



CreativeAI: Deep Learning for Computer Graphics

Unsupervised Learning in CG



Timetable

		Niloy	lasonas	Paul	Nils	Leonidas
Introduction	9:00	X				
Neural Network Basics	~9:15		Х			
Supervised Learning in CG	~9:50	X				
Unsupervised Learning in CG	~10:20			X		
Learning on Unstructured Data	~10:55					X
Learning for Simulation/Animation	~11:35				Х	
Discussion	12:05	X	Х	X	X	X



Unsupervised Learning

There is no direct ground truth for the quantity of interest

Focus on **generative** models:

- Variational Autoencoders (VAEs)
- Normalizing Flows
- Autoregressive Models (slides only)
- Generative Adversarial Networks (GANs)





- Assumption: the dataset are samples from an unknown distribution $p_{
 m data}(x)$
- Goal: create a new sample from $p_{\mathrm{data}}(x)$ that is not in the dataset





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 m data}(x)$
- Goal: create a new sample from $p_{
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Dataset

Generated





 $p_{\text{data}}(x) \approx p_{\theta}(x)$

Generative model with parameters heta





How do we measure the similarity of $p_{\theta}(x)$ and $p_{\text{data}}(x)$?

Which model?



How do we measure the similarity of $p_{\theta}(x)$ and $p_{\text{data}}(x)$?

1) Likelihood of data samples in $p_{\theta}(x)$

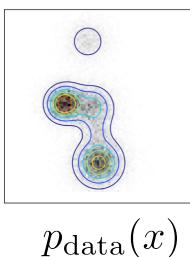
2) Adversarial game

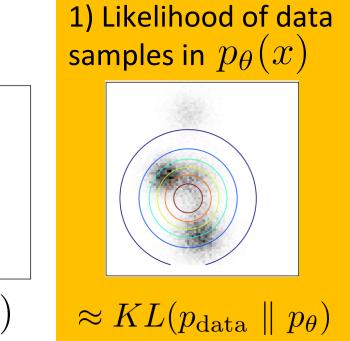
Variational Autoencoders (VAEs)Generative AdversarialNormalizing FlowsNetworks (GANs)

Autoregressive Models

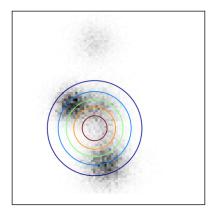


How do we measure the similarity of $p_{\theta}(x)$ and $p_{\text{data}}(x)$?





2) Adversarial game



 $\approx JS(p_{\text{data}} \parallel p_{\theta})$



Image Credit: How (not) to Train your Generative Model: Scheduled Sampling, Likelihood, Adversary?, Ferenc Huszár

Likelihood-Based Models: Two Goals

Sample? Evaluate?

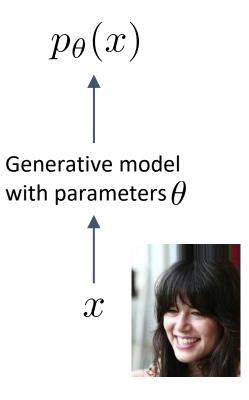
1) Sample from the generative model

2) Evaluate the likelihood of a given sample in the model



Generative model with parameters θ

 $x \sim p_{\theta}$





The Feature Space

Data distribution in 2D feature space (colors are class labels)

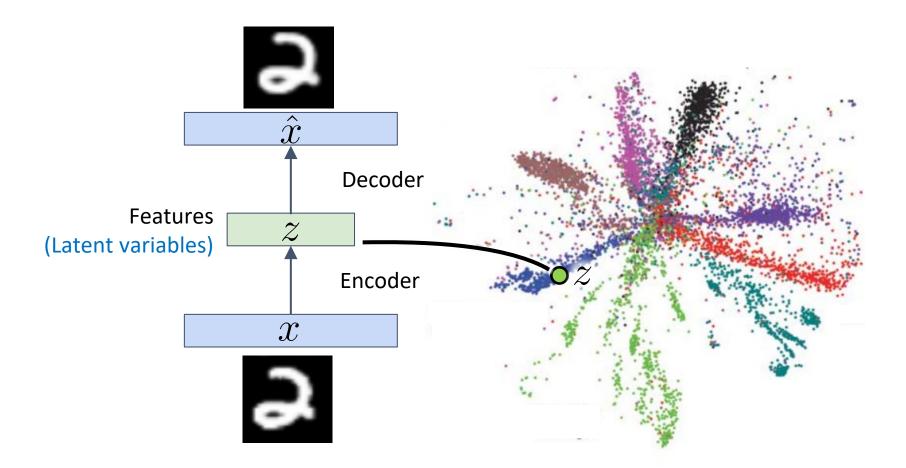




Image Credit: Reducing the Dimensionality of Data with Neural Networks, Hinton and Salakhutdinov

Autoencoders as Generative Models?



	• Is a trained decoder a ge	ene	era	tiv	<i>v</i> e	m	00	de	?		
Decoder = Generator?	• Can we generate a new	sar	mp	ole	x	\sim		p_{θ}	?		
	sample grid	random samples									
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p(z)	in feature space								>	З	ð
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data distribution	55555555555555555555555555555555555555	9	4	2	0	2	З	3	З	قر)	×
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		4	5	5		8	1	2	٥	4	2



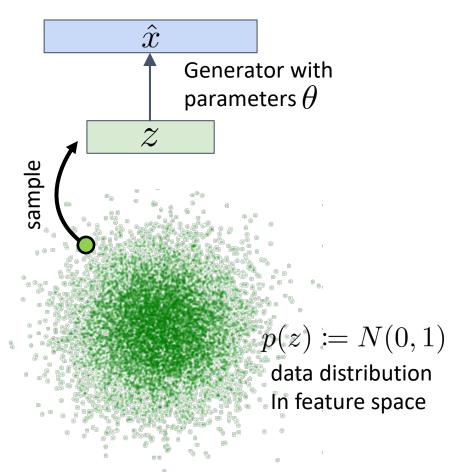
 $\hat{x}$ 

 $\mathcal{Z}$ 

random

#### **Latent Variable Model**



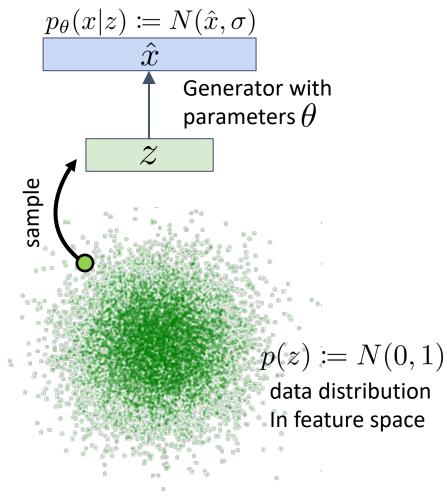


• Define p(z) as a known distribution



#### Latent Variable Model



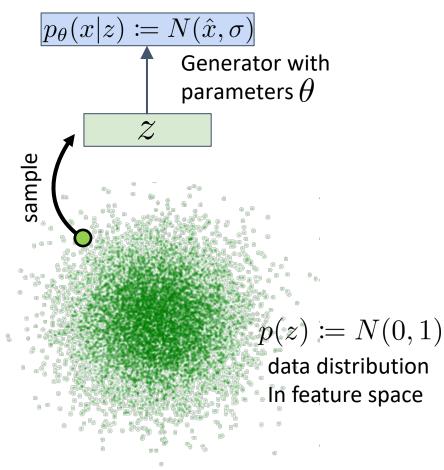


(Negative log-likelihood) • Train generator with NLL of data as loss  $-\log \sum_{x_i \in \text{data}} p_{\theta}(x_i)$ • Can we compute the likelihood  $p_{\theta}(x)$ ?  $p_{\theta}(x) = \int p_{\theta}(x|z) \ p(z) \ dz$ 



#### Latent Variable Model

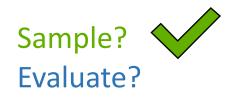


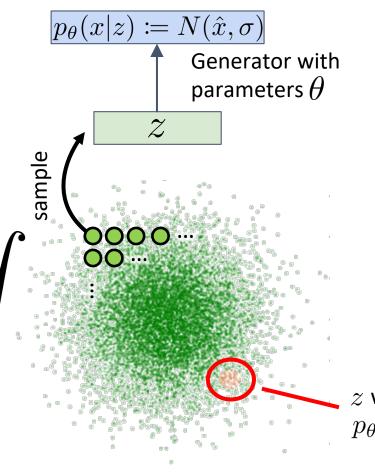


• Train generator with NLL of data as loss  $-\log \sum_{x_i \in \text{data}} p_{\theta}(x_i)$ • Can we compute the likelihood  $p_{\theta}(x)$ ?  $p_{\theta}(x) = \int p_{\theta}(x|z) \ p(z) \ dz$ 



### Latent Variable Model: Monte-Carlo





(Negative log-likelihood)

• Can we compute the likelihood  $p_{ heta}(x)$  ?

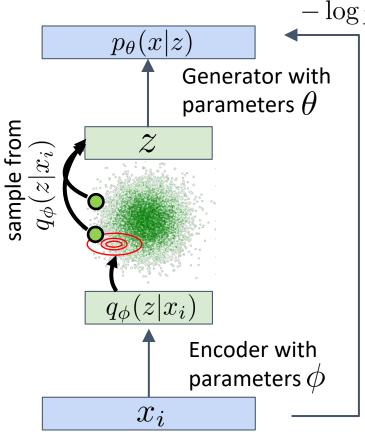
$$p_{\theta}(x) = \int p_{\theta}(x|z) \ p(z) \ dz$$

- Monte-Carlo integration to solve integral for each data sample
- Very expensive, or very inaccurate (depending on sample count)

z with non-zero  $p(z|x_i)$   $p_{ heta}(x_i|z)$ 



#### Variational Autoencoders (VAEs): The Encoder



- Loss: NLL of data  $-\log p_{\theta}(x_i|z)$  with  $z \sim q_{\phi}(z|x_i)$ 
  - During training, another network can learn to approximate the distribution  $p(\boldsymbol{z}|\boldsymbol{x}_i)$

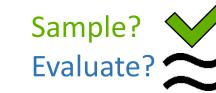
Sample?

