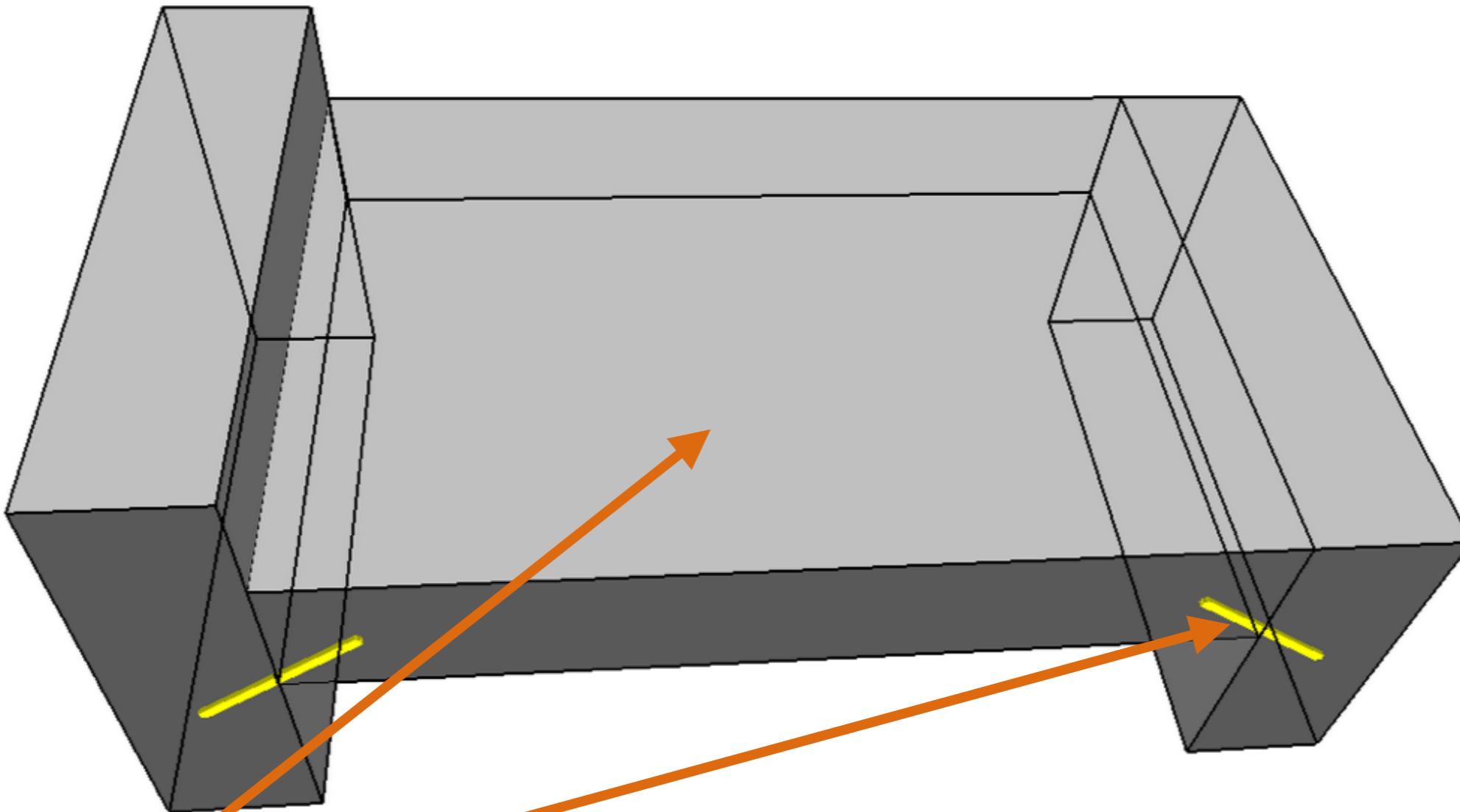
# Part and joint optimisation



$$E(B, L) = \sum_i \left\| B_i - \bar{B}_i \right\|^2 + \sum_j \left\| L_j - \bar{L}_j \right\|^2$$