**Evaluate?** 

- $q_{\phi}(z|x_i)$  should be much smaller than p(z)
- Makes the computing the integral tractable  $p_{\theta}(x) = \int p_{\theta}(x|z) \ p(z) \ dz$
- Instead of integrating over all p(z) , integrate over  $q_{\phi}(z | x_i)$  only
- A single random sample from  $q_{\phi}(z|x_i)$  per iteration is usually enough

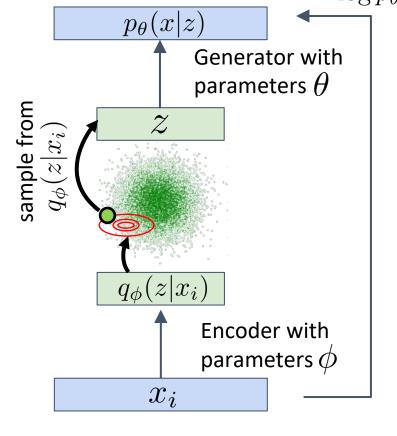


### Variational Autoencoders (VAEs): Regularization



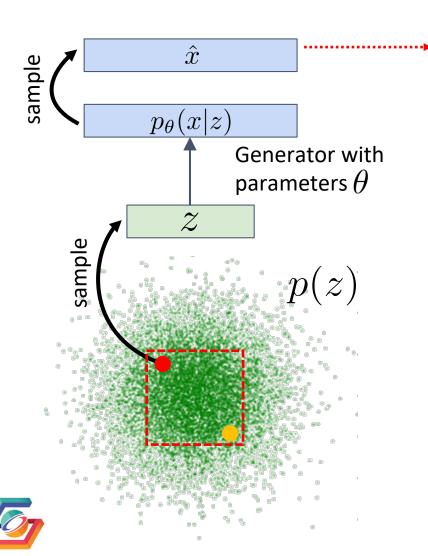
NLL of data as loss  $-\log p_{\theta}(x_i|z)$  with  $z \sim q_{\phi}(z|x_i) + KL(q_{\phi}(z|x_i) \parallel p(z))$ 

- The network can choose  $q_{\phi}(z|x_i)$  freely
- But it is regularized it to approximate  $p(\boldsymbol{z})$
- Neg. loss is a lower bound for the data's likelihood in the generated distribution





#### **Generating Data**



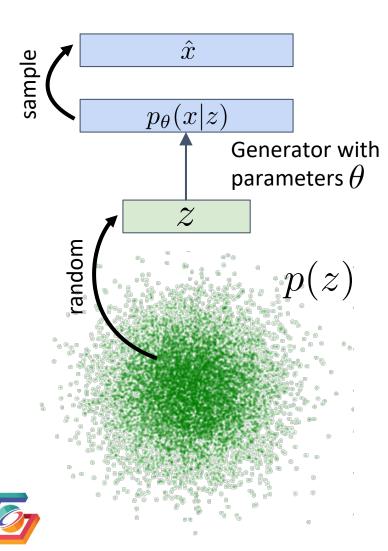
VAE

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Image Credit: Auto-Encoding Variational Bayes, Kingma and Welling

Autoencoder

#### **Generating Data**



VAE

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#### Autoencoder



#### Feature Space of Autoencoders vs. VAEs

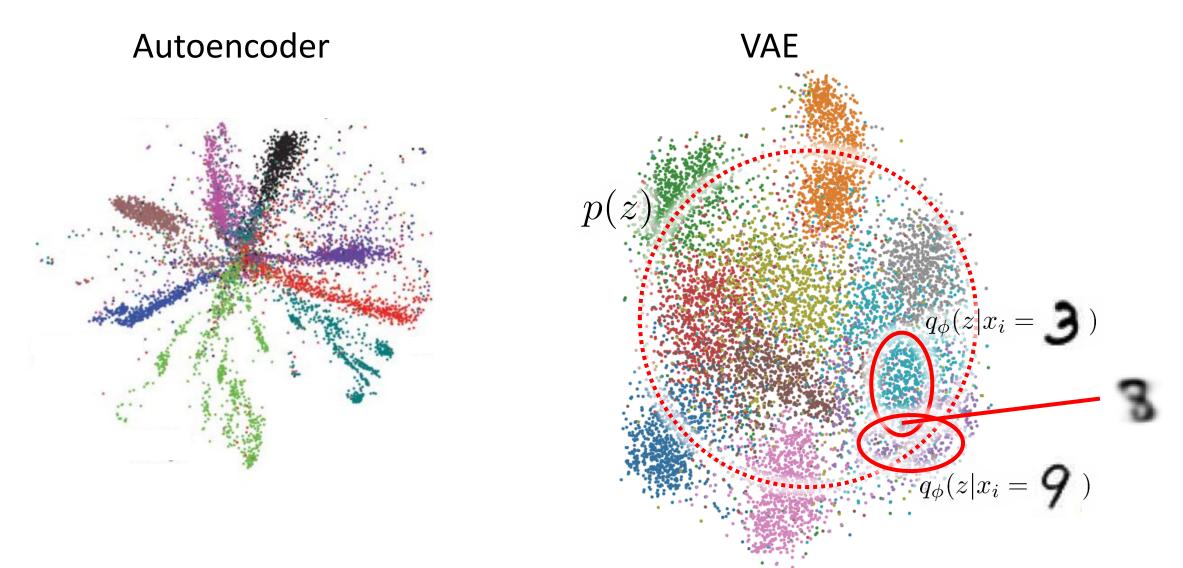


Image Credit: Reducing the Dimensionality of Data with Neural Networks, Hinton and Salakhutdinov

### Summary: Variational Autoencoders (VAEs)

#### **Positives**

- Creates a feature space
- Relatively stable to train

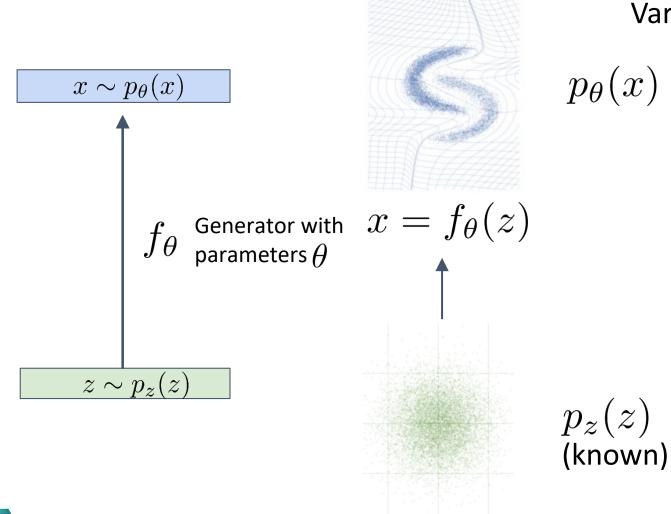
#### Negatives

- Likelihood evaluation can only be approximated
- Projection of sample into feature space can only be approximated
- Regularization makes the results a bit blurry



### **Normalizing Flows**





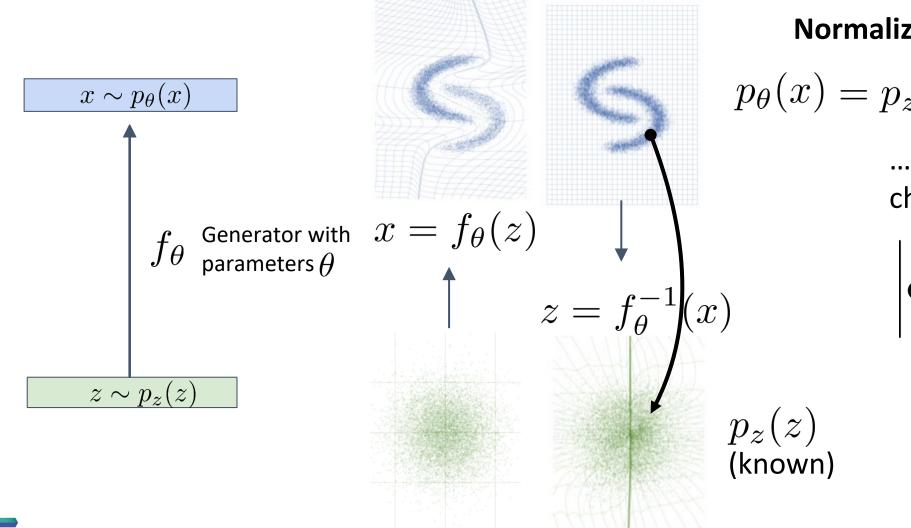
Variational Autoencoders (VAEs):

$$p_{\theta}(x) = \int p_{\theta}(x|z) p(z) dz$$

5

### **Normalizing Flows**

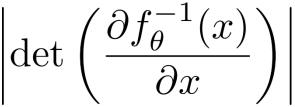




#### **Normalizing Flows:**

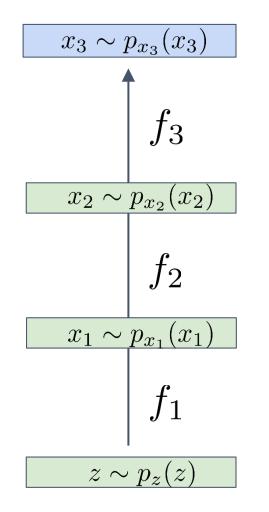
$$p_{\theta}(x) = p_z\left(f_{\theta}^{-1}(x)\right)$$

... times the local density change caused by  $f_{\theta}$ 



### **Normalizing Flows: Chaining**





$$p_3(x_3) = p_z \left( f_1^{-1} \circ f_2^{-1} \circ f_3^{-1} (x_3) \right)$$

... times the local density change caused by the chain of transformations

$$\prod_{i=1}^{3} \left| \det \left( \frac{\partial f_i^{-1}}{\partial x_i} \right) \right|$$



### **Example: Glow**

Invertible functions:

- Linear (1x1 conv) layer with weight matrix parameterized by its LU decomposition
- Affine coupling layer to propagate information between pixels





#### Training: 40 GPUs, 2 weeks

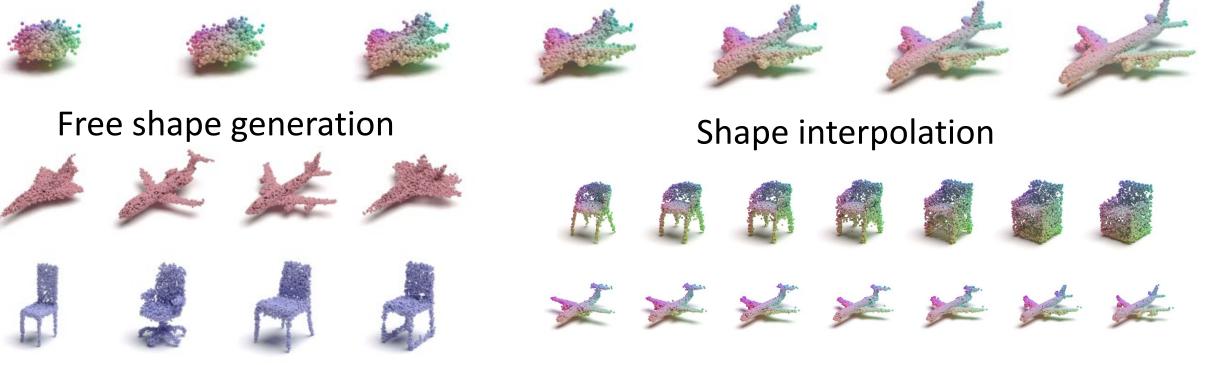


Image Credit: Glow: Generative Flow with Invertible 1x1 Convolutions, Kingma and Dhariwal

#### **Example: PointFlow**

Two flows: One to create the distribution of shape feature vectors, one for the distribution of points on a shape

Shape generation flow



### **Summary: Normalizing Flows**

#### **Positives**

- Creates a feature space
- Exact projection to feature space
- Exact likelihood evaluation

#### Negatives

- Only a limited set of functions (invertible and Jacobian easy to compute)
- Currently takes longer and needs more parameters than GANs for same quality



- Create output step-by-step
- Each step depends on the output of all previous steps

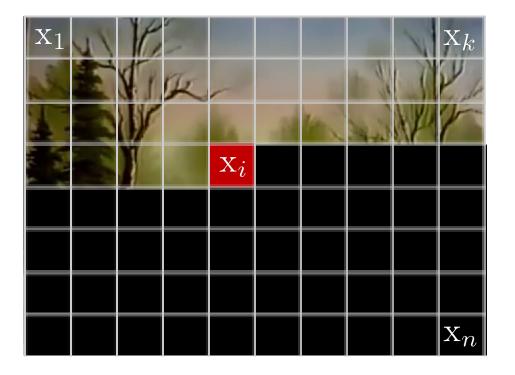






Video Credit: YouTube user karwan kalary, Bob Ross Time Lapse

- Create output step-by-step
- Each step depends on the output of all previous steps



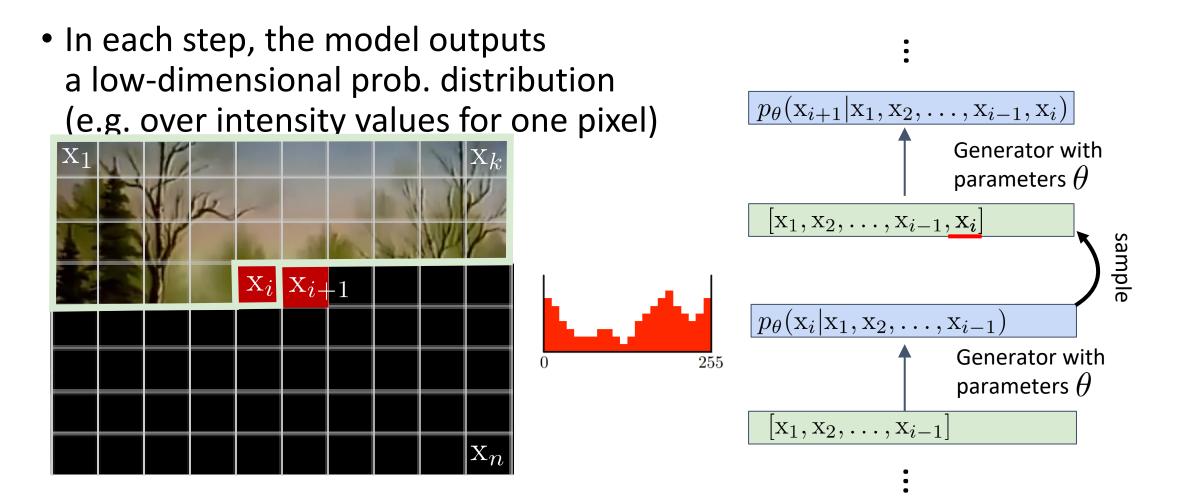
$$x = [\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_n]$$
$$p_{\theta}(x) = p_{\theta}(\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_n)$$

Chain rule of probability:  

$$p_{\theta}(x) = \prod_{i=1}^{n} p_{\theta}(\mathbf{x}_i | \mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_{i-1})$$









Video Credit: YouTube user karwan kalary, Bob Ross Time Lapse



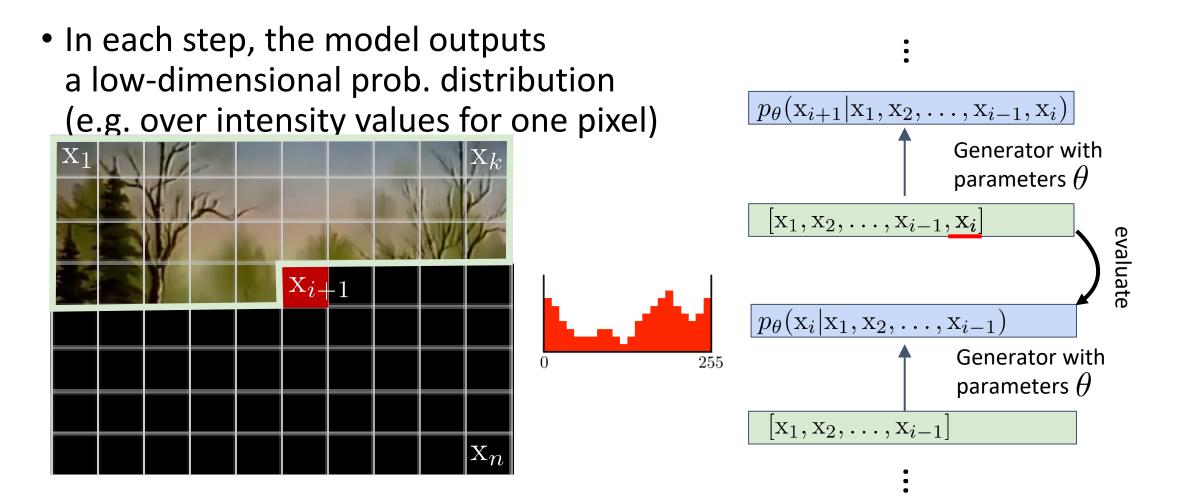
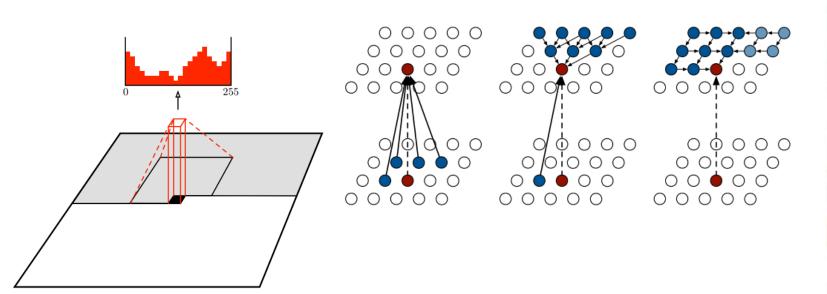




Image Credit: YouTube user karwan kalary, Bob Ross Time Lapse

### **Example: PixelRNN and PixelCNN**

- Recursive network that has an **input** and a **state** (LSTM)
- Only recent steps are used as **input**, the **state** summarizes older steps









Lhasa Apso (dog)



Brown bear



#### **Example: Graph Generation**

GraphRNN Learning Deep Generative Models of Graphs  $h_1$  $h_6$  $h_2$  $h_4$  $h_5$  $h_3$ (1)Add node (0)? Add edge? Add node (1)? Add edge? Pick node (0) to (yes/no) (yes/no) (yes/no) (yes/no) add edge (0,1) 0 0 0 0 (1)1 1 (2)Grid **Training Set** Ego Training Set GraphRNN New model Baseline

**Baseline** 

Image Credit: Conditional Image Generation with PixelCNN Decoders, Oord et al. GraphRNN: Generating Realistic Graphs with Deep Auto-regressive Models, You et al. Learning Deep Generative Models of Graphs , Li et al.