subject to functional constraints

# Part and joint optimisation

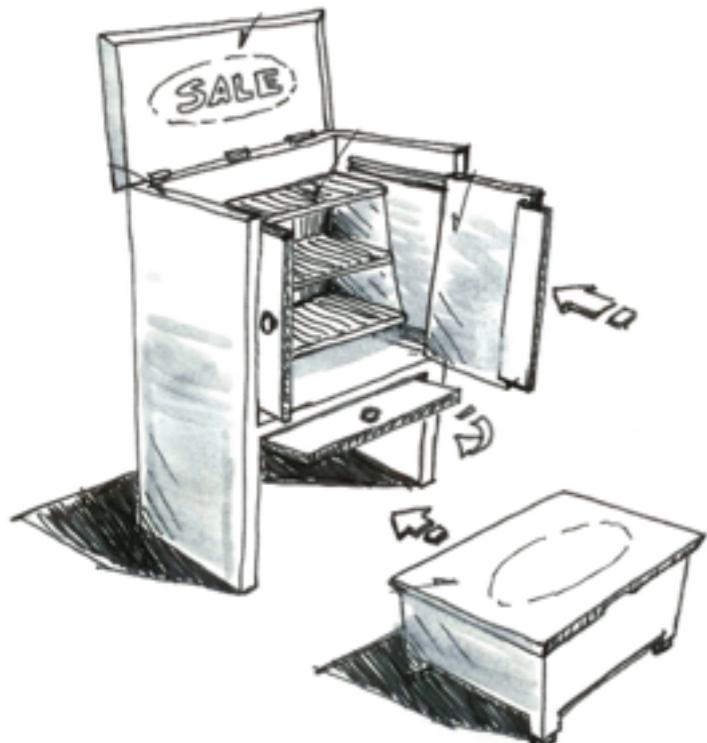


$$E(B, L) = \sum_i \|B_i - \bar{B}_i\|^2 + \sum_j \|L_j - \bar{L}_j\|^2$$