### **Summary: Autoregressive Models**

#### **Positives**

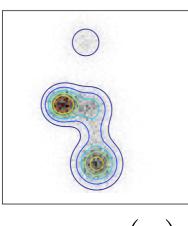
- Flexible output length
- Exact likelihood evaluation

#### Negatives

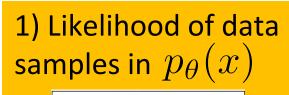
- No feature space
- Sequential generation (usually slow)



#### How do we measure the similarity of $p_{\theta}(x)$ and $p_{\text{data}}(x)$ ?



 $p_{\text{data}}(x)$ 



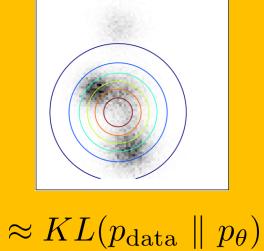






Image Credit: How (not) to Train your Generative Model: Scheduled Sampling, Likelihood, Adversary?, Ferenc Huszár

#### **Generative Adversarial Networks (GANs)**



#### $\mathcal{Z} \rightarrow \mathsf{Player 1: generator}$

Scores if discriminator can't distinguish output from real image



from dataset

# Player 2: discriminator → real/fake Scores if it can distinguish between real and fake

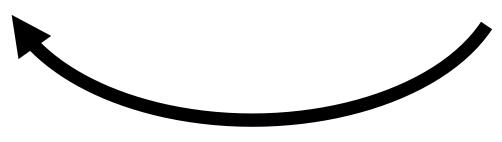


## **Generative Adversarial Networks (GANs)**

#### **Player 1: generator** Scores if discriminator can't distinguish output from real image

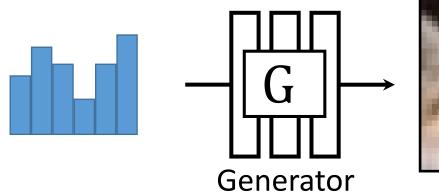
#### **Player 2: discriminator**

Scores if it can distinguish between real and fake





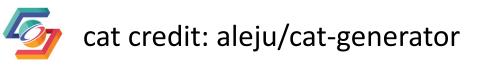




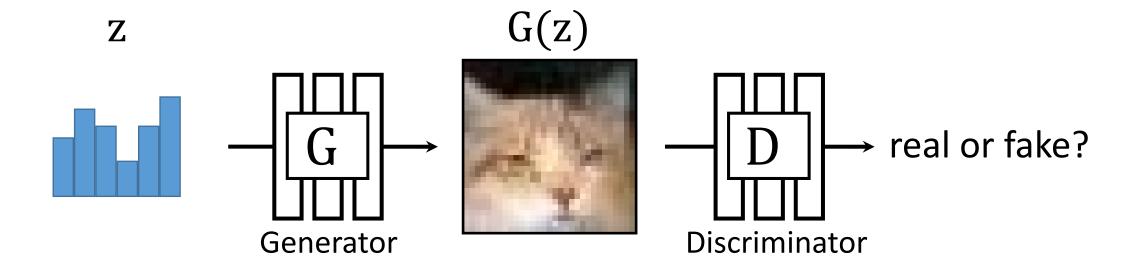
Ζ



### G: generate fake samples that can fool D







## G: generate fake samples that can fool D D: classify fake samples vs. real images

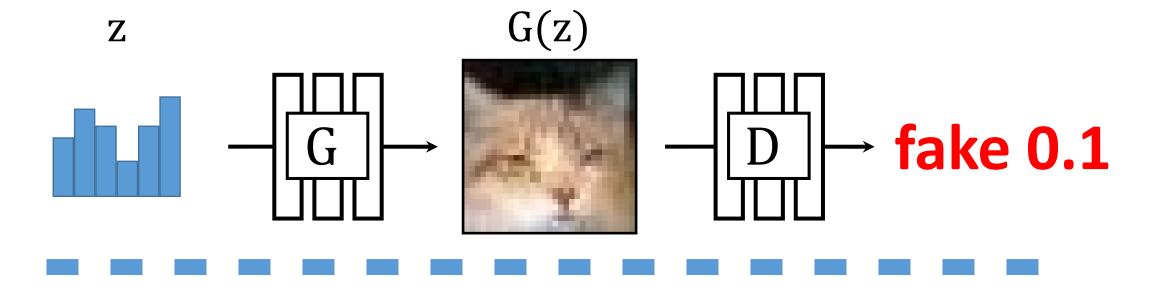






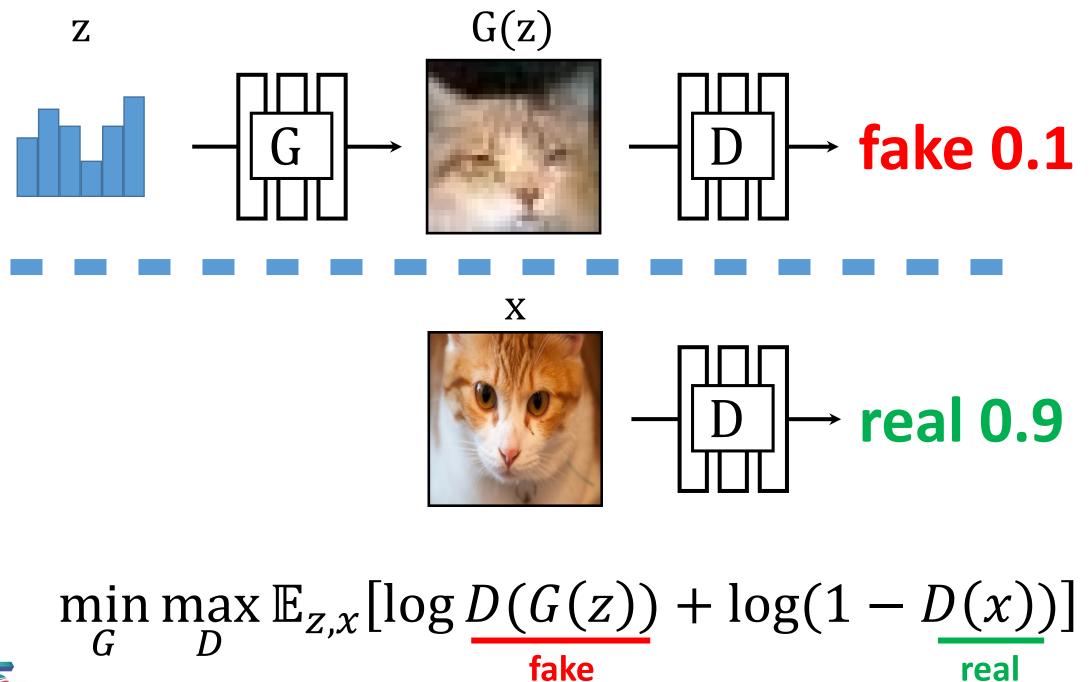
 $\min_{G} \max_{D} \mathbb{E}_{z,x}[$ 



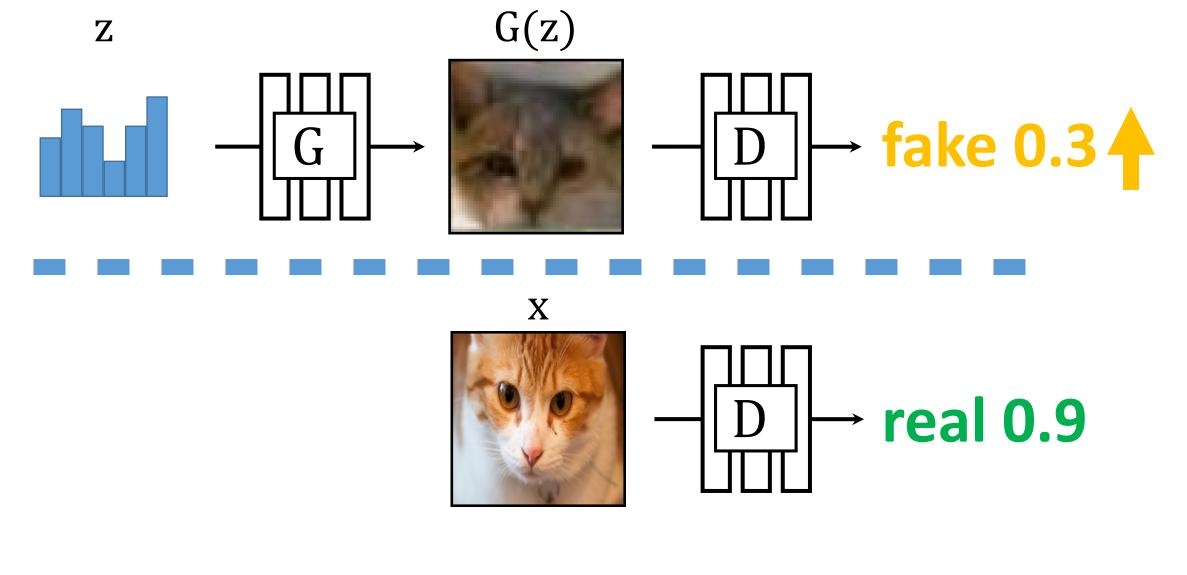


 $\min_{G} \max_{D} \mathbb{E}_{z,x}[\log D(G(z))]$ fake

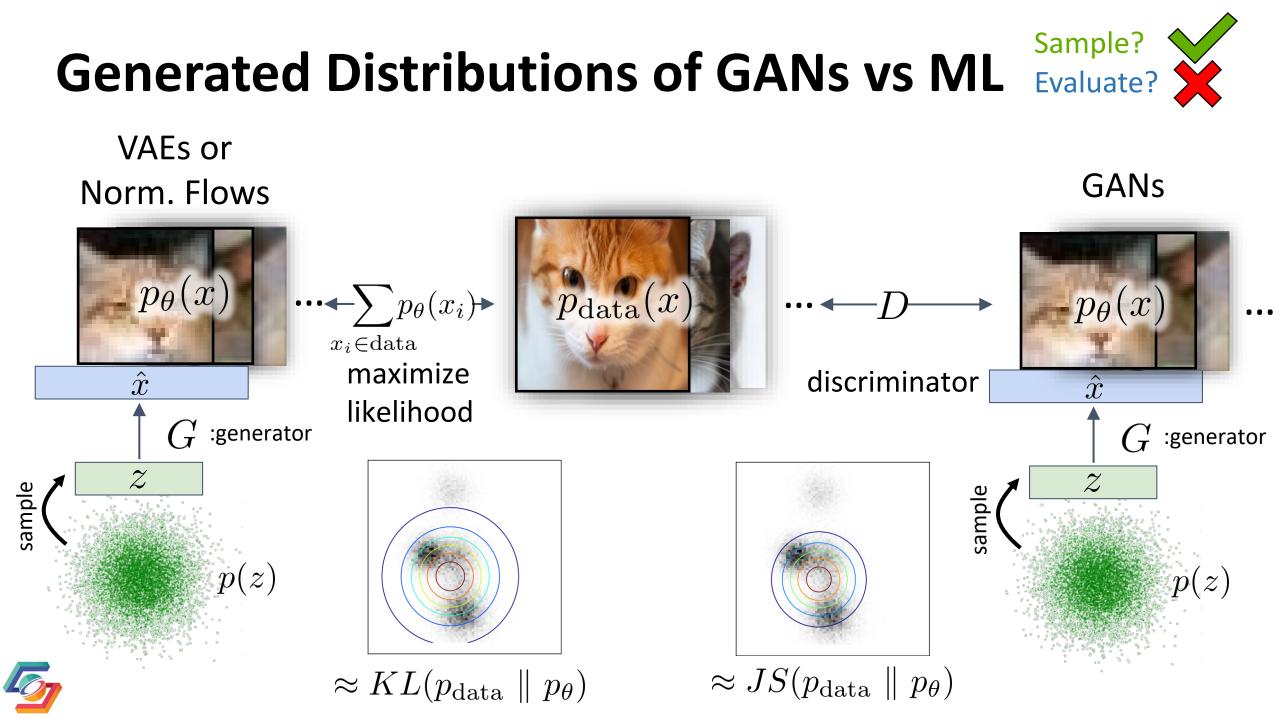




slide credit: Phillip Isola & Jun-Yan Zhu



# $\min_{G} \max_{D} \mathbb{E}_{z,x}[\log D(G(z)) + \log(1 - D(x))]$ Update G



## StyleGAN

Additional Tricks:

- Coarse-to-fine training
- Transformation of p(z) to a more complex distr.

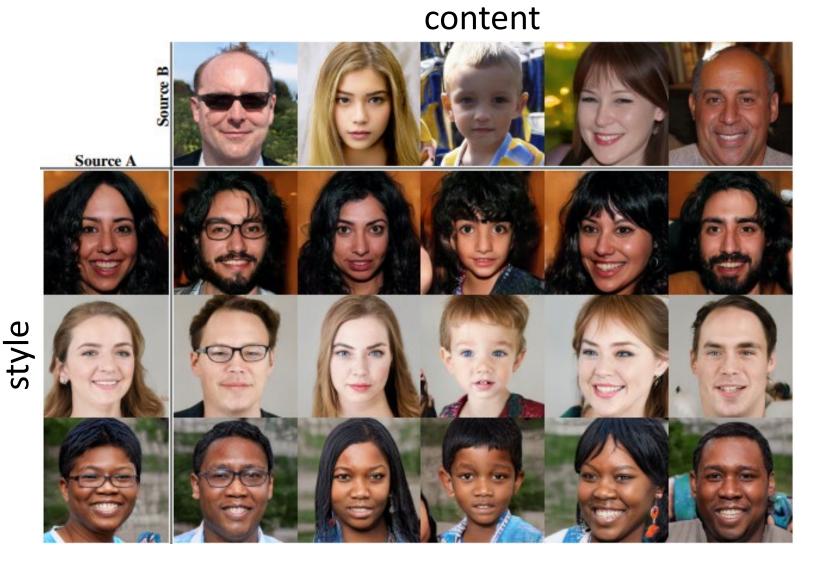




Image credit: A Style-Based Generator Architecture for Generative Adversarial Networks, Karras et al.

## **Summary: GANs**

#### **Positives**

- Creates a feature space
- Currently highest-quality results

#### Negatives

- Can be unstable to train
- Not guaranteed to cover all of the data distribution
- Cannot evaluate likelihood



## **Open Problems**

- More control
- Irregular data
- GAN training convergence
- Evaluating GANs



## **Conditional GAN: Pix2Pix**

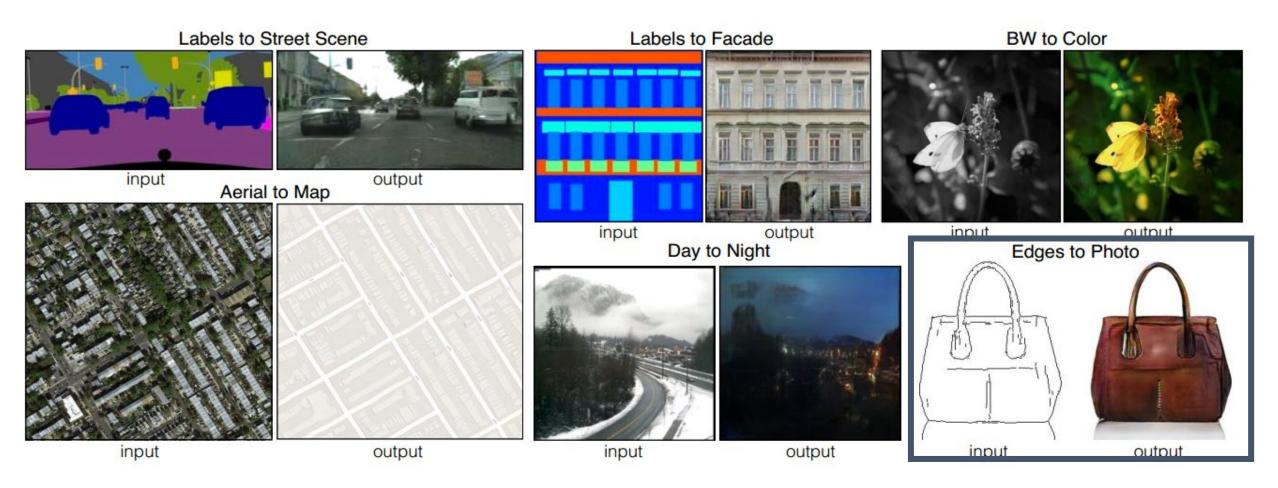
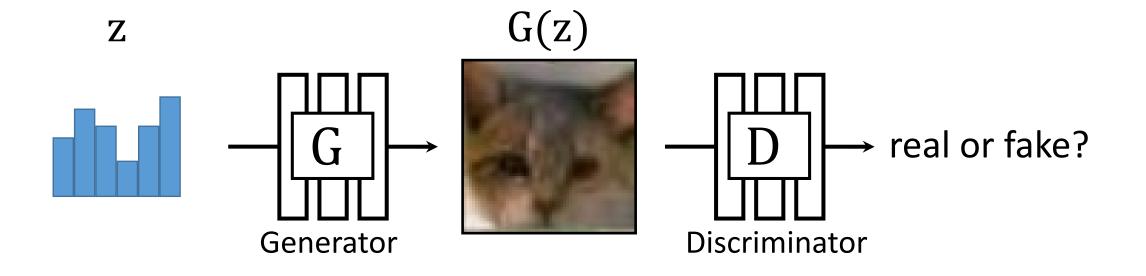
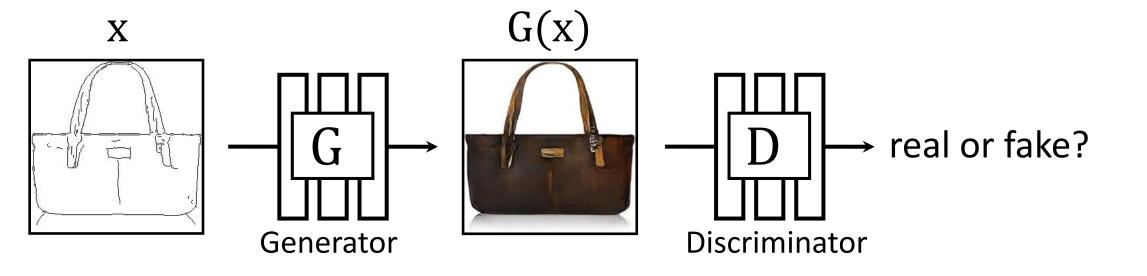


Image-to-image Translation with Conditional Adversarial Nets Phillip Isola, Jun-Yan Zhu, Tinghui Zhou, Alexei A. Efros. CVPR 2017 slide credit: Phillip Isola & Jun-Yan Zhu



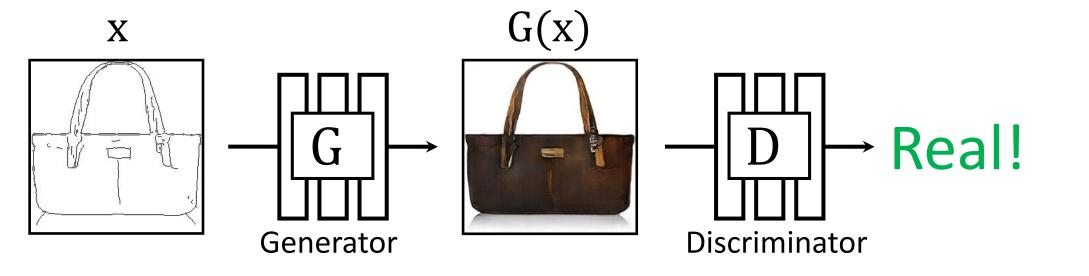
## $\min_{G} \max_{D} \mathbb{E}_{z,x}[\log D(G(z)) + \log(1 - D(x))]$