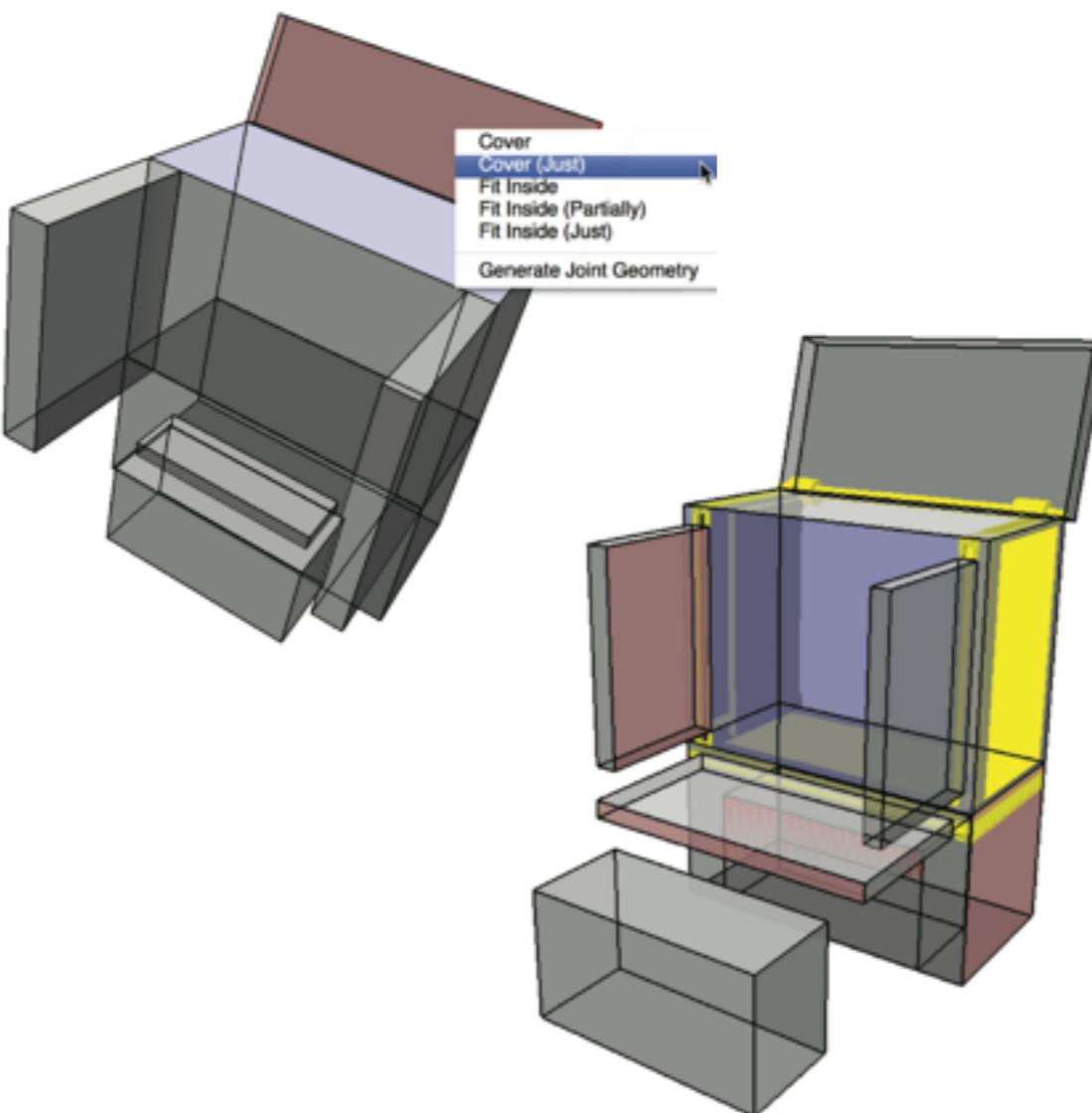
subject to functional constraints

# Overview

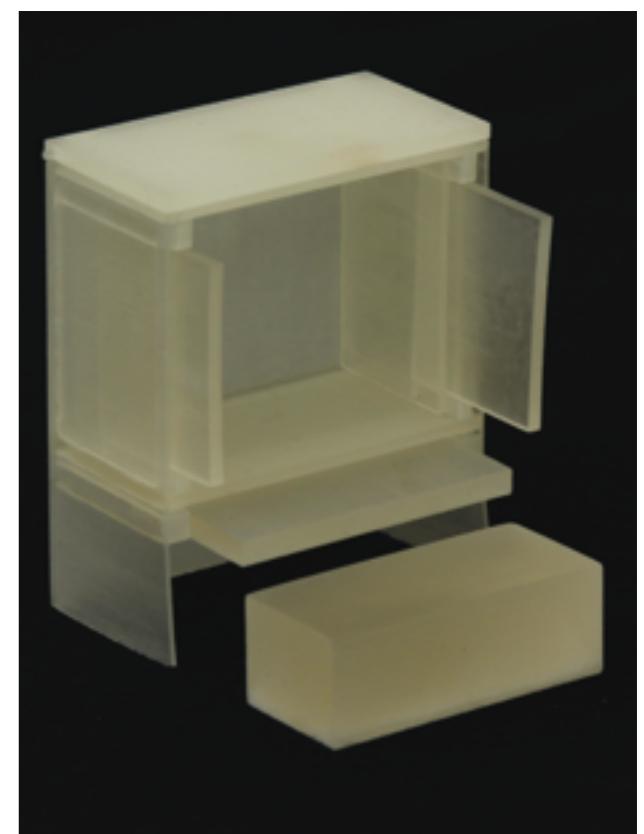
## Input



## 1. Constraints