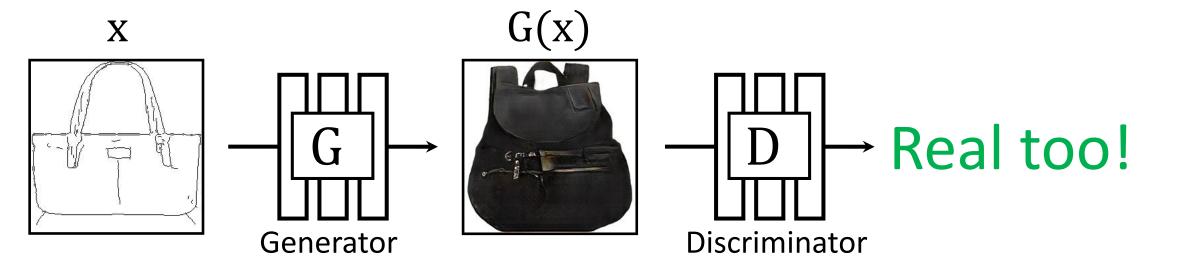
# $\min_{G} \max_{D} \mathbb{E}_{x,y}[\log D(G(x)) + \log(1 - D(y))]$





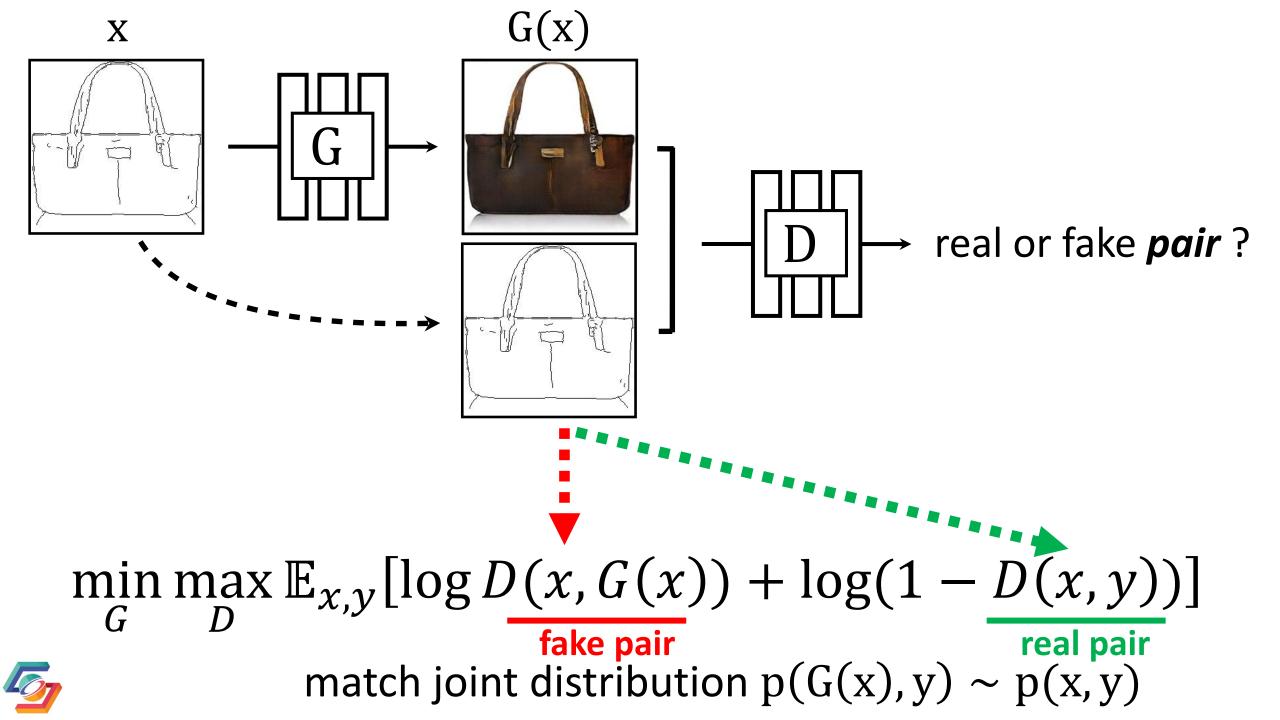
# $\min_{G} \max_{D} \mathbb{E}_{x,y}[\log D(G(x)) + \log(1 - D(y))]$





## $\min_{G} \max_{D} \mathbb{E}_{x,y}[\log D(G(x)) + \log(1 - D(y))]$



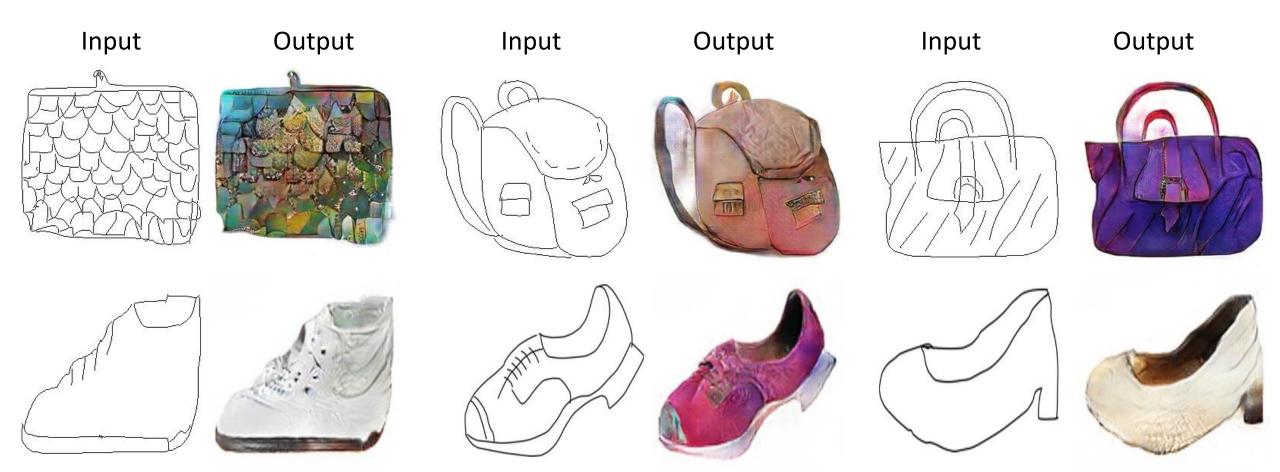


### $Edges \rightarrow Images$



Edges from [Xie & Tu, 2015]

### Sketches $\rightarrow$ Images



Trained on Edges  $\rightarrow$  Images

Data from [Eitz, Hays, Alexa, 2012]



## **Decomposition into Steps: FrankenGAN**







Slide Credit: FrankenGAN, Kelly and Guerrero et al.

## **Decomposition into Steps: FrankenGAN**





## **GAN Dissection**

**Question:** How does a GAN create an image? What do individual neurons do? **Insight:** Neurons are specialized to create objects of specific types



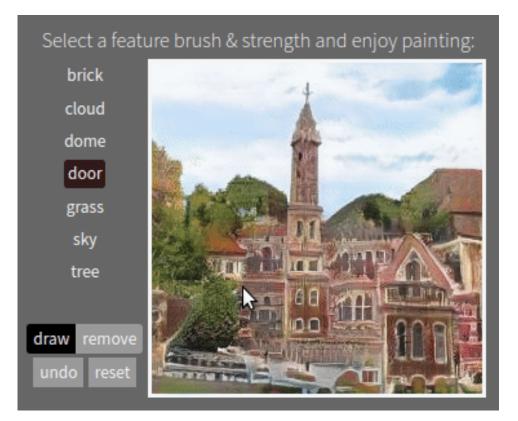




Image Credit: GAN Dissection: Visualizing and Understanding Generative Adversarial Networks, Bau et al.

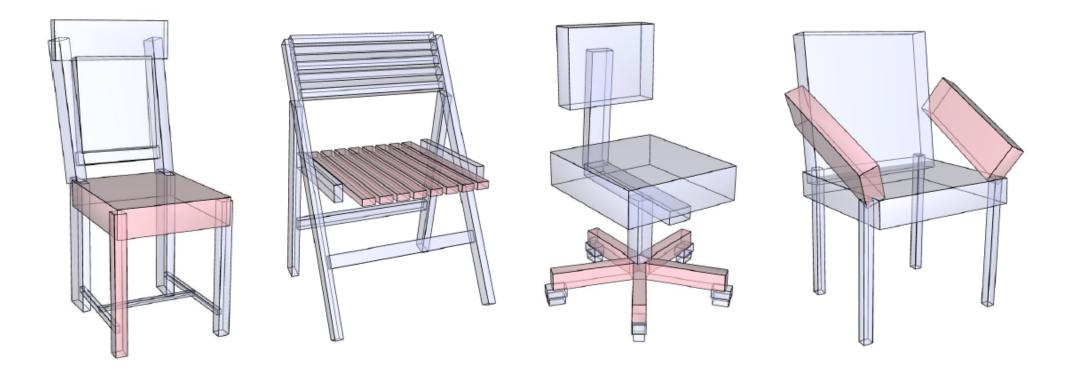
## **Open Problems**

- More control
- Irregular data
- GAN training convergence
- Evaluating GANs





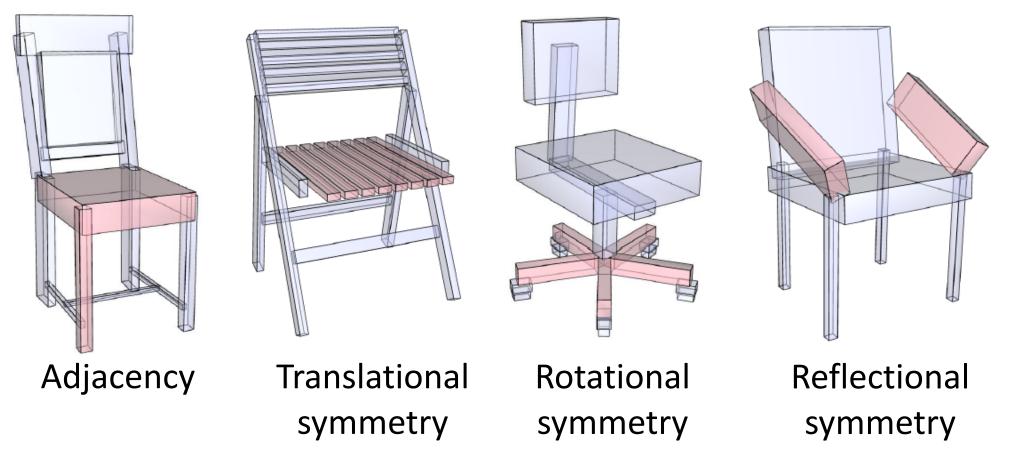
#### Space of chairs?