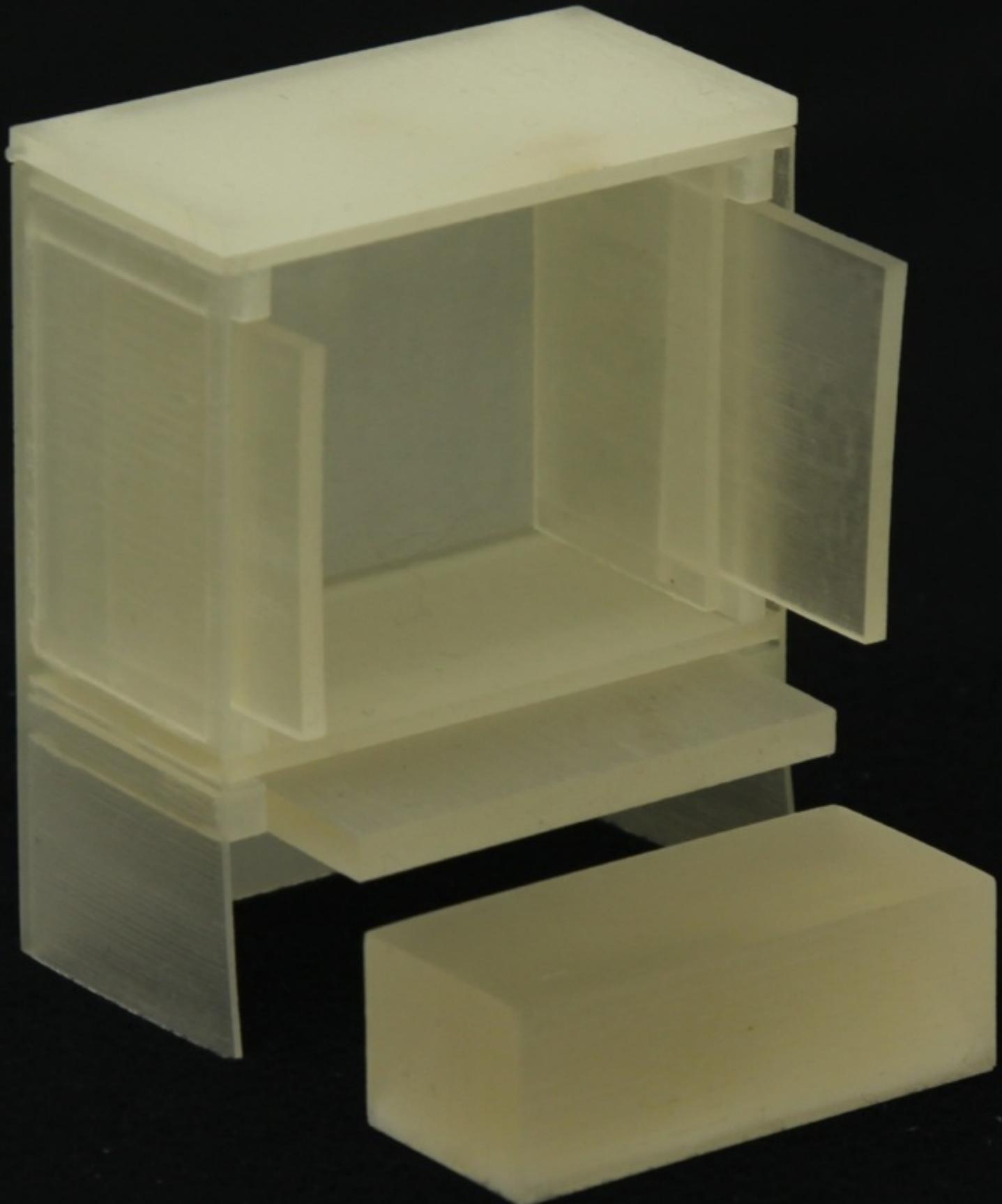
## 2. Optimisation



## Output

# Ready-to-fabricate models

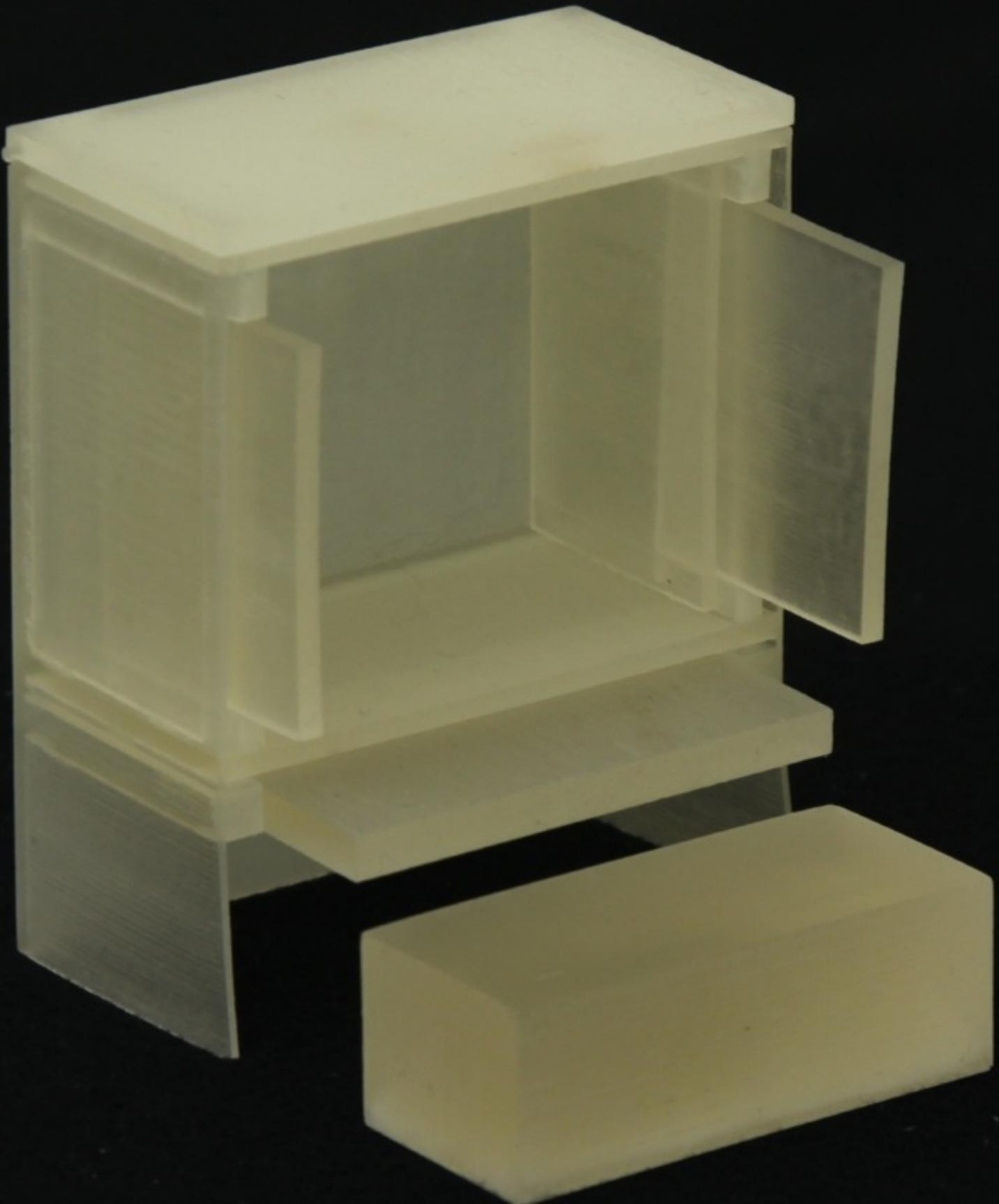
## Cavities



# Ready-to-fabricate models

Cavities

Joint geometry

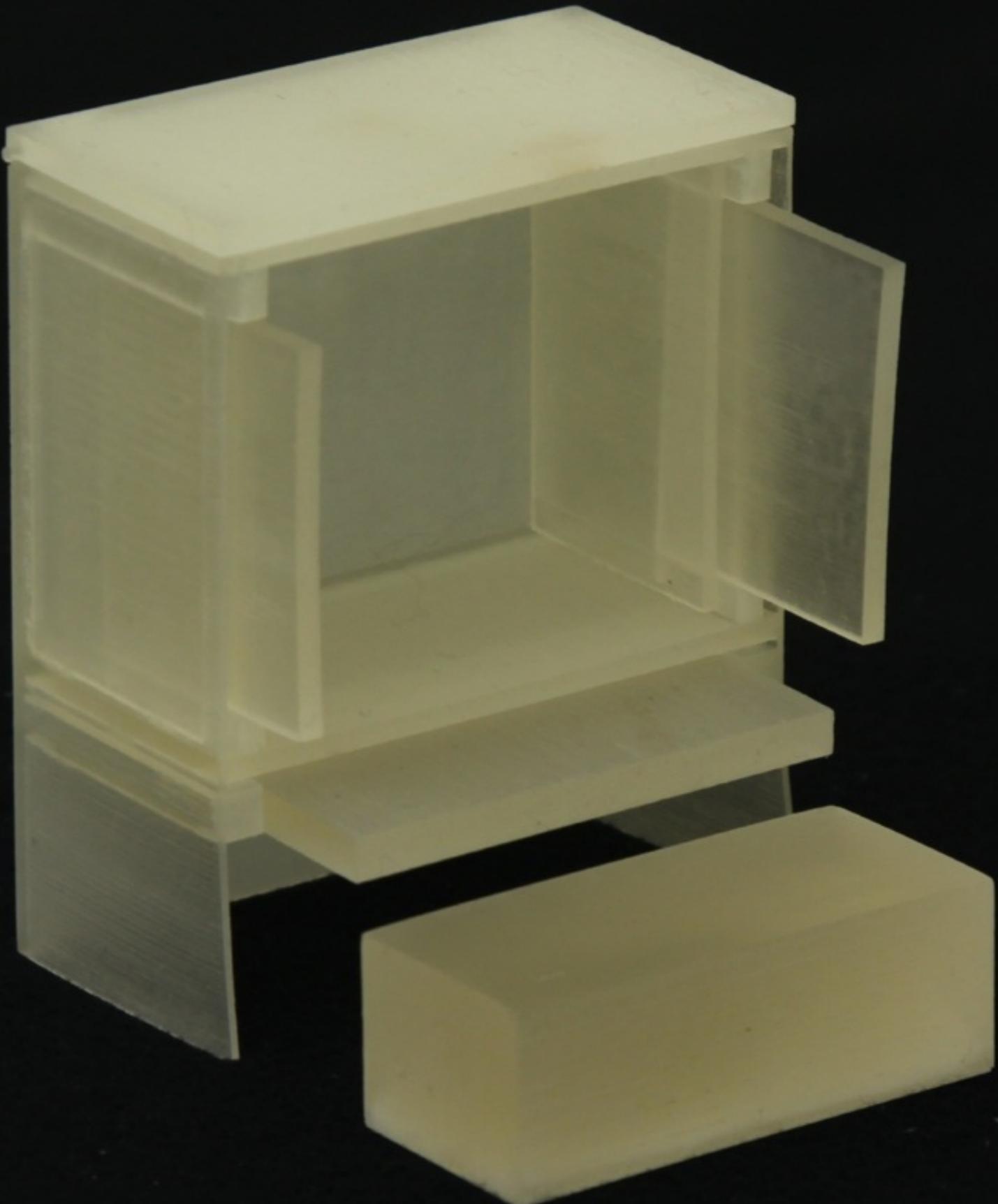


# Ready-to-fabricate models

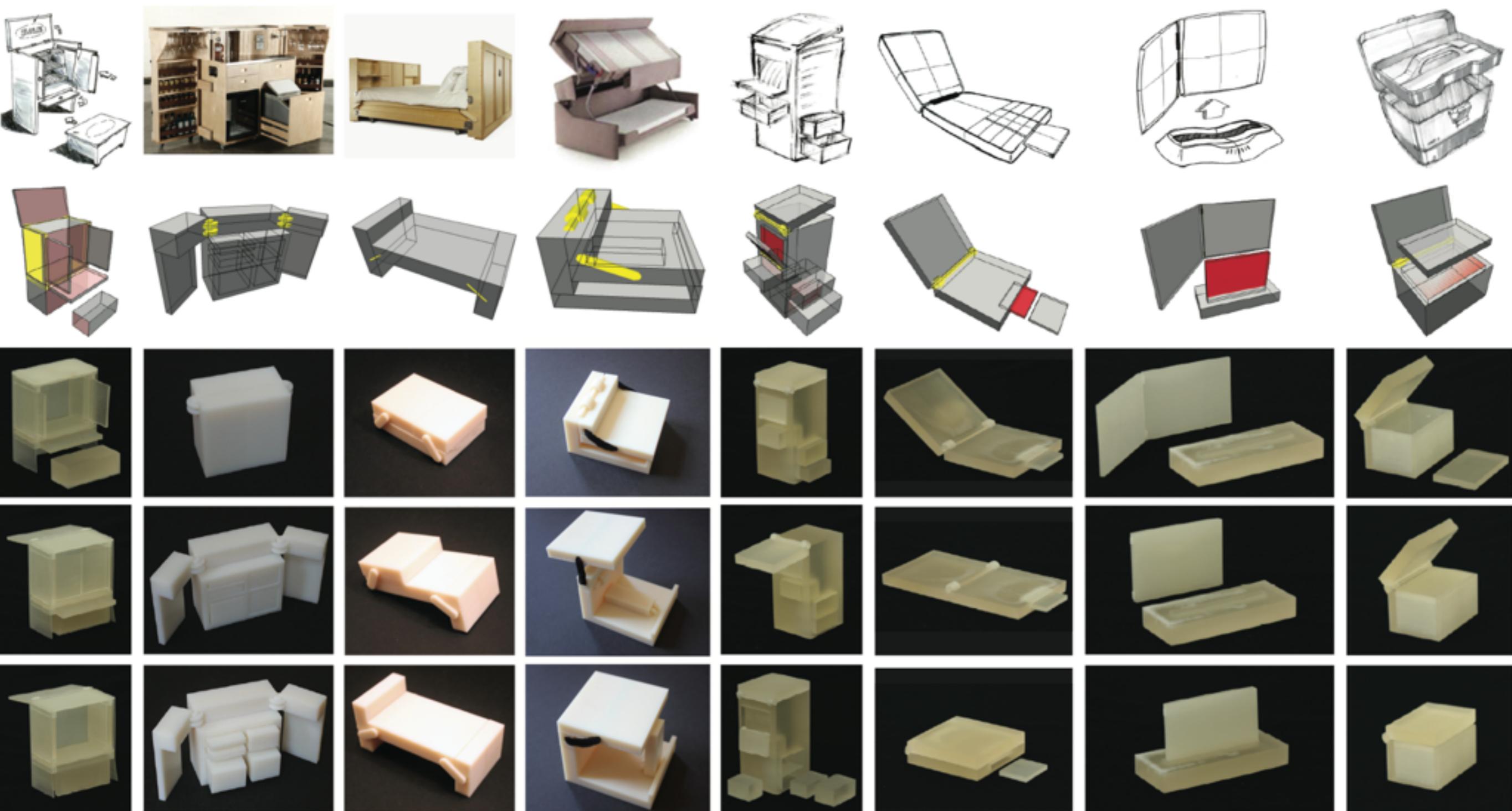
Cavities

Joint geometry

Gaps



# Results



# Results

Fabricated Prototypes

# Results

Fabricated Prototypes

# Limitations

**Limited part and joint types**

# Limitations

**Limited part and joint types**

**Few functional relationships**

# Thanks!

Model STLs available on:



Sponsors:



European Research Council  
Established by the European Commission