Part bounding boxes and their relationships represent a shape

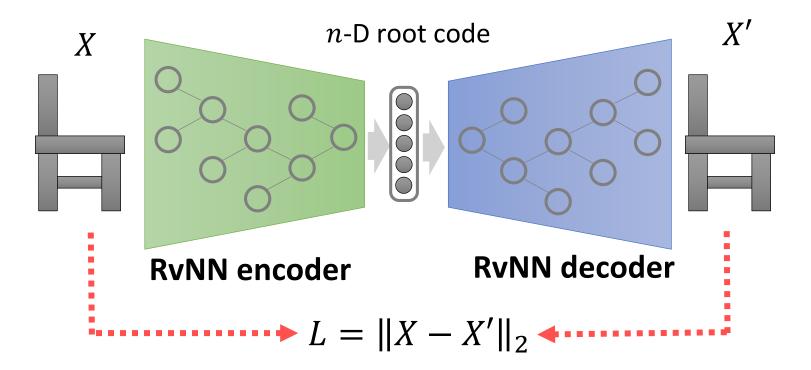




Slide Credit: GRASS: Generative Recursive Autoencoders for Shape Structures, Li et al.

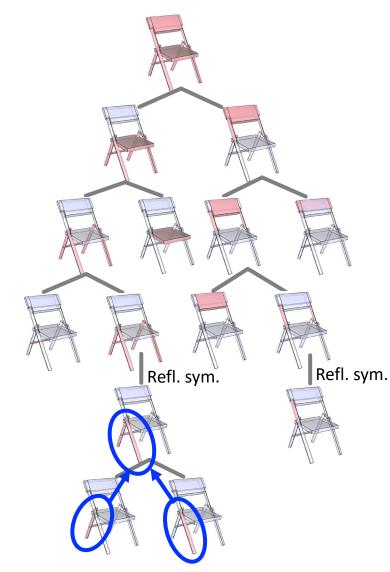
## **GRASS** Training

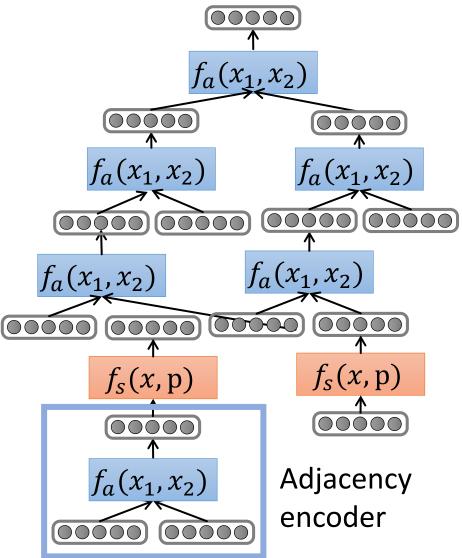
VAE using a hierarchical encoder and decoder





## **GRASS Hierarchical Encoder**

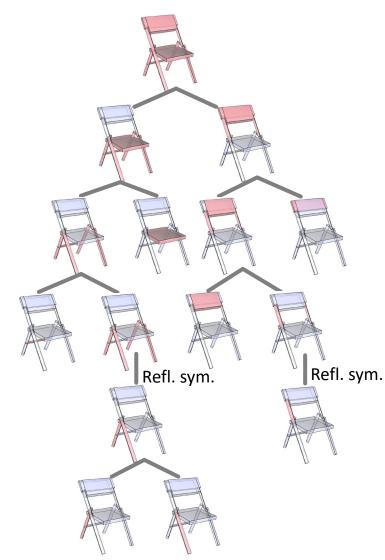


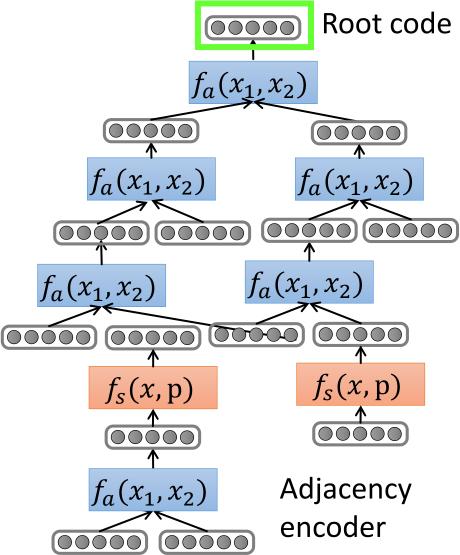




Bottom-up merging

## **GRASS Hierarchical Encoder**



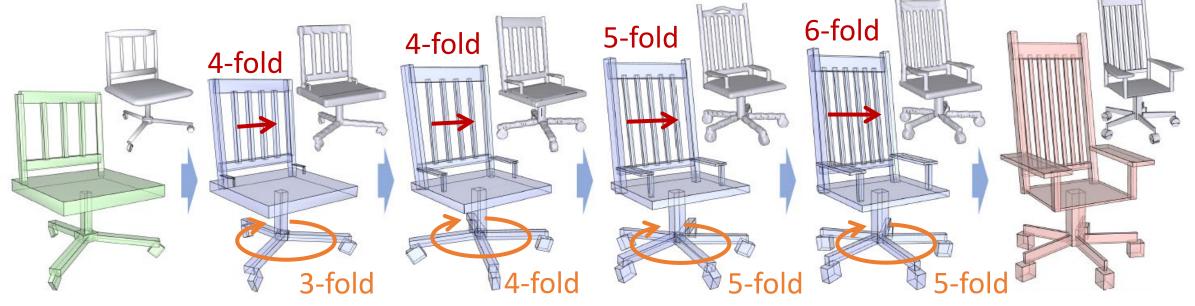


Bottom-up merging

Slide Credit: GRASS: Generative Recursive Autoencoders for Shape Structures, Li et al.

## **GRASS Results**

#### interpolation



free generation



Slide Credit: GRASS: Generative Recursive Autoencoders for Shape Structures, Li et al.

## StructureNet

• Consistent structure across the dataset

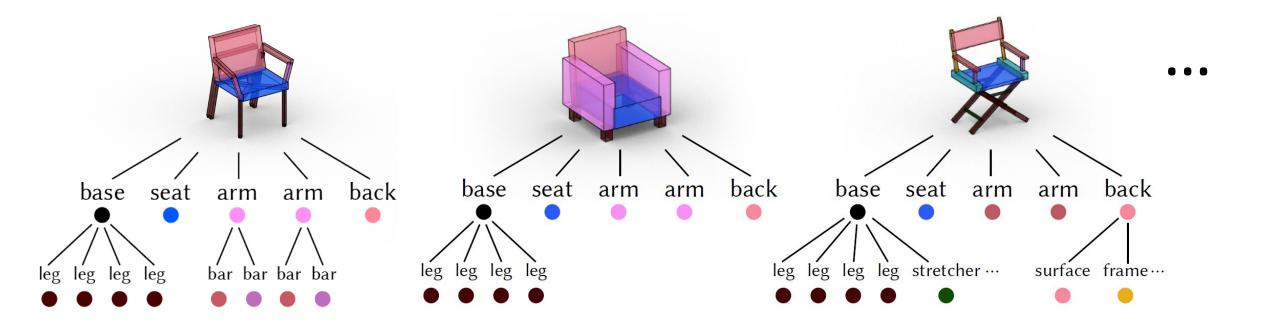




Image Credit: StructureNet: Hierarchical Graph Networks for 3D Shape Generation, Mo and Guerrero et al.

## StructureNet

- Consistent structure across the dataset
- Richer structure

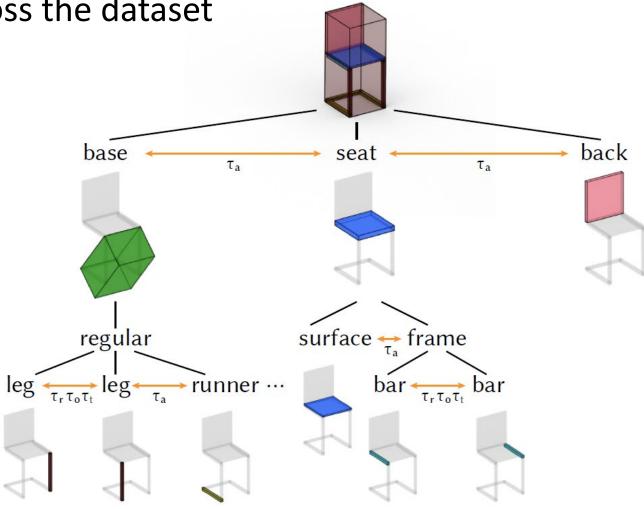




Image Credit: StructureNet: Hierarchical Graph Networks for 3D Shape Generation, Mo and Guerrero et al.

## **Hierarchical Graph Networks as Encoder and Decoder**

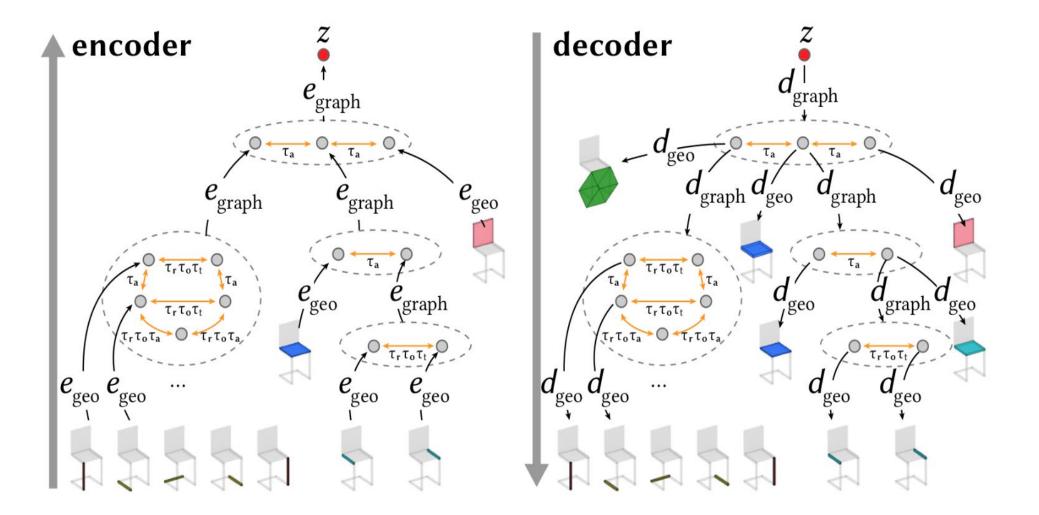
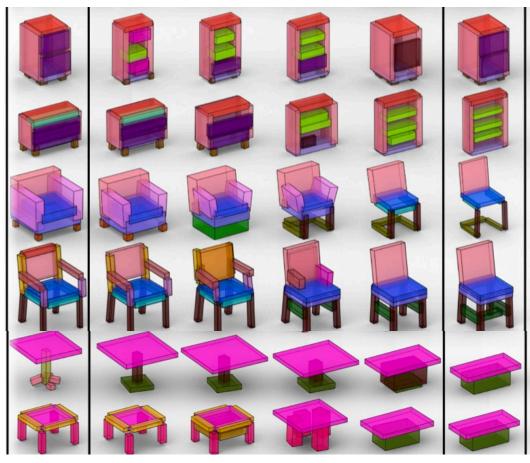




Image Credit: StructureNet: Hierarchical Graph Networks for 3D Shape Generation, Mo and Guerrero et al.

## **StructureNet Results**

#### interpolation



free generation





Image Credit: StructureNet: Hierarchical Graph Networks for 3D Shape Generation, Mo and Guerrero et al.

## **Open Problems**

- More control
- Irregular data
- GAN training convergence
- Evaluating GANs



## **GAN Training Convergence**

GAN training can be unstable

- Generator and discriminator do now always converge (Nash equilibrium)
- Vanishing discriminator gradients
- Mode Collapse





## **Vanishing Discriminator Gradients**

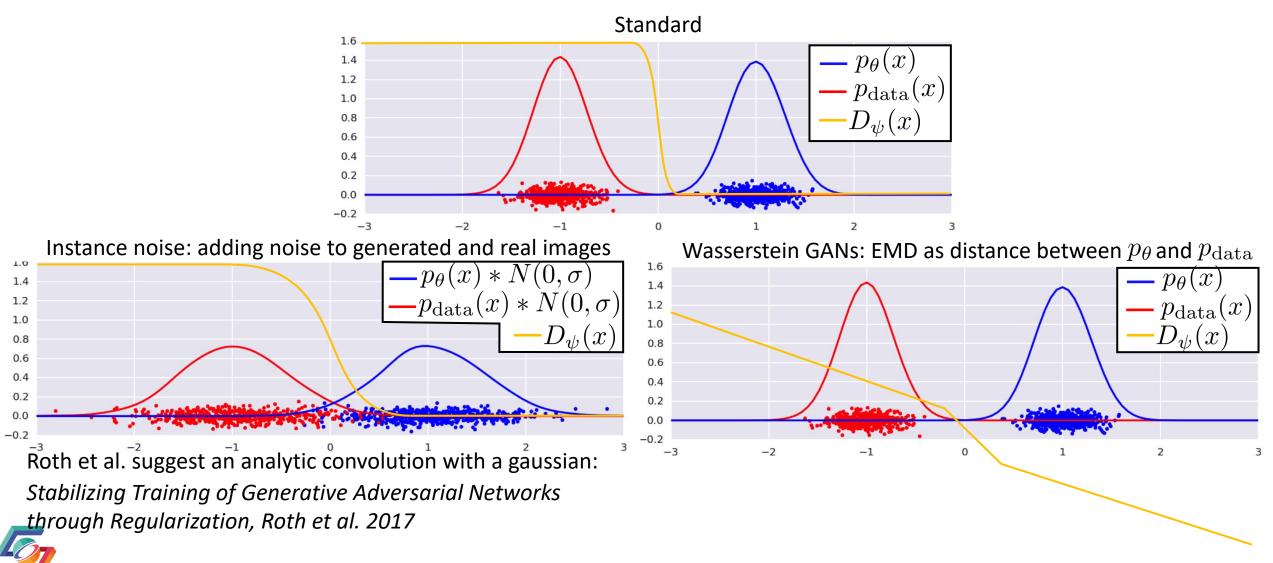


Image Credit: Amortised MAP Inference for Image Super-resolution, Sønderby et al.

## Mode Collapse

 $p_{ heta}$  only covers one or a few modes of  $p_{\mathrm{data}}$ 

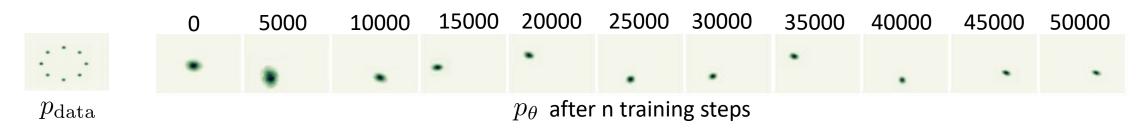




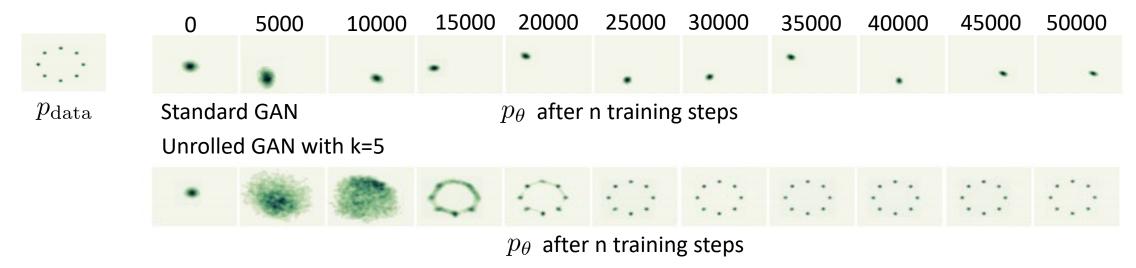


Image Credit: *Wasserstein GAN*, Arjovsky et al. *Unrolled Generative Adversarial Networks*, Metz et al.

## Mode Collapse

Solution attempts:

- Minibatch comparisons: Discriminator can compare instances in a minibatch (*Improved Techniques for Training GANs*, Salimans et al.)
- Unrolled GANs: Take k steps with the discriminator in each iteration, and backpropagate through all of them to update the generator



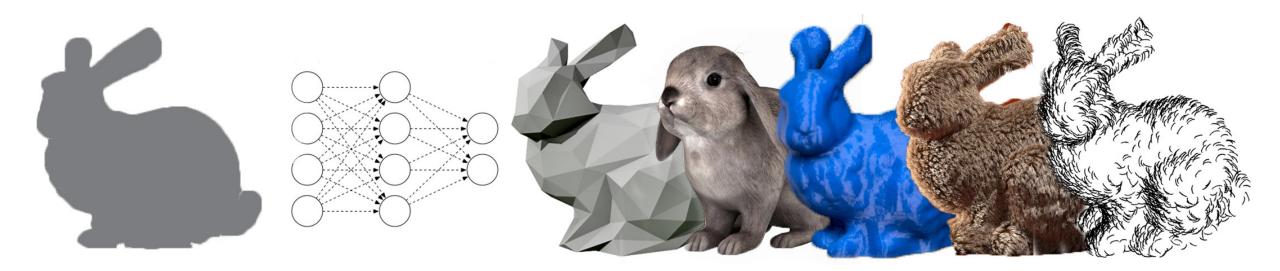


## Summary

- Autoencoders
  - Can create a feature space, but bad generators
- VAEs
  - Lower quality generated samples (usually blurry)
  - Relatively stable to train
- Normalized Flows
  - Better quality generated samples
  - Invertible
  - Relatively stable, but expensive to train
- GANs
  - Can not find a latent representation for a given sample (no encoder)
  - Usually better generators than VAEs
  - Currently unstable training (active research)



## **Course Information (slides/code/comments)**



#### http://geometry.cs.ucl.ac.uk/creativeai/



